# OXFORD

# Specification Analysis of Structural Credit Risk Models\*

# Jing-Zhi Huang<sup>1</sup>, Zhan Shi<sup>2</sup>, and Hao Zhou<sup>2</sup>

<sup>1</sup>Smeal College of Business, Pennsylvania State University and <sup>2</sup>PBC School of Finance, Tsinghua University

## Abstract

Empirical studies of structural credit risk models so far are often based on calibration, rolling estimation, or regressions. This paper proposes a GMM-based method that allows us to estimate model parameters and test model-implied restrictions in a unified framework. We conduct a specification analysis of five representative structural models based on the proposed GMM procedure, using information from both equity volatility and the term structure of single-name credit default swap (CDS) spreads. Our test results strongly reject the Merton (1974) model and two diffusionbased models with a flat default boundary. The other two models, one with jumps and one with stationary leverage ratios, do improve the overall fit of CDS spreads and equity volatility. However, all five models have difficulty capturing the dynamic behavior of both equity volatility and CDS spreads, especially for investment-grade names. On the other hand, these models have a much better ability to explain the sensitivity of CDS spreads to equity returns.

JEL classification: G12, G13, C51, C52

\* The authors would like to thank Amit Goyal (the editor), an anonymous referee, Jean Helwege, Anh Le, George Tauchen, Marliese Uhrig-Homburg; seminar participants at Arizona, Central University of Finance and Economics, Cheung Kong Graduate School of Business, China Europe International Business School, Lehigh, MIT, Shanghai University of Finance and Economics; and conference participants (and especially discussants) at the 2006 Econometric Society North American Winter Meeting in Boston (Viral Acharya), the 2006 Derivatives and Risk Management Conference at FDIC, the 2007 Federal Reserve Board Conference on Credit Risk and Credit Derivatives, Moody's 4th Annual Credit Risk Conference in Copenhagen (Rangarajan Sundaram), the 2007 Gutmann Center Symposium on Credit Risk and the Management of Fixed-Income Portfolios in Vienna (Thomas Dangl), the 2007 China International Conference in Finance (Yi Zhou), the 2008 Mitsui Symposium at Michigan (Ren-Raw Chen), the 2008 Singapore International Conference on Finance (Jan Ericsson), the 2008 Northern Finance Association Meeting in Manitoba (Pascal Francois), and the 2009 American Finance Association Meeting in San Francisco (Ilya Strebulaev) for helpful comments and suggestions. We also thank Terry O'Brien for his editorial assistance. J.-Z.H. acknowledges a Smeal Summer Research Grant for partial support.

© The Author(s) 2019. Published by Oxford University Press on behalf of the European Finance Association. All rights reserved. For permissions, please email: journals.permissions@oup.com **Keywords:** Structural credit risk models, GMM, Consistent specification analysis, Credit default swaps, CDS hedging, Jump-diffusion models, Stochastic asset volatility, Realized equity volatility

Received April 1, 2017; accepted February 4, 2019 by Editor Amit Goyal.

## 1. Introduction

A widely used approach to credit risk modeling is the so-called structural method, originated from Black and Scholes (1973) and Merton (1974). A growing literature has empirically examined the implications of structural models for various financial variables, such as credit spreads (Eom, Helwege, and Huang, 2004), real default probabilities (Leland, 2004), both spreads and default rates (Huang and Huang, 2012), hedge ratios (Schaefer and Strebulaev, 2008), corporate bond return volatility (Bao and Pan, 2013), and prices of different (de facto) seniority levels (Bao and Hou, 2017). The main empirical methods used in this literature include calibration, rolling estimation, and regressions. Although these methods are intuitive, easy to implement, and widely used, it is known that, from a statistical point of view, they have some limitations.

In this study, we propose an alternative approach to testing structural credit risk models. More specifically, we construct a specification test based on certain model-implied variables, such as credit spreads and equity volatility. By assuming that both equity and credit markets are efficient and that the underlying structural model is correct, we obtain moment restrictions on model parameters (e.g., asset volatility and default boundary). We then use generalized method of moments (GMMs) of Hansen (1982) to conduct parameter estimation as well as a specification analysis of the structural model. Three aspects of this GMMbased specification test are worth noting. First, the test provides consistent econometric estimation of the model parameters. Second, the test allows us to conduct a precise inference on whether the model is rejected or not in the data. Third, the test is based on the joint behavior of time-series of asset dynamics and cross-sectional pricing errors for structural models.

For illustration, we apply the proposed approach to five affine, representative structural models of default that incorporate various economic considerations. For each of the five models, we construct its moment conditions using equity volatility and term structures of single-name credit default swap (CDS) spreads. We then test whether all the restrictions of the model are satisfied using the GMM, based on the model-implied CDS spreads and equity volatility. By minimizing the effect of measurement error from using firm characteristics, this test attributes the test results mostly to the specification error. Lastly, we examine the ability of the model to explain equity volatility, the CDS term structure, default rates, sensitivity of CDS spreads to equity returns, etc.

For the purpose of this study, using CDS data has at least two advantages over using corporate bond data. One is that CDS spread curves are readily available. The other is that in general the CDS market is more liquid than the corporate bond market. We include equity return volatility in moment conditions mainly because few empirical studies have examined the implications of structural models for this second moment variable.<sup>1</sup> In other

<sup>1</sup> There is ample empirical evidence that individual equity volatility is time-varying and stochastic (see, e.g., the survey articles by Bollerslev, Chou, and Kroner, 1992; Bollerslev, Engle, and Nelson,

words, while equity volatility is usually used as an input in the empirical literature on structural models, this study treats equity volatility as an output of the models. Additionally, we use the so-called "model-free" realized equity volatility in our empirical analysis. As it is estimated using intraday high-frequency equity returns and involves no overlapping observations, realized volatility is more accurate than volatility estimates based on daily or monthly returns. Moreover, the use of the latter estimates implies that structural models are implicitly assumed to be able to fit perfectly the time series of equity volatility involving overlapping observations. Lastly, focusing on realized equity volatility is consistent with the evidence that volatility dynamics have a strong potential to help explain credit spreads (e.g., Zhang, Zhou, and Zhu, 2009).

For reasons of tractability and comparison, we focus on the Merton (1974) model and its four extensions with an exogenous default boundary in this study.<sup>2</sup> The four barriertype models include the Black and Cox (1976) (BC) model with a flat default boundary, the Longstaff and Schwartz (1995) (LS) model with stochastic interest rates, the Collin-Dufresne and Goldstein (2001) (CDG) model with a stationary leverage, and the double-exponential jump diffusion (DEJD) model used in Huang and Huang (2002) and Kou (2002).<sup>3</sup>

We test each of the five models using a sample of 93 industrial companies in the USA that have a balanced panel of monthly realized equity volatility and CDS term structure over the period January 2002–December 2004. As the main purpose of our empirical analysis is to illustrate the proposed specification test of structural models, the choice of the sample period is not essential to the analysis. Nonetheless, this post dot-com bubble (and also post the Enron collapse) period includes many major corporate defaults and "actions." On the other hand, relatively "quiet" compared with the recent financial crisis, this sample period is less subject to illiquidity concern documented for the corporate bond market during the financial crisis (Dick-Nielsen, Feldhütter, and Lando, 2012; Friewald, Jankowitsch, and Subrahmanyam, 2012).

Our GMM-based specification tests strongly reject the Merton, BC, and LS models. The DEJD model is found to significantly outperform these three models. The CDG model is the best performing one among the five models: the model is not rejected by the GMM test for more than half of the 93 companies in our sample. Nonetheless, the fact that both the DEJD and CDG models are still rejected by a substantial number of firms in the sample indicates that something is missing in these models.

The pricing error results from the five models provide similar evidence. On the one hand, jumps and dynamic leverage help improve the model fit for investment-grade (IG) and high-yield (HY) names, respectively. On the other hand, the five models all substantially underestimate both equity volatility and CDS spreads for IG names during 2002 when credit risk is relatively high. In other words, these models have difficulty in capturing the

1994). This stylized fact should be taken into account in examining structural models that consider equity to be a contingent claim on the underlying firm asset value.

- 2 To be more precise, the Merton model implemented in this study is the "extended Merton model" tested in Eom, Helwege, and Huang (2004). A similar model is also studied in Bao and Pan (2013).
- 3 Kou (2002) develops the first DEJD-based equity option pricing model. Concurrently, Ramezani and Zeng (2007) use the DEJD to model individual stock returns. Huang and Huang (2002, 2012) provide the first application of the DEJD model in credit risk. Other examples using the DEJD-based structural model include Cremers, Driessen, and Maenhout (2008); Bao (2009); and Chen and Kou (2009).

dynamic behavior of both equity volatility and CDS spreads, especially for IG names-even

(2016) focus on the cross-section of spreads implied by structural models. Examples of studies that link CDS premiums with variables from structural models using a regression analysis include Ericsson, Jacobs, and Oviedo (2009) and Zhang, Zhou, and Zhu (2009).

This paper differs from the aforementioned studies in at least two aspects. First, it proposes and conducts a GMM-based specification test of structural models. In particular, equity volatility is treated as an output variable in the proposed test. Second, as a result, this study uses a different method for model parameter estimation. Consider, for example, asset volatility (a driving force behind the firm default risk). Estimates of this important parameter, used in the empirical analysis of structural models, include those calibrated to historical equity volatility and equity value (Jones, Mason, and Rosenfeld, 1984), option-implied equity volatilities (Hull, Nelken, and White, 2005), and default rates (Huang and Huang, 2012); those estimated using historical equity and bond return volatilities (Schaefer and Strebulaev, 2008); and those implied by corporate bond prices (Eom, Helwege, and Huang, 2004) or by CDS spreads (Kelly, Manzo, and Palhares, 2016). In our analysis, asset volatility is estimated using the GMM method with CDS term structures and realized equity volatility.

Our paper also fits in the literature on the implications of structural models for second moment variables (such as equity return volatility) as well as on their impact on credit risk. For instance, Campbell and Taksler (2003) find that idiosyncratic equity volatility can explain a significant part of corporate bond yield spreads cross-sectionally. Huang and Huang (2012) conjecture that a structural model with stochastic asset volatility and jumps may help solve the credit spread puzzle. Huang (2005) considers an affine class of structural models with both stochastic asset volatility and Lévy jumps. Based on regression analysis, Zhang, Zhou, and Zhu (2009) provide empirical evidence that a stochastic asset volatility model may improve the model performance. Perrakis and Zhong (2015) extend the Leland and Toft (1996) model to allow for constant elasticity of variance. Kelly, Manzo, and Palhares (2016) provide more recent evidence of stochastic asset volatility; see also Du, Elkamhi, and Ericsson (2018) and McQuade (2018). In a closely related study, Bao and Pan (2013) focus on corporate bond return volatility and document that the volatility implied from the Merton (1974) model with stochastic interest rates underestimates substantially the observed corporate bond return volatility.

The literature on hedge ratios implied by structural models goes back to Schaefer and Strebulaev (2008), who find that on average, the Merton model-implied sensitivity of a firm's corporate bond returns to its equity returns is not statistically different from the insample empirically estimated hedge ratios. Bao and Hou (2017) investigate how a corporate bond's position in its issuer's maturity structure affects its sensitivity to the issuer's equity return. They show that both the direction and the magnitude of this *de facto* seniority effect are consistent with what are implied from an extended Merton model. Huang and Shi (2016) document that on average, the Merton model also captures the in-sample sensitivity of corporate bond spreads to equity returns. In addition, they examine the actual hedging performance of model-implied sensitivities of both corporate bond returns and spreads, thereby providing an out-of-sample test of the explanatory power of hedging portfolios. On the other hand, focusing on pairs of stock returns and CDS spread changes with the same underlying over a short interval (e.g., 5 days), Kapadia and Pu (2012) find that about 41% of stock returns are associated with CDS spread changes in the same direction, as opposed to the prediction of the Merton model. This discrepancy is shown to reflect an imperfect equity-credit market integration at short horizons. Huang, Rossi, and Wang (2015) find similar results based on pairs of stock and corporate bond returns and also provide evidence that equity market sentiment helps improve the equity-credit market integration, especially after the financial crisis.

In this study we examine not only hedge ratios of CDS spreads but also actual hedging performance of structural models. In addition, we go beyond the Merton model.

As mentioned before, we use CDS data instead of corporate bond data in our empirical analysis, partly to avoid the liquidity problem in the latter market. For evidence on corporate bond illiquidity, see Bao, Pan, and Wang (2011); Bongaerts, de Jong, and Driessen (2017); Chen, Lesmond, and Wei (2007); Das and Hanouna (2009); Han and Zhou (2016); Helwege, Huang, and Wang (2014); Longstaff, Mithal, and Neis (2005); Mahanti *et al.* (2008); Schestag, Schuster, and Uhrig-Homburg (2016), among others. In addition, using CDS term structures facilitates the implementation of the proposed GMM-based test—it is known that data on term structures of corporate bond spreads are not easily available for individual firms. For a recent survey on the CDS market, see Augustin *et al.* (2016).

Lastly, note that there is a large theoretical literature on structural credit risk modeling (see, e.g., Huang and Huang, 2012; Sundaresan, 2013, and references therein), although for tractability and comparison we consider only five structural models in our empirical analysis. For example, the class of endogenous-default models, not considered in this paper, includes those without strategic default, such as Geske (1977) and Leland and Toft (1996), and strategic default models, such as Anderson and Sundaresan (1996), Mella-Barral and Perraudin (1997), Acharya and Carpenter (2002), and Acharya *et al.* (2006, 2019). Strategic default models of perpetual bonds are considered in Huang and Huang (2012). Endogenous default models with finite maturity of Geske (1977) and Leland and Toft (1996) are examined in Eom, Helwege, and Huang (2004). Another example not covered in this paper is the Duffie and Lando (2001) model with incomplete accounting information. Additionally, François and Morellec (2004) examine the impact of the US bankruptcy procedure on risky debt prices. He and Xiong (2012) and He and Milbradt (2014) consider both rollover risk and corporate bond illiquidity.

## 3. Affine Structural Credit Risk Models

In this section, we first review the five structural models to be tested in our specification analysis. We then discuss the model implications for CDS spreads, equity volatility, and sensitivities of CDS spreads to equity return.

#### 3.1 Models

Although the five models differ in certain economic assumptions, they all belong to the class of affine structural credit risk models and can be considered to be different specifications of one single model.

Let *V* be the firm's asset process, *K* the default boundary, and *r* the default-free interest rate process. Assume that, under a risk-neutral measure  $\mathbb{Q}$ ,

$$\frac{\mathrm{d}V_t}{V_{t-}} = (r_t - \delta)\mathrm{d}t + \sigma_{\nu}\mathrm{d}W_t^{\mathbb{Q}} + \mathrm{d}\left[\sum_{i=1}^{N_t^{\mathbb{Q}}} \left(Z_i^{\mathbb{Q}} - 1\right)\right] - \lambda^{\mathbb{Q}}\xi^{\mathbb{Q}}\mathrm{d}t,\tag{1}$$

$$d\ln K_t = \kappa_\ell \left[ -\nu - \phi(r_t - \theta_r) - \ln \left( K_t / V_t \right) \right] dt,$$
(2)

$$dr_t = (\alpha - \beta r_t)dt + \sigma_r dW_{rt}^Q, \qquad (3)$$

where  $\delta$ ,  $\sigma_{\nu}$ ,  $\kappa_{\ell}$ ,  $\nu$ ,  $\phi$ ,  $\alpha$ ,  $\beta$ ,  $\sigma_r$ , and  $\theta_r = \alpha/\beta$  are constants, and  $W^Q$  and  $W^Q_r$  are both onedimensional standard Brownian motion under the risk-neutral measure and are assumed to have a constant correlation coefficient of  $\rho$ . In Equation (1), the process  $N^Q$  is a Poisson process with a constant intensity  $\lambda^Q > 0$ , the  $Z_i^Q$ s are i.i.d. random variables, and  $Y^Q \equiv$  $\ln (Z_1^Q)$  has a double-exponential distribution with a density given by

$$f_{Y^{Q}}(y) = p_{u}^{Q} \eta_{u}^{Q} e^{-\eta_{u}^{Q} y} \mathbf{1}_{\{y \ge 0\}} + p_{d}^{Q} \eta_{d}^{Q} e^{\eta_{d}^{Q} y} \mathbf{1}_{\{y < 0\}}.$$
 (4)

In Equation (4), parameters  $\eta_u^Q, \eta_d^Q > 0$  and  $p_u^Q, p_d^Q \ge 0$  are all constants, with  $p_u^Q + p_d^Q = 1$ . The mean percentage jump size  $\xi^Q$  is given by

$$\xi^{Q} = \mathbf{E}^{Q} \left[ \mathbf{e}^{Y^{Q}} - 1 \right] = \frac{p_{u}^{Q} \eta_{u}^{Q}}{\eta_{u}^{Q} - 1} + \frac{p_{d}^{Q} \eta_{d}^{Q}}{\eta_{d}^{Q} + 1} - 1.$$
(5)

All five models are special cases of the general specification in Equations (1)–(5). For instance, if the jump intensity is zero, then the asset process is a geometric Brownian motion. This specification is used in the four diffusion models, namely, the models of Merton (1974), BC, LS, and CDG.

Regarding the specification of the default boundary *K*, it is a point at the bond maturity in the (original) Merton model and a discrete barrier in the extended Merton model. If  $\kappa_{\ell}$  is set to be zero, then the default boundary is flat (a continuous barrier), an assumption made in the BC, LS, and the DEJD models.

If  $\alpha$ ,  $\beta$  and  $\sigma_r$  in Equation (3) are zero, then the interest rate is constant. This leads to the three one-factor models: the Merton, BC, and DEJD models. If both  $\beta$  and  $\sigma_r$  are greater than zero, then we have the two-factor models, LS and CDG, where the dynamics of the risk-free rate follow the Vasicek model specified in Equation (3). Additionally, the CDG model assumes that  $\kappa_{\ell} > 0$  and that the default boundary follows the mean-reverting specification in Equation (2).

Lastly, we obtain the DEJD model if the jump intensity is strictly positive, the risk-free rate is constant, and the default boundary is flat.

We assume a constant recovery rate for comparison with other studies and also because the CDS database that we use includes recovery rate estimates for each CDS contract.

#### 3.2 Valuation of Single-Name CDS Contracts

Under each of the five structural models, it is straightforward to calculate the CDS spread. Let Q(0, T) denote the survival probability over (0, T] under the *T*-forward measure. Then the CDS spread of a *T*-year CDS contract is given by

$$\operatorname{cds}(0,T) = \frac{(1-R)E^{\mathbb{Q}}\left[e^{-\int_{0}^{\tau} r(u)du}I_{\{\tau < T\}}\right]}{\sum_{i=1}^{4T}B(0,T_{i})Q(0,T_{i})/4},$$
(6)

where *R* is the recovery rate,  $B(0, \cdot)$  the default-free discount function,  $\tau > 0$  the default time,  $I_{\{\cdot\}}$  the indicator function, and  $E^{\mathbb{Q}}[\cdot]$  the expectation under the risk-neutral measure. To simplify the computation, we follow the literature to make the standard assumption

that the settlement of the contract occurs on the next payment day. It then follows from Equation (6) that

$$\operatorname{cds}(0,T) = \frac{(1-R)\sum_{i=1}^{4T} B(0,T_i)[Q(0,T_{i-1}) - Q(0,T_i)]}{\sum_{i=1}^{4T} B(0,T_i)Q(0,T_i)/4}.$$
(7)

As a result, the implementation of a structural model amounts to the calculation of the survival probability  $Q(0, \cdot)$ . In the Merton (1974) and BC models,  $Q(0, \cdot)$  has closed-form solutions. The survival probabilities in the LS, CDG, and DEJD models do not have known closed-form solutions but can be calculated numerically (see, e.g., Huang and Huang, 2012, for details).

In addition to CDS spreads, other model-implied credit market variables include CDS spread changes, CDS volatilities, corporate bond return volatilities, etc. However, corporate bond volatilities have a sizable illiquidity component and CDS volatilities might also be a bit high compared with fundamentals (Bao and Pan, 2013; Bao *et al.*, 2015). Therefore, given the purpose of this study, we do not consider these second moment variables in credit markets in our empirical analysis.

#### 3.3 Equity Market Variables

In this subsection we focus on more liquid equity market variables, which have received relatively little attention in the empirical literature on structural models.

Consider equity return volatility first. As pointed out by Merton (1974), the function relating the equity volatility and asset volatility is also model-dependent

$$\sigma_E(t) = \sigma_v \frac{V_t}{E_t} \frac{\partial E_t}{\partial V_t},\tag{8}$$

where  $E_t$  is the time-*t* equity value, and Equation (8) applies to equity volatility of the continuous diffusion component for the DEJD model. Note that  $\sigma_E(t)$  is time-varying even if  $\sigma_v$ is assumed to be constant.

Next, we consider comovements between CDS and equity, in order to better understand their relative pricing as well as how to hedge their common exposures across markets. Following Schaefer and Strebulaev (2008), we express the sensitivity of a CDS spread to the underlying equity return in terms of their partial derivatives with respect to the underlying firm value

$$\Delta_{E,t}^{\text{cds}} \equiv \frac{\partial \text{cds}(t,T)}{\partial E_t / E_t} = \frac{\partial \text{cds}(t,T) / \partial V_t}{\partial E_t / \partial V_t} E_t.$$
(9)

As illustrated in Sections 4.3 and 6.5, both  $\partial cds(t,T)/\partial V_t$  and  $\partial E_t/\partial V_t$  are functions of  $\partial Q(t,\cdot)/\partial V_t$ . As such, once  $Q(t,\cdot)$  is known,  $\Delta_{E,t}^{cds}$  can be calculated using Equation (9).

Unlike its counterpart for corporate bonds, the hedge ratio for a CDS contract is not the same as its sensitivity to equity. Instead, the latter hedge ratio is defined as the dollar change in the value of the CDS contract for each percentage change in the equity value

$$b_{E,t}^{\rm cds} \equiv \frac{\partial V_t^{\rm cds}}{\partial E_t / E_t} = \frac{\partial {\rm cds}(t,T)}{\partial E_t} E_t D_t^{\rm cds},\tag{10}$$

where  $V_t^{\text{cds}}$  denotes the time-*t* value of a CDS contract with a notional of \$10 million, and  $D_t^{\text{cds}} = \sum_{i=1}^{4T} B(t, T_i) Q(t, T_i) \times 2.5$  million is defined as the change in the mark to market value (in million) for each unit of change in the quoted spread.<sup>5</sup>

## 4. A Specification Test of Structural Models

In this section, we propose a specification test of structural models under the GMM framework of Hansen (1982). We first review the framework albeit using moment conditions pertinent to structure models. We then discuss finite-sample properties of GMM. Lastly, we focus on the implementation of the proposed specification test.

#### 4.1 GMM Estimation of Structural Credit Risk Models

As mentioned before, the fundamental pricing relationship implied by a structural model has implications for credit spreads, equity volatility, default probabilities, leverage, corporate bond returns, corporate bond return volatility, hedge ratios, etc. To evaluate the model, we first estimate the model parameters that may include asset volatility, default boundary, asset jump intensity, or dynamic leverage coefficients. Let  $\theta$  denote the vector of the model parameters to be estimated and  $\hat{\theta}$  the estimated vector. We then take  $\hat{\theta}$  as given and examine the pricing performance of the (estimated) model. Below we describe how to implement this idea using GMM, following largely Cochrane (2009).

As noted before, we focus on model-implied CDS spreads and equity volatility in the empirical analysis. Let  $cds(t, t + T_m)$  and  $\sigma_E(t)$  be the time-*t* CDS spread with maturity  $t + T_m$  and equity volatility under a given structural model, specified in Equations (7) and (8), respectively. Let  $cds(t, t + T_m)$  and  $\tilde{\sigma_E}(t)$  be the time-*t* observed counterparts of  $cds(t, t + T_m)$  and  $\sigma_E(t)$ . Consider the following vector of pricing errors (so-called moment conditions):

$$f(\theta, t) = \begin{bmatrix} \widetilde{\operatorname{cds}}(t, t + T_1) - \operatorname{cds}(t, t + T_1) \\ \cdots \\ \widetilde{\operatorname{cds}}(t, t + T_M) - \operatorname{cds}(t, t + T_M) \\ \widetilde{\sigma_E}(t) - \sigma_E(t) \end{bmatrix},$$
(11)

where *M* denotes the number of CDS contracts with different maturities and the same underlying firm. Under the null hypothesis that the model is correctly specified, we have

$$E[f(\theta, t)] = 0. \tag{12}$$

To test the cabody e hsy postes is, we construct that time 2 eries of. 1 6 5 1 0 T D

 $M > \dim(\theta) - 1$  as in our case; that is, there are more moment conditions than parameters. In this case, we can pick  $\theta$  such that linear combinations of the moment conditions are zero. This is a challenging task, however, especially given that both CDS spreads and equity volatility are allowed to be observed with measurement errors in this analysis. As such, we choose  $\theta$  to minimize a quadratic function of the pricing errors. Doing so leads to the so-called GMM estimator:

$$\hat{\theta} = \arg\min g(\theta, T)' W(T) g(\theta, T), \tag{14}$$

where W(T), a weighting matrix, denotes the asymptotic covariance matrix of  $g(\theta, T)$  (Hansen, 1982). With mild regularity conditions,  $\hat{\theta}$  is  $\sqrt{T}$ -consistent and asymptotically normally distributed, under the null hypothesis.

Furthermore, we implement the iterative GMM. That is, we begin with W(T) = I, the identity matrix, and estimate  $\theta$ . Next, we use a heteroscedasticity robust estimator for the variance–covariance matrix W(T) that allows for autocorrelation in the errors (Newey and West, 1987), and obtain a new  $\hat{\theta}$ . We repeat this procedure until it converges.

Given  $\hat{\theta}$  that minimizes the quadratic form specified in Equation (14), we can then examine how well the candidate model fits. If the pricing errors are "large" under the appropriately defined GMM metric, the candidate model specification will be rejected. Formally, we conduct the following test:

$$J_T = T \min_{\alpha} g(\theta, T)' W(T) g(\theta, T) \sim \chi^2(N^{\text{oi}}), \tag{15}$$

where  $N^{oi} = M + 1 - \dim(\theta)$ , the degree of freedom of the  $\chi^2$ -distribution, equals the number of overidentifying moment conditions. As a result, the GMM  $J_T$ -test allows for an omnibus test of the overidentifying restrictions.

#### 4.2 Finite-Sample Properties of GMM

The  $I_T$ -test specified in Equation (15) is an asymptotic test. Several studies have examined finite-sample properties of GMM estimators applied to asset pricing models, although the literature has focused mainly on consumption-based models and linear factor models in the equity market (see, e.g., Hall, 2005, and references therein). For instance, Tauchen (1986) considers the Hansen and Singleton (1982) consumption-based asset pricing model and examines the behavior of the two-step GMM estimator using one asset in the estimation. He finds that the bias of the estimator tends to increase as the degree of overidentification  $(N^{\circ 1})$  increases but the empirical sizes of the  $I_T$ -test tend to be close to the asymptotic value. Kocherlakota (1990) extends the analysis of Tauchen (1986) to multiple assets and his findings suggest that the iterated GMM estimator considerably improves the finite-sample behavior of GMM. Using predictive regression models for stock returns, Ferson and Foerster (1994) find that while sizes of the two-step GMM-based  $I_T$  statistics are often too large with finite samples, the iterated GMM approach has superior finite-sample properties. Hansen, Heaton, and Yaron (1996) consider a consumption-based asset pricing model where the representative agent's utility function allows for time non-separability. They find that when the number of the overidentifying restrictions is high (five), the asymptotic theory is far from the finite-sample property. Lettau and Ludvigson (2001) argue that the onestage GMM is more appropriate than the two-stage GMM with an estimated weighting matrix in the application pursued in their study-where the time-series sample is small relative to the cross-sectional sample size.

In our specification analysis, we test a given candidate model firm by firm. Based on the insights from the aforementioned studies, in order to mitigate the potential small sample problems in our tests, we need to keep the degree of overidentification minimal. As discussed in Section 4.3, for a given firm, the number of parameters to be estimated using the GMM ranges from one for the Merton model to four for the CDG model. As such, we use four CDS contracts and realized equity volatility (i.e., five moment conditions) with 36 monthly observations in each GMM test. That is, the degree of overidentification ranges from one in CDG to four in Merton in our tests. As a robustness check, we also test the Merton model using only one CDS contract and realized equity volatility such that the degree of overidentification is one. The number of time-series observations relative to the number of moment conditions is reasonably large, given that the latter is no more than five in our tests. Additionally, we implement the iterative GMM. Taken together, the findings of the aforementioned studies based on the equity market suggest that small sample problems are not a major concern in our GMM tests.

#### 4.3 Implementation

In this subsection, we discuss the implementation of the proposed GMM specification test.

compute the month-t vector  $f(\theta, t)$  of pricing errors defined in Equation (11)

#### 5.1 CDS Spreads

We use CDS data from Markit, a comprehensive data source that assembles a network of industry-leading partners who contribute information across several thousand credits on a daily basis. Based on the contributed quotes, Markit creates daily composite quotes for each CDS contract, which must pass the stale data test, flat curve test, and outlying data test. Together with the pricing information, the Markit data set also reports average recovery rates used by data contributors in pricing each CDS contract. In addition, an average of Moody's and S&P ratings is also included.

We begin with collecting all CDS quotes written on US entities (sovereign entities excluded) and denominated in US dollars. Following previous empirical studies on structural models (e.g., Eom, Helwege, and Huang, 2004), we exclude financial and utility sectors from the sample. In addition, we focus on senior unsecured CDS contracts and exclude the subordinated class of CDS contracts. Furthermore, we limit our sample to CDS contracts with modified restructuring clauses, as they are the most traded in the US market.

For the purpose of GMM estimation, we restrict the sample to those CDS names with at t,2X1Di1rs;i2;(17)

which converges to the integrated or average variance during period t. For a jump-diffusion model, the continuous component of equity volatility (squared) can be estimated with the so-called "bi-power variation" as follows:

$$\widetilde{\sigma_E}(t)^2 \equiv \frac{\pi}{2} \frac{1/\Delta}{1/\Delta - 1} \sum_{i=2}^{1/\Delta} |r_{t,i-1}^s| |r_{t,i}^s| \,.$$
(18)

As shown by Barndorff-Nielsen and Shephard (2004), such an estimator of realized equity volatility is robust to the presence of rare and large jumps.

Realized equity volatilities used in our analysis are estimated using TAQ data. The monthly realized variance is the sum of daily realized variances, constructed from the squares of intraday 5-min returns. Then, monthly realized volatility is just the square-root of the annualized monthly realized variance.

#### 5.3 Capital Structure and Asset Payout

Assets and liabilities are key variables in evaluating structural models of credit risk. The accounting information is obtained from Compustat on a quarterly basis and assigned to each month within the quarter. We calculate the firm asset as the sum of total liabilities plus market equity, where the market equity is obtained from the monthly CRSP data on shares outstanding and equity prices. Leverage ratio is estimated by the ratio of total liabilities to the firm's assets. The asset payout ratio is estimated by the weighted average of the interest expense and dividend payout. Both ratios are reported as annualized percentages.

#### 5.4 Risk-Free Interest Rates

Default-free interest rates used in the calculation of CDS spreads are estimated from the 3month LIBOR and interest rate swaps with maturities of 1, 2, 3, 5, 7, and 10 years. These data are available from the Federal Reserve H.15 Release.

#### 5.5 Summary Statistics

Table I provides summary statistics on firm characteristics and CDS spreads across either rating categories (panel A) or sectors (panel B). As can be seen from panel A1, our sample is concentrated in A-rated (25) and BBB firms (45), which account for 75% of the full sample, reflecting the fact that contracts on IG names dominate the CDS market. In terms of the average over both the time-series and cross-section in our sample, the 5-year CDS spread is 144 bps with a standard deviation of 3.18%, equity volatility 38.40% (annualized), the leverage ratio 48.34%, asset payout ratio 2.14%, and the quoted recovery rate 40.30%. As expected, the CDS spread, equity volatility, and leverage ratio all increase as the credit rating deteriorates. The recovery rate largely decreases as the rating deteriorates but has low variations.

Figure 1 plots both the term structure (from 1 to 10 years) and time evolution of the average CDS spreads over the full sample period January 2002–December 2004. Clearly, the average spreads show large variations and have a peak around late 2002.

Figure 2 plots both the 5-year CDS spreads (top panel) and equity volatility (bottom panel) by three different rating groups (AAA–A, BBB, and BB–CCC) over the full sample period. An inspection of the figure indicates that CDS spreads and equity volatilities appear to move together sometime during market turmoils but are only loosely related during quiet periods. The 5-year CDS spreads clearly have a peak in late 2002 across all three rating

Table I. Summary statistics on single-name corporate CDS spreads

This table reports summary statistics on the full sample of 93 single-name corporate CDS contracts, by either credit ratings (Panel A) or sectors (Panel B). Rating is the average of Moody's and Standard and Poor's ratings. Equity volatility is estimated using 5-min intraday returns. Leverage ratio is total liabilities divided by the total asset (total liability plus market equity). Asset payout ratio is the weighted average of dividend payout and interest expense over the

Sector	Sample fir	ms	Equity	Leverage	Asset	Recovery
	Number	Percentage	volatility (%)	ratio (%)	payout (%)	rate (%)
Communications	6	6.45	48.72	42.93	1.99	40.14
Consumer cyclical	32	34.41	38.95	48.56	2.01	40.45
Consumer staple	14	15.05	33.77	41.68	2.24	40.87
Energy	8	8.60	39.93	53.89	2.47	40.05
Industrial	18	19.35	40.24	53.90	2.01	39.90
Materials	11	11.83	32.85	49.34	2.73	41.35
Technology	4	4.30	45.22	40.20	1.29	38.95
Overall	93	100.00	38.68	48.39	2.14	40.39

#### Table I. Continued

Panel B1	Firm	characteristics	hv	sectors
ranci Dr.	1 11 111	characteristics	UY.	sectors

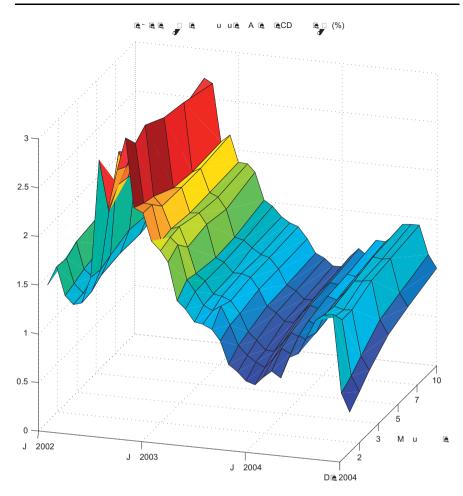
Panel B2: Average CDS spreads (%) by CDS maturities and sectors

	Maturity	of CDS				
	1-Year	2-Year	3-Year	5-Year	7-Year	10-Year
Communications	2.04	1.99	2.09	2.23	2.16	2.10
Consumer cyclical	1.57	1.58	1.58	1.61	1.62	1.66
Consumer staple	0.74	0.81	0.86	0.92	0.94	0.98
Energy	1.58	1.38	1.53	1.43	1.47	1.48
Industrial	1.29	1.38	1.41	1.46	1.48	1.53
Materials	0.92	0.96	1.03	1.10	1.14	1.20
Technology	1.38	1.43	1.48	1.48	1.51	1.52
Overall	1.34	1.36	1.40	1.44	1.45	1.49

Panel B3: Standard deviation of CDS spreads (%) by CDS maturities and sectors

Communications	4.82	4.13	4.58	4.74	4.33	3.80
Consumer cyclical	6.19	5.25	4.65	4.06	3.85	3.65
Consumer staple	2.08	2.21	2.18	2.10	2.02	1.92
Energy	5.60	3.66	4.80	3.32	3.45	3.14
Industrial	2.36	2.54	2.34	2.16	2.09	2.07
Materials	1.46	1.42	1.43	1.39	1.38	1.34
Technology	2.20	2.17	2.12	1.82	1.74	1.59
Overall	4.43	3.78	3.62	3.18	3.04	2.85

groups, although the BB-CCC group has another spike in late 2004. On the other hand, equity volatility is much higher in 2002 than the later part of the sample period and, in particular, has two huge spikes in 2002. There is clear evidence that equity volatility and credit spreads are intimately related (Campbell and Taksler, 2003), and the linkage appears to be nonlinear in nature (Zhang, Zhou, and Zhu, 2009). In the next section, we examine whether structural models can capture the dynamics of CDS spreads and equity volatility in our sample, among other things.



**Figure 1.** Average CDS spreads over the full sample period. This figure plots the average CDS spreads (in annualized percentage) of 93 firms in the full sample with maturities ranging from 1 to 10 years from January 2002 to December 2004.

# 6. Empirical Results

In this section, we present the results from our empirical analysis. We consider first the proposed GMM specification test of the five candidate models. We then examine the GMM estimates of model parameters and the pricing performance of the models. We also provide diagnostics on model specifications. Lastly, we focus on the model implications for hedge ratios and default probabilities.

### 6.1 GMM Specification Test

Our GMM specification test is based on the model-implied pricing relationship for CDS spreads and equity volatility. Table II reports the test results and, in particular, the number of firms where each of the five candidate models is *not* rejected, for the whole sample as well as subsamples by either credit ratings (panel A) or sectors (panel B). Note from the table that at the conservative 10% significance level, the number of firms (out of 93) where

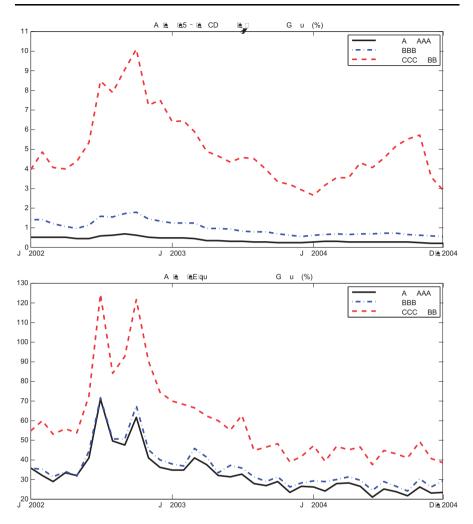


Figure 2. Time series of CDS spreads and equity volatility. This figure plots the average 5-year CDS spread (top panel) and the average realized equity volatility (bottom panel) by rating groups (A–AAA, BBB, and CCC–BB) over the period January 2002–December 2004. Realized equity volatility is estimated using 5-min intraday stock return data.

the given model is not rejected is 0, 1, 2, 13, and 52 for the Merton, BC, LS, DEJD, and CDG models, respectively. At the 1% significance level, none of the five models have a rejection rate of 100% and the number of firms with the model not being rejected increases to 5, 6, 12, 42, and 72 for the Merton, BC, LS, DEJD, and CDG models, respectively. Judged by these results on the number of firms where each of the five models is not rejected, the ranking of these models is as follows:

Merton 
$$\approx$$
 Black–Cox < LS  $\ll$  DEJD < CDG.

Notably, the two more recent models—the DEJD and CDG models—outperform the other three models. This finding implies that both jumps and time-varying leverage improve

dit risk models
l cre
structura
of
test
Specification
=
Table

This table reports the omnibus GMM test results of overidentifying restrictions under each of five structural models considered. The five moment conditions used in the test are constructed based on the pricing relationship for 1-, 3-, 5-, and 10-year CDS spreads and for the equity volatility estimated based on 5-min intraday data. The five model specifications considered include Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2002). Data used in the test are monthly CDS spreads and equity volatility from January 2002 to December 2004.

Metton         Black-Cox         Longstift-Schwattz         DFJD           Anticolution         Anti	Ź	Number of firms						Structu	Structural credit risk models estimated	risk mode	ls estimato	pa					
Chi-square values           4         3         3         3         3         2           16: $\frac{1}{59}$ $\frac{1}{53}$ <td< th=""><th></th><th></th><th></th><th>Merton</th><th></th><th>E</th><th>llack-Cox</th><th></th><th>Long</th><th>staff–Schv</th><th>vartz</th><th></th><th>DEJD</th><th></th><th></th><th>CDG</th><th></th></td<>				Merton		E	llack-Cox		Long	staff–Schv	vartz		DEJD			CDG	
4         3         3         3         2         2           les $p_5$									Chi-squ	uare value	ş						Ì
les $\frac{16.59}{p5}$ $\frac{14.79}{p5}$ $\frac{14.79}{p5}$ $\frac{14.41}{p5}$ $\frac{9.32}{p5}$ $\frac{9.32}{p5}$ $\frac{9.32}{p5}$ $\frac{9.32}{p5}$ $\frac{9.32}{p5}$ $\frac{9.33}{p5}$ $\frac{9.35}{p5}$ $\frac{9.3}{p5}$ $9.$	d.o.f.			4			3			3			2			Ч	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Mean Percentiles		16.59 p5	p50	<i>p</i> 95	$\frac{14.79}{p5}$	p50	<i>p</i> 95	14.41 <i>p5</i>	<i>p</i> 50	p95	$9.32 \\ p5$	p50	<i>p</i> 95	3.83 p5	p50	<i>p</i> 95
: Number of firms with the model being not rejected: by ratings 1 1 0 0 0 0 0 0 0 1 1 1 1 2 5 0 0 0 0 0 0 0 1 1 1 1 1 2 5 0 0 0 0 0 0 0 1 1 1 1 1 1 1 1 1 1 1 1	Sig. level		$12.59 \\ 0.01$	$17.12 \\ 0.05$	$17.92 \\ 0.10$	$12.03 \\ 0.01$	$15.08 \\ 0.05$	$16.26 \\ 0.10$	$13.66 \\ 0.01$	$14.53 \\ 0.05$	$14.62 \\ 0.10$	$1.57 \\ 0.01$	9.36 0.05	$15.73 \\ 0.10$	$0.01 \\ 0.01$	2.21 0.05	$13.27 \\ 0.10$
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Panel A: Number of fir	ms with the mod	el being n	ot rejecte	d: by rati	sgn											
	AAA	-	0	0	0	0	0	0	0	0	0	1	1	-	0	0	0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	AA	9	0	0	0	0	0	0	0	0	0	7	-	1	4	4	ŝ
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	А	25	0	0	0	0	0	0	0	0	0	10	8	9	22	22	21
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	BBB	44	2	0	0	2	0	0	9	2	1	22	~	4	36	29	23
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	BB	12	ŝ	0	0	2	1	1	4	2	1	4	1	0	9	4	ŝ
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	В	4	0	0	0	7	0	0	-	-	0	7	7	-	4	4	7
	CCC	1	0	0	0	0	0	0	-	1	0	-	0	0	0	0	0
mications6100200100300nercyclic $32$ 10000003100nerstable1400000000522 $8$ 00001100431 $8$ 10001110431 $1$ 110011061106 $1$ 1100110021000 $1$ 110011110000 $1$ 100111000000 $1$ 110011100000 $1$ 100111100000 $1$ 100111100000 $1$ 100111100000 $1$ 1100111100000 $1$ 10	Panel B: Number of fir	ms with the mod	el being ne	ot rejected	d: by sect	ors											
nercyclic $32$ 1       0       0       0       3       1       0       16       8       4         nerstable       14       0       0       0       0       0       0       5       2       2         a       1       1       0       1       1       0       1       4       3       1         al       18       1       0       0       1       1       1       4       3       1         bls       11       1       0       0       1       1       4       2       2       2       2       3       3       1         old       11       1       1       1       1       1       0       4       3 </td <td>Communications</td> <td>6</td> <td>1</td> <td>0</td> <td>0</td> <td>2</td> <td>0</td> <td>0</td> <td>1</td> <td>0</td> <td>0</td> <td>ę</td> <td>0</td> <td>0</td> <td>5</td> <td>5</td> <td>4</td>	Communications	6	1	0	0	2	0	0	1	0	0	ę	0	0	5	5	4
Inerstable     14     0     0     0     0     0     0     0     5     2     2 $a $ $8$ $0$ $0$ $0$ $0$ $0$ $0$ $5$ $2$ $2$ $a $ $18$ $1$ $0$ $0$ $1$ $1$ $0$ $4$ $3$ $a $ $11$ $1$ $1$ $1$ $1$ $0$ $0$ $4$ $3$ $b $ $11$ $1$ $0$ $0$ $1$ $1$ $0$ $4$ $3$ $b $ $4$ $1$ $0$ $0$ $1$ $1$ $0$ $5$ $3$ $3$ $b $ $4$ $1$ $0$ $0$ $1$ $1$ $0$ $5$ $3$ $3$ $b $ $4$ $1$ $0$ $0$ $1$ $1$ $0$ $5$ $3$ $3$ $b $ $0$ $0$ $1$ $1$ $0$ $0$ $5$ $3$ $3$ $b $ $0$ $0$ $1$ $1$ $1$ $0$ $5$ $3$ $3$ $b $ $0$ $0$ $0$ $1$	Consumer cyclic	32	-	0	0	0	0	0	б	1	0	16	8	4	21	18	15
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Consumer stable	14	0	0	0	0	0	0	0	0	0	5	2	2	11	10	~
al     18     1     0     0     1     1     1     4     2     2     9     4     3       ls     11     1     0     0     1     0     0     2     1     0     5     3     3       logy     4     1     0     0     1     0     0     5     3     3       logy     6     1     1     0     0     1     0     0     0	Energy	8	0	0	0	1	0	0	1	1	0	4	ŝ	-	9	5	4
tials     11     1     0     0     1     0     5     3     3       nology     4     1     0     0     1     0     0     1     0     0     0       33     5     1     0     6     1     1     12     6     2     42     20     13	Industrial	18		0	0			1	4	7	7	6	4	ŝ	16	14	11
nology         4         1         0         0         1         1         0 <td>Materials</td> <td>11</td> <td></td> <td>0</td> <td>0</td> <td></td> <td>0</td> <td>0</td> <td>7</td> <td>-</td> <td>0</td> <td>5</td> <td>ŝ</td> <td>ŝ</td> <td>10</td> <td>6</td> <td>6</td>	Materials	11		0	0		0	0	7	-	0	5	ŝ	ŝ	10	6	6
93 5 1 0 6 1 1 1 2 6 2 42 20 13	Technology	4		0	0	-	0	0	-		0	0	0	0	ŝ	2	7
	Total	93	5	-	0	9	Ļ	-	12	9	2	42	20	13	72	63	52

Downloaded from https://academic.oup.com/rof/article/24/1/45/5477416 by National Science and Technology Library -Root user on 29 September 2020

Table III. Parameter estimation of structural credit risk models

This table reports the GMM estimation results of the model parameters in each of five structural models. The five moment conditions used in the test are conestimate  $\sigma_v$  in all five models, Panel B reports the default boundary estimate K in three barrier type models, and Panel C reports jump intensity estimate  $\lambda^a$  in the structed based on the pricing relationship for 1-, 2-, 5-, and 10-year CDS spreads and for the equity volatility estimated based on 5-min intraday data. The five model specifications include Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2002). Panel A reports the asset volatility parameter DEJD model and dynamic leverage parameters,  $\kappa_\ell,
u$ , and  $\phi$ , in the CDG model.

Panel A: Estimates of the asset volatility under different structural models

	Number of firms						Struc	tural cred	Structural credit risk models estimated	dels estin	ated					
Total	93		Merton		В	Black-Cox		Long:	Longstaff–Schwartz	vartz		DEJD			CDG	
Mean			0.154			0.168			0.177			0.160			0.199	
Standard deviation			(0.007)			(0.007)			(060.0)			(0.010)			(0.042)	
Percentiles		p5	p50	p95	p5	p50	p95	p5	p50	p95	p5	p50	p95	p5	p50	p95
		0.070	0.135	0.337	0.097	0.151	0.274	0.061	0.153	0.407	0.075	0.154	0.252	0.098	0.170	0.337
Asymptotic SEs		(0.002)	(0.006)	(0.014)	(0.003)	(0.006)	(0.016)	(0.006)	(0.047)	(0.228)	(0.003)	(0.006)	(0.031)	(0.005)	(0.011)	(0.031)
AAA	1	0.133	0.133	0.133	0.100	0.100	0.100	0.160	0.160	0.160	0.141	0.141	0.141	0.114	0.114	0.114
AA	9	0.053	0.075	0.106	0.156	0.243	0.267	0.153	0.291	0.380	0.154	0.186	0.239	0.134	0.242	0.339
Α	25	0.068	0.112	0.168	0.090	0.149	0.203	0.088	0.153	0.250	0.128	0.164	0.221	0.114	0.173	0.325
BBB	44	0.095	0.137	0.222	0.102	0.145	0.216	0.058	0.139	0.227	0.072	0.148	0.224	0.077	0.166	0.276
BB	12	0.111	0.198	0.408	0.114	0.194	0.388	0.054	0.205	0.645	0.076	0.135	0.392	0.104	0.206	0.554
В	4	0.263	0.361	0.399	0.183	0.297	0.351	0.072	0.434	0.602	0.075	0.175	0.264	0.105	0.349	0.473
CCC	1	0.369	0.369	0.369	0.270	0.270	0.270	0.054	0.054	0.054	0.054	0.054	0.054	0.042	0.042	0.042
Communications	9	0.069	0.184	0.399	0.113	0.151	0.335	0.074	0.181	0.412	0.138	0.161	0.264	0.107	0.292	0.451
Consumer cyclic	32	0.091	0.150	0.309	0.097	0.167	0.268	0.045	0.153	0.290	0.055	0.150	0.237	0.042	0.167	0.325
Consumer stable	14	0.053	0.081	0.239	0.094	0.146	0.265	0.106	0.148	0.557	0.085	0.159	0.237	0.106	0.171	0.307
Energy	8	0.105	0.134	0.340	0.112	0.158	0.206	0.072	0.150	0.240	0.097	0.142	0.216	0.113	0.161	0.296
Industrial	18	0.097	0.135	0.403	0.091	0.125	0.378	0.066	0.131	0.583	0.086	0.149	0.343	0.095	0.165	0.526
Materials	11	0.081	0.110	0.222	0.107	0.151	0.230	0.108	0.155	0.201	0.101	0.148	0.276	0.115	0.187	0.243
Technology	4	0.098	0.169	0.304	0.176	0.209	0.275	0.198	0.245	0.441	0.174	0.179	0.289	0.233	0.248	0.493

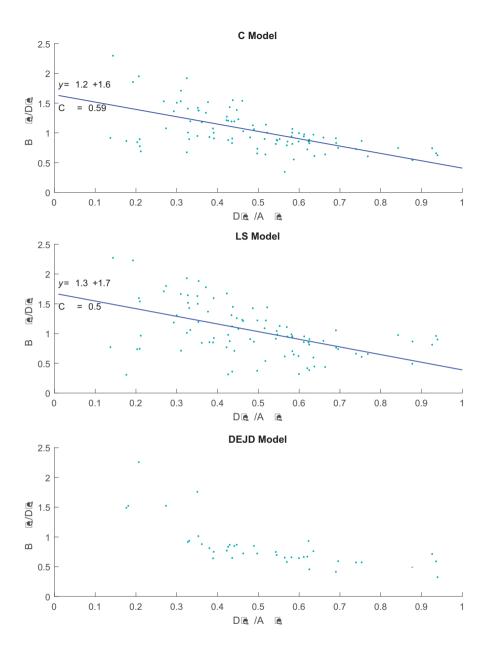
(continued)

oundary
p
ult
defau
the
of
Estimate
В:
Panel

	Number of firms				ouructural cr	ouructural credit risk models considered	s considered			
Total	93		Black-Cox		Lo	Longstaff-Schwartz	rtz		DEJD	
Mean			1.176			1.161			0.830	
Standard deviation			(0.145)			(0.274)			(0.183)	
Percentiles		p5	p50	p95	p5	p50	p95	p5	p50	p95
		0.640	1.055	1.923	0.536	1.049	2.018	0.419	0.752	1.734
Asymptotic SEs		(0.006)	(0.134)	(0.217)	(0.020)	(0.173)	(0.859)	(0.020)	(0.163)	(0.316)
AAA	1	0.971	0.971	0.971	1.086	1.086	1.086	0.723	0.723	0.723
AA	9	0.844	0.905	2.296	0.751	1.034	2.442	0.807	1.553	1.773
Α	25	0.887	1.362	2.425	0.751	1.180	2.449	0.304	0.886	1.904
BBB	44	0.638	1.072	1.685	0.597	1.057	1.835	0.443	0.696	1.174
BB	12	0.655	0.867	1.782	0.430	0.921	1.783	0.422	0.672	1.759
В	4	0.550	0.793	0.983	0.333	0.718	1.004	0.380	0.538	0.700
CCC	1	0.959	0.959	0.959	1.011	1.011	1.011	0.706	0.706	0.706
Communications	9	0.612	1.295	1.675	0.449	1.208	1.846	0.087	0.614	1.137
Consumer cyclic	32	0.648	1.094	2.199	0.618	1.174	2.211	0.501	0.749	1.570
Consumer stable	14	0.606	1.007	2.740	0.417	0.894	2.813	0.474	0.822	1.980
Energy	8	0.638	0.938	1.951	0.417	0.925	2.094	0.350	0.656	1.862
Industrial	18	0.660	1.019	1.840	0.635	1.033	1.813	0.405	0.710	0.953
Materials	11	0.865	1.062	1.513	0.756	1.150	1.657	0.427	0.807	1.025
Technology	4	0.655	0.958	1.630	0.548	0.928	1.636	0.635	0.775	1.767

C	
<u> </u>	
÷.	
_	
_	
_	
_	
ell	
ole II	
ell	
ole II	
able II	
able II	
able II	

Panel C: Estimates o.	Panel C: Estimates of other parameters in the DEJD and CDG models	the DEJD	and CDG n	nodels									
(1)	(2) Number of firms	(3)	(4)	(5)	(6) Str	(7) uctural cree	(8) dit risk mod	(7) (8) (9) Structural credit risk models considered	(10) red	(11)	(12)	(13)	(14)
Total	93		DEJD						CDG				
Parameter			γ			$\kappa_\ell$			λ			φ	
Mean			0.181			15.155			0.222			2.829	
Standard deviation			$\{0.078\}$			$\{3.258\}$			$\{0.274\}$			$\{2.070\}$	
Percentiles		p5 0.042	p50 0.126	$p95 \\ 0.499$	<i>p5</i> 0.446	p50 15.347	<i>p</i> 95 35.466	p5 0.069	$p50 \\ 0.163$	p95 1.180	p5 -0.103	$p50 \\ 1.878$	p95 6.242
Asymptotic SEs		(0.009)	(0.029)	(0.132)	(0.007)	(0.062)	(0.439)	(0.003)	(0.008)	(0.137)	(0.048)	(0.181)	(1.867)
AAA	1	0.119	0.119	0.119	15.042	15.042	15.042	0.106	0.106	0.106	1.184	1.184	1.184
AA	9	0.057	0.092	0.227	1.608	17.715	22.097	0.185	0.293	1.988	0.359	3.142	36.208
А	25	0.034	0.113	0.277	10.189	16.826	35.489	0.099	0.173	0.555	1.352	2.279	10.199
BBB	44	0.054	0.123	0.465	8.717	15.357	35.489	0.068	0.142	0.261	-0.095	1.736	2.952
BB	12	0.008	0.209	0.483	0.047	1.414	20.708	-4.117	0.209	1.158	-12.185	1.367	11.763
В	4	0.420	0.493	0.981	0.476	5.191	8.877	0.069	0.261	1.017	-0.797	1.581	6.336
CCC	1	0.580	0.580	0.580	-0.021	-0.021	-0.021	1.566	1.566	1.566	37.416	37.416	37.416
Communications	9	0.044	0.166	0.420	1.905	12.767	15.833	0.191	0.255	1.389	1.428	3.091	29.644
Consumer cyclic	32	0.060	0.151	0.559	0.126	15.434	33.934	0.069	0.164	1.946	-0.099	1.876	32.980
Consumer stable	14	0.043	0.114	0.468	2.982	17.280	35.489	0.073	0.148	0.295	0.148	1.862	3.507
Energy	8	0.040	0.118	0.469	8.877	14.580	19.271	0.090	0.136	0.277	-0.797	1.340	3.508
Industrial	18	0.043	0.107	0.713	0.647	15.437	35.489	0.069	0.146	0.888	-7.485	1.743	2.796
Materials	11	0.057	0.096	0.441	0.062	17.096	24.548	-4.351	0.159	0.277	-0.025	1.908	5.671
Technology	4	0.001	0.088	0.114	0.406	8.633	16.944	0.195	0.418	1.209	-9.763	2.566	12.435



To be more specific, given a candidate model and its estimated model parameters, in each month we calculate the model-implied equity volatility and CDS spreads for each maturity including 2 and 7 years. Note that while 2- and 7-year contracts are too sparse to be included in estimation, they are still useful to be included in pricing error evaluation. Then we compute the simple difference, absolute difference, and percentage difference between the model-implied and observed ones, for every name in the sample. Next, we calculate the mean of the pooled pricing errors.

Table IV reports the pricing errors on CDS spreads for the full sample as well as by each rating group and sector. In terms of pricing errors on the spread level (panel A), the overall average pricing error is negative except for the Merton model. This is to say that on average, the Merton model overestimate the CDS spread while the other four models underestimate the spreads.<sup>8</sup> Specifically, the average pricing error is –0.18% for CDG, –0.44% for DEJD, –0.71% for LS, and –0.91% for BC. Thus, the CDG and DEJD models underfit the CDS spread less than the BC and LS models.

Note that the overall positive pricing error of the Merton model is mainly driven by the four B-rated names and the single CCC firm (Delta Air Lines) in the sample. To see that, recall first from Appendix Table AI that these five names all have high leverage and high equity volatility: Delta Air has an equity volatility of 81.9% and a leverage of 93.9%; the average equity volatility and leverage on the four B-rated names are 83.2% and 72.6%, respectively. It is known that the Merton model-implied short-term credit spread with high leverage and equity volatility can be very high (Merton, 1974), consist with our panel C of Figure 4. As a result, the Merton pricing error on these five names is large as reported in panel A of Table IV. Next, note from panel A that the average pricing error for IG names is negative, regardless of the structural models considered; that is, on average, all five candidate models underestimate the CDS spread on IG names, consistent with the findings of Bao (2009) using the BC and DEJD models as well as those of Eom, Helwege, and Huang (2004) and Huang and Huang (2012) based on IG bonds.

In terms of absolute pricing performance (panel B), the BC and LS models outperform the Merton model but underperform the DEJD and CDG models in both the full sample and each of the seven credit-rating groups (except for the single CCC firm where the BC model slightly outperforms CDG). Furthermore, between the two more recent models, the DEJD model performs relatively better for the IG names while the CDG model does better for the HY names (except for the single CCC firm). These results differ from the findings of Eom, Helwege, and Huang (2004) based on corporate bond data that richer model specifications do not necessarily have lower pricing errors.

Results on percentage pricing errors, reported in panel C, indicate that on average, the CDG model overestimates the CDS spread while the other four models underestimate the spread. Among the IG names, the Merton, BS, LS, and DEJD models all underestimate the spread substantially in each of the four rating categories, except that the DEJD model overestimates the single AAA name's spread. On the other hand, the CDG model overestimates the spread for three IG-rated subgroups. These results indicate that although the newer models (DEJD and CDG) do improve upon the older ones (Merton, BC and LS), the CDG model can raise the spread too much for names in certain rating groups in terms of the percentage pricing errors.

8 Predescu (2005) also observes that combining equity price and CDS spreads would make the Merton model overfit the spread.

model
isk
credit r
structural
.⊆
errors
pricing
CDS
≥
Table

s

vations from January 2002 to December 2004. The five model specifications include Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang This table reports the pricing errors of CDS spreads under each of five structural models. Pricing errors are calculated as the average, absolute, average percentage, and absolute percentage differences between the model implied and observed spreads, across six maturities, 1, 2, 3, 5, 7, and 10 years, and monthly obser-01001

Firms by		CDS pricin	CDS pricing errors in five different models	different mov	dels						
Ratings or Sectors	number	Merton	BC	LS	DEJD	CDG	Merton	BC	ΓS	DEJD	CDG
			Panel A: Av	Panel A: Average pricing error (%)	error (%)			Panel B: Ab	Panel B: Absolute pricing error (%	error (%)	
Overall	93	0.37	-0.91	-0.71	-0.44	-0.18	1.54	0.99	0.98	0.75	0.78
AAA	1	-0.14	-0.30	-0.28	0.00	-0.11	0.24	0.30	0.28	0.19	0.20
AA	9	-0.19	-0.12	-0.16	-0.06	-0.03	0.19	0.15	0.16	0.09	0.11
A	25	-0.31	-0.25	-0.25	-0.08	-0.03	0.34	0.28	0.29	0.17	0.18
BBB	44	0.11	-0.63	-0.61	-0.32	0.00	1.23	0.66	0.68	0.45	0.59
BB	12	0.16	-1.65	-1.60	-0.10	-0.07	2.46	1.82	1.95	1.47	1.41
В	4	6.39	-4.34	-4.24	-3.62	-0.89	8.05	4.95	4.68	4.28	3.31
CCC	1	11.55	-12.95	4.00	-8.82	-10.92	17.14	12.96	10.26	9.94	11.43
Communications	9	-0.50	-1.61	-1.84	-1.51	-0.28	1.29	1.62	1.86	1.53	1.08
Consumer cyclic	32	1.02	-1.09	-0.59	-0.50	-0.54	2.27	1.10	1.08	0.72	0.88
Consumer stable	14	0.43	-0.64	-0.67	-0.13	-0.11	1.06	0.67	0.72	0.31	0.34
Energy	8	1.47	-1.04	-0.71	-0.71	-0.20	2.35	1.07	0.78	0.82	0.81
Industrial	18	-0.29	-0.61	-0.53	-0.53	0.08	0.85	0.92	0.90	0.70	0.71
Materials	11	-0.28	-0.69	-0.77	-0.41	0.60	0.81	0.70	0.80	0.54	0.94
Technology	4	-1.17	-1.19	-0.89	1.33	-0.56	1.17	1.19	0.94	1.92	0.97

Firms by		CDS pricing	CDS pricing errors in five different models	different mode	sle						
Ratings or Sectors	number	Merton	BC	LS	DEJD	CDG	Merton	BC	LS	DEJD	CDG
		Panel C: Av	Panel C: Average percentage pricing error (%)	ge pricing errc	or (%)		Panel D: Ab	<sup>2</sup> anel D: Absolute percentage pricing error (%)	age pricing err	or (%)	
Overall	93	-29.62	-70.91	-68.94	-11.88	24.42	114.29	76.20	78.17	45.63	68.88
AAA	1	-6.60	-82.04	-74.13	47.96	3.40	70.69	82.04	75.42	80.03	56.99
AA	9	-100.00	-67.72	-85.95	-21.09	-3.91	100.00	82.60	86.11	44.56	69.12
А	25	-82.60	-71.86	-68.88	-1.95	9.69	97.29	78.14	80.27	47.33	55.39
BBB	44	-25.54	-72.85	-69.50	-17.29	40.35	119.78	76.84	78.82	44.37	80.26
BB	12	15.92	-70.77	-69.28	-6.81	16.01	111.45	72.73	76.82	43.01	58.47
В	4	182.82	-50.96	-50.61	-29.71	33.91	196.57	62.82	59.60	51.82	64.48
COC	1	117.78	-50.82	-7.35	-16.28	-54.47	131.60	50.85	42.83	37.14	58.59
Communications	9	-62.16	-76.83	-77.03	-39.66	31.97	82.63	77.83	79.42	51.39	87.03
Consumer cyclic	32	14.04	-72.77	-72.08	-6.97	6.22	154.04	75.83	80.02	43.77	60.93
Consumer stable	14	-55.69	-71.10	-64.90	-17.18	3.18	107.27	80.71	79.44	38.03	43.72
Energy	8	-5.28	-66.81	-76.71	-23.08	17.52	133.16	71.67	78.17	38.10	50.46
Industrial	18	-51.63	-66.06	-56.16	-19.15	41.55	74.67	76.29	75.49	45.10	71.85
Materials	11	-66.48	-70.35	-73.29	9.67	86.40	85.74	72.67	75.50	58.27	125.59
Technology	4	-87.25	-77.93	-75.78	4.83	-0.78	87.25	79.34	76.47	61.09	60.87

Table IV. Continued

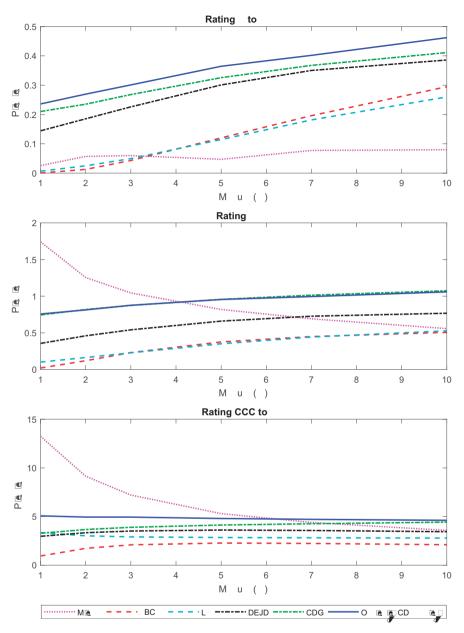


Figure 4. Observed and model-implied CDS term structures. This figure plots the time-series average of both observed and model-implied CDS term structures, by three rating groups, over the period January 2002–December 2004. The structural models considered include Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2002).

Panel D reports the results on absolute percentage pricing errors. The ranking of the five models is largely the same as before: the DEJD and CDG models outperform the BC and LS models, both of which outperform the Merton model. Nonetheless, the accuracy of all five models is still a problem: the average absolute percentage pricing error ranges from 45.6% for the DEJD model to 114.3% for the Merton model. This finding echos a similar one in the corporate bond market documented in Eom, Helwege, and Huang (2004).

Table V presents the results on fitting errors of equity volatility. Broadly speaking, they display similar patterns to those on the CDS spreads (Table IV). For instance, consider panel A. Note that for each model the overall sign of fitting errors on equity volatility is consistent with those on CDS spreads, though the magnitude of volatility fitting errors is generally larger. To some extent, this result is not surprising given that credit spreads increase with the asset volatility in the candidate models. Note also that the Merton fitting error is positive overall mainly because of overfitting in the four B-rated and one CCC-rated bonds. In fact, the model underfits equity volatility of AA and A names substantially. The other four models also underfit equity volatility of IG names, except for the single AAA-rated name in the case of the BC, LS, and DEJD models and for the AA-rated names in the case of the BC model.

In terms of absolute fitting performance (panel B), on average, the DEJD and CDG models have the lowest errors (11.61% and 11.87%, respectively), while the Merton model has the highest one (26.11%). The BC model slightly underperforms CDG but outperforms LS substantially. Between the two more recent models, on average, the DEJD model underperforms CDG in IG names but outperforms CDG in HY names.

In terms of percentage fitting errors on equity volatility (panel C), the overall sign is consistent with those on CDS spreads for the BC, DEJD, and CDG models. This is not the case, however, for the Merton and LS models, which both have an overall positive volatility fitting error. Additionally, note that the magnitude of overall percentage fitting errors on equity volatility is much lower than its counterpart on spreads, because the level of equity volatility is typically higher than the CDS spread.

The ranking of the five models based on the overall absolute percentage fitting error on equity volatility (panel D) is the same as that based on the overall absolute fitting error on equity volatility (panel B) except that the BC and CDG models switch their places. In addition, for each of the seven different rating groups, the DEJD model outperforms the CDG model except for the single AAA-rated name.

To summarize, the results of this section provide evidence that the two more recent models (the DEJD and CDG models) outperform the three older ones (the Merton, BC, and LS models) in fitting CDS spreads as well as equity volatility. Nonetheless, we find that on average, the five structural models all underestimate CDS spreads as well as equity volatility for IG names. In addition, the accuracy of all five models in fitting either the CDS spread or equity volatility is low.

#### 6.4 Further Diagnostics on Model Specifications

In this subsection, we examine the average CDS term structure as well as the time series of the 5-year CDS spread and equity volatility. Doing so can provide further insights on model specification errors and consequently on how to improve the models.

Figure 4 plots the sample average of the CDS term structure from 1 to 10 years from the observed data (in solid blue) as well as each of the five candidate models, for three different

Downloaded from https://academic.oup.com/rof/article/24/1/45/5477416 by National Science and Technology Library -Root user on 29 September 2020

Firms by		Fitting erro	rs of equity vc	Fitting errors of equity volatility in five different models	lifferent model	S					
Ratings or Sectors	number	Merton	BC	LS	DEJD	CDG	Merton	BC	LS	DEJD	CDG
			Panel C: Ave	Panel C: Average PCT fitting error (%)	g error (%)			Panel D: Abs	Panel D: Absolute PCT fitting error (%)	ng error (%)	
Overall	93	7.09	-5.44	6.40	-8.96	7.33	58.29	27.88	40.49	25.53	28.41
AAA		5.03	21.40	39.47	22.23	0.60	31.98	43.20	51.85	41.33	30.02
AA	9	-72.12	6.57	25.67	-15.04	6.61	72.12	31.67	45.25	25.31	27.39
А	25	-37.18	-4.21	-11.83	-8.99	5.20	44.10	28.02	29.56	24.74	25.49
BBB	44	12.06	-7.42	1.02	-9.32	6.11	48.81	26.10	35.00	24.02	25.59
BB	12	36.98	-4.59	39.25	-6.92	8.54	53.62	27.91	58.90	29.27	34.20
В	4	120.65	-28.54	64.24	-11.47	21.05	125.78	32.33	95.26	31.34	45.24
CCC		559.59	33.77	-75.23	-1.53	55.91	559.59	46.11	75.23	29.67	92.76
Communications	9	-13.47	-11.92	-10.51	-21.16	10.67	38.70	29.91	32.49	29.44	38.85
Consumer cyclic	32	37.53	-6.48	-4.13	-11.58	7.48	84.72	27.37	38.63	24.56	27.90
Consumer stable	14	-20.12	-0.98	26.74	-3.49	5.77	67.18	30.26	50.61	25.48	26.17
Energy	8	19.65	-18.90	15.72	-0.47	11.07	54.35	27.63	53.61	24.22	28.89
Industrial	18	-2.65	-0.80	2.79	-9.97	6.66	32.14	27.43	34.52	25.08	25.63
Materials	11	-18.31	0.83	11.02	-5.59	0.41	33.54	25.44	31.32	22.54	25.54
Technology	4	-21.83	-14.32	29.84	-10.53	21.20	38.76	29.83	57.78	40.55	44.02

Table V. Continued

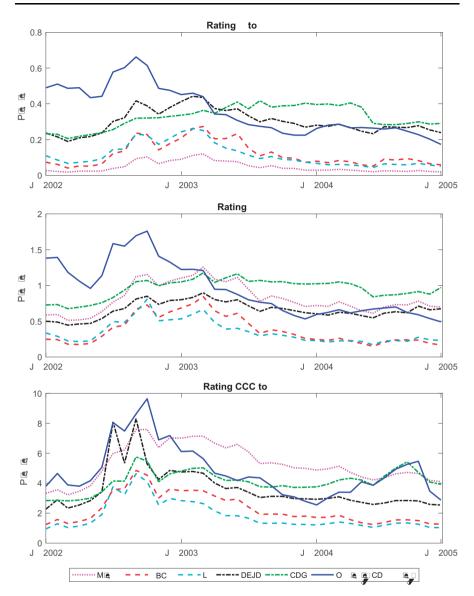
credit-rating groups, AAA–A (top panel), BBB (middle), and BB–CCC (bottom). A few observations are worth mentioning here: (1) all five models underfit the average term structure except for the Merton model that overfits the short end for the BBB and BB–CCC groups; (2) the best-fitting model, CDG, fits the BBB average term structure almost perfect-ly and underfits slightly for the AAA–A group; (3) the DEJD model is the second best; (4) the BC model largely captures the shape of the average term structure but underfits its level considerably; (5) the LS model slightly underperforms the BC model for IG names with short maturity but outperforms the latter for HY names; (6) the Merton model underfits the AAA–A curve substantially, especially in the long end but underfits the long end of the BBB and BB–CCC curves less than the BC and LS models.

Overall, both the CDG and DEJD models match the shape of the average term structure of CDS spreads well, especially for IG names. The two models, however, still underfit the level of the curve, although the CDG model-implied curve is much closer to the observed one than the DEJD-implied curve is.

Figure 5 plots the observed 5-year CDS spread against the five model-implied ones. For the HY names (the BB–CCC group), all models seem to capture the time-variations of the 5-year CDS spread reasonably well, although the DEJD and CDG models seem to be the best two. Furthermore, while the DEJD model outperforms the CDG mode in the first third of the sample period, the latter outperforms the former in the last third of the sample period. For the IG names (the AAA–A and BBB groups), most models completely miss the dynamics of the CDS spread, especially for the first third of the sample, when the risk-free rate remains as low as 1%. Interestingly, even the best-fitting CDG model that can get the average level right is not able to describe the evolution of the CDS spread. This finding suggests that a time-varying factor in addition to the interest rate and leverage ratio—like stochastic asset volatility—may be needed in order for a structural model to fully capture the temporal changes in CDS spreads for IG names.

Figure 6 reports the average model-implied and realized equity volatilities over the full sample period, for three different credit-rating groups, AAA–A (top panel), BBB (middle), and BB–CCC (bottom). Note that for both IG groups, all five models miss completely the volatility spikes during the early sample period. Moreover, every model generates a nearly constant equity volatility while the observed equity volatility varies substantially over time. For the HY group, the model performance is relatively better. In particular, the Merton model captures the volatility spikes to some degree and the LS and DEJD models reasonably fit the second half of the volatility time series. However, these results are mainly driven by the unrealistically high model-implied volatility for the single CCC-rated name. Overall, Figure 6 provides evidence suggesting that without time varying asset volatility, the structural models have difficulty replicating the observed equity volatility dynamics, especially for IG names.

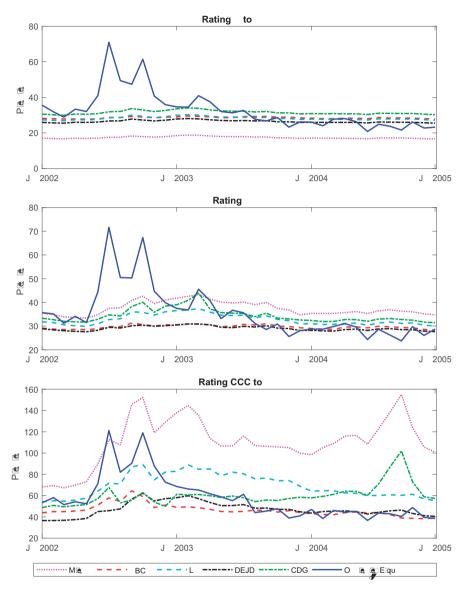
Figure 7 plots the initial spot log leverage ratio  $\log(K_t/V_t)$  and the long-run mean of risk-neutral log leverage ratio implied from the CDG model, for three different creditrating groups, AAA–A (top panel), BBB (middle), and BB–CCC (bottom). It is clear from the figure that these two leverages are fairly close to each other for the HY group (the CCC–BB names). On the other hand, for the BBB names the observed leverage is significantly lower than its risk-neutral counterpart, and the difference between the risk-neutral and observed leverages is even more dramatic for the AAA–A names. This finding mirrors the stylized fact that highly profitable firms may opt to borrow little or no debt (Chen and



**Figure 5.** Observed and model-implied 5-year CDS spreads. This figure plots observed and modelimplied 5-year CDS spreads, for three credit rating groups, over the period January 2002–December 2004. The structural models considered include Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2002).

Zhao, 2006; Strebulaev and Yang, 2013). Such a puzzle may be worth further investigation.

In sum, dynamic leverage ratios and, to a lesser degree, jumps in asset returns help match CDS spreads and equity volatility better. However, something else is still missing in the five candidate models as they all fail to adequately capture the dynamic behavior of CDS spreads and equity volatility, especially for the IG names. Our findings suggest that

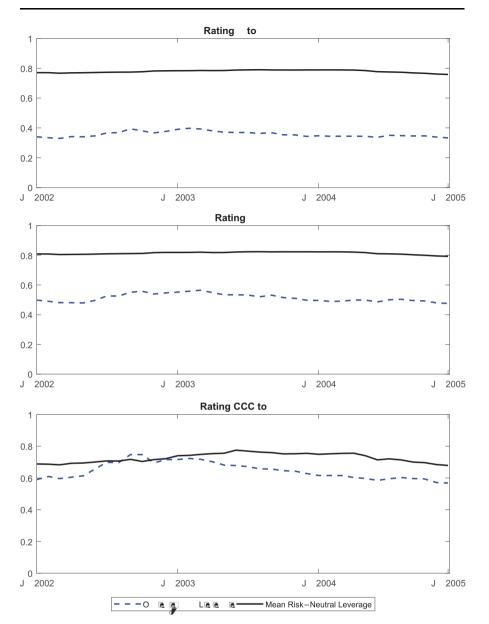


**Figure 6.** Observed and model-implied equity volatilities. This figure plots realized volatility (estimated using 5-min intraday stock returns) and five model-implied equity volatilities, for three credit rating groups, over the period January 2002–December 2004. The five structural models are Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2002).

incorporating a stochastic asset volatility may improve the performance of the existing structural models.

# 6.5 Model-Implied Equity Sensitivities of CDS Spreads

The implications of the estimated structural models go beyond CDS spreads and equity volatilities, the variables included as moment conditions and examined in Sections 6.3 and 6.4.



**Figure 7.** Observed spot leverage and the long-run mean of risk-neutral leverage. This figure plots the observed spot leverage (debt/asset) and the model-implied long-run mean of the risk-neutral leverage, for three rating groups, over the period January 2002–December 2004. The long-run mean of the risk-neutral leverage is estimated using the CDG model.

In this subsection, we focus on one firm-specific variable not included in the moment conditions, the sensitivity of 5-year CDS spreads to equity returns discussed in Section 3.3.

#### 6.5.a. Regression tests of model-implied sensitivities

We first test the accuracy of model-implied sensitivities in a linear regression setting. Consider the following regression model:

$$\Delta cds(t, t+5)_i = \alpha_i + \beta_{1,i} \Delta r_{f,t}^{10y} + \beta_{2,i} \Delta_{E,i,t}^{cds} r x_{i,t}^E + u_{it},$$
(19)

where  $\Delta cds(t, t + 5)_i$  denotes the monthly change in the observed 5-year CDS spread for firm *i*;  $r_{f,t}^{10y}$  the month-*t* 10-year zero yield extracted from swap rates and included to control for changes in the "risk-free" term structure;  $rx_{i,t}^E$  firm-*i*'s monthly equity return minus the one-month LIBOR; and  $\Delta_{E,i,t}^{cds}$  is the model-implied sensitivity of the CDS spread to equity return for firm *i* as specified in Equation (9)<sup>9</sup> and is calculated using the parameter vector  $\hat{\theta}$ estimated with the full sample (see Section 6.2)—for example,  $\hat{\theta} = (\hat{\sigma}_v)$  for the Merton model (Section 4.3). If the model accurately describes the equity sensitivity of CDS spreads,  $\beta_{2,i}$  should be equal to one. On the other hand, if the model consistently underpredicts the sensitivity, then  $\beta_{2,i}$  is expected to be significantly greater than one.

As such, we can test the null hypothesis (H1) that  $\beta_{2,i} = 1$  on a firm-by-firm basis and report the number of firms for which H1 is not rejected in our sample. In the analysis that follows, we conduct the test based on a modified Equation (19) with a smoothed  $\Delta_{E,i,t}^{cds}$ :

$$\Delta \widetilde{cds}(t,t+5)_i = \alpha_i + \beta_{1,i} \Delta r_{f,t}^{10y} + \beta_{2,i} \overline{\Delta}_{E,i,t}^{cds} r x_{i,t}^E + u_{it}, \qquad (20)$$

where  $\bar{\Delta}_{E,i,t}^{cds}$  denotes the month-*t* average of model-implied sensitivities across firms in the same rating or industry category as firm *i*. This is because using a smoothed model-implied hedge ratio can help reduce the noise in the firm-by-firm estimates of model parameters (see, e.g., Schaefer and Strebulaev, 2008).<sup>10</sup>

Table VI reports the results from regression in Equation (20) where  $\bar{\Delta}_{E,i,t}^{cds}$  used is either by ratings (panel A) or by industries (panel B). Consider panel A first. Note that  $\bar{\beta}_{2,i}$ , the average of the estimates of  $\beta_{2,i}$  over the whole sample, is 0.74 and 0.76 for the BC and LS models, respectively, but  $\bar{\beta}_{2,i}$  is around one for the other three models. An inspection of the means of  $\hat{\beta}_{2,i}$  in each rating category finds that the means are below one regardless of the

- 9 In the implementation of Equation (9),  $\frac{\partial cds(f_{i}+5)}{\partial V_{i}}$  is calculated using Equation (7) and  $\frac{\partial E}{\partial V_{i}}$  is set to one minus the delta of a 5-year par bond (see footnote 6), an approximation except for the Merton model. In an untabulated analysis using the BC model, we find that including the expected bankruptcy cost in  $\frac{\partial E}{\partial V_{i}}$  has little impact on the model's performance in fitting both CDS spreads and equity volatility as well as in hedging CDS.
- 10 The formulation of H1 is in the spirit of Schaefer and Strebulaev (2008) and Huang and Shi (2016), who examine the Merton-implied equity sensitivities of corporate bond returns and spreads, respectively; however, we conduct our hypothesis test slightly differently due to the size of our sample. Those two studies focus on the averages of regression coefficients (counterparts of the  $\beta_{2,}$  estimates here) across bonds in their samples and test whether the mean slope coefficients are close to one. In our case, inferences based on the mean of ninety-three estimates of  $\beta_{2,}$  may not be reliable—given the limited effects of the smoothing in those rating categories or sectors that each include less than ten firms. Still, the means of  $\beta_{2,}$  estimates over the full sample as well as each rating category or sector are reported in Table VI for completeness.

Downloaded from https://academic.oup.com/rof/article/24/1/45/5477416 by National Science and Technology Library -Root user on 29 September 2020

Table VI. Continued

Regression-	Panel A:	Rating-spe	Panel A: Rating-specific average sensitivities	șe sensitivii	ties			Panel B: Sector-specific average sensitivities	ecific averag	ge sensitivi	ties			
related variables	Rating	Rating Number	Models used	ed				Sector	Number	Models used	sed			
		of tirms	Merton	BC	LS	DEJD	CDG		ot tirms	Merton	BC	ΓS	DEJD	CDG
$ar{eta}_{2,i}$	BBB	44	1.00	0.73	0.76	0.94	1.04	Energy	8	1.16	0.70	0.67	1.23	0.74
Number of No-Rej			< 41 >	> 4 $>$ $<$ 4	< 9 >	< 40 >	< 35 >			< 9 >	< 0 >	$\stackrel{\scriptstyle \wedge}{}$	< 9 >	< 9 >
$R^2$			[0.279]	[0.236]	[0.263]	[0.278]	[0.199]			[0.160]	[0.103]	[0.107]	[0.189]	[0.219]
$\bar{B}_{2,i}$	BB	12	1.58	0.81	0.76	1.42	0.94	Industrial	18	1.03	0.70	0.68	0.99	1.06
Number of No-Rej			< 10 >	< 3 >	< 2 >	< 10 >	<12>			< 15 >	< 0 >	< 5 >	< 13 >	<16>
$R^2$			[0.507]	[0.385]	[0.443]	[0.506]	[0.180]			[0.268]	[660.0]	[0.139]	[0.277]	[0.133]
$\bar{B}_{2,i}$	В	4	2.90	0.88	0.83	2.52	1.25	Materials	11	0.92	0.70	0.70	06.0	0.88
Number of No-Rej			< 4 >	< 3 >	< 3 >	< 4 >	< 4 >			< 7 >	< 0 >	< 0 >	< 7 >	$< \frac{8}{8}$
$R^2$			[0.390]	[0.360]	[0.384]	[0.393]	[0.110]			[0.276]	[0.107]	[0.111]	[0.300]	[0.166]
$\bar{B}_{2,i}$	CCC	Ļ	3.90	0.95	0.86	3.49	1.00	Technology	4	1.43	0.70	0.69	1.37	0.80
Number of No-Rej			< 1 >	< 1 >	< 1 >	< 1 <	< 1 >			> 4 $<$ $<$ 4	< 0 >	< 2 >	< 3 >	< 1 >
$R^2$			[0.152]	[0.089]	[0.095]	[0.171]	[0.054]			[0.596]	[0.124]	[0.109]	[0.669]	[0.423]
$\bar{B}_{2,i}$	Overall	93	1.12	0.74	0.76	1.05	0.96	Overall	93	1.02	0.70	0.71	1.01	0.96
Number of No-Rej			< 72 >	< 12 >	< 18 >	< 69 >	< 76 >			< 68 >	< 0 >	< 25 >	< 65 >	< 73 >
$R^2$			[0.304]	[0.263]	[0.286]	[0.302]	[0.187]			[0.281]	[0.119]	[0.132]	[0.300]	[0.186]

rating categories for both the BC and LS models. This result indicates that these two models consistently overpredict the equity sensitivity of CDS spreads. On the other hand, for the Merton and DEJD models, the average  $\hat{\beta}_{2,i}$  is below or very close to one for IG names but is greater than one for HY names—and, in fact, the pair of the coefficients for B and CCC names are (2.90, 3.90) and (2.52, 3.49) for the Merton and DEJD models, respectively. The variation in the average  $\beta_{2,i}$  across different rating categories is much less for the CDG model, with the average  $\beta_{2,i}$  ranging from 0.73 for AA names to 1.25 for AAA- or B-rated names.

For how many firms out of 93 the null hypothesis H1 is not rejected (for a given model), based on the *t*-statistics using the Newey–West standard error estimator? As indicated in panel A, the answer is 72 (Merton), 12 (BC), 18 (LS), 69 (DEJD), and 76 (CDG), at the 5% significance level. Recall from Table II that the number of firms where a given model is not rejected by the GMM-based specification test at the 5% significance level is 1 (Merton), 1 (BC), 6 (LS), 20 (DEJD), and 63 (CDG). That is, all five models capture the sensitivity of CDS spreads to equity much better than they capture CDS spreads and equity volatility. This is true especially for the Merton model.

Regression  $R^2$ , shown in the last row of panel A, is 30.4% for Merton, 26.3% for BC, 28.6% for LS, 30.2% for DEJD, and 18.7% for CDG. Note that the  $R^2$  generated by the CDG model is the lowest among the five models—and even lower than its counterpart from the otherwise same regression excluding  $\bar{\Delta}_{E,i,t}^{cds}$  (untabulated). How to reconcile this result with the evidence that the number of firms where H1 is not rejected is the highest under CDG? One explanation is that the *t*-test conducted at the firm level may fail to reject the null hypothesis even if the point estimate of the slope coefficient substantially deviates from unity, due to the large standard error estimated using the Newey–West adjustment. Therefore, although among the five candidate models the CDG model has the largest number of non-rejected firms, the model does not necessarily make the most accurate prediction of hedge ratios.

The results reported in panel B of Table VI are largely similar to those in panel A. For example, the means of estimated  $\beta_{2,i}$  in every sector are 0.70 for the BC model and below 0.76 for LS. On the other hand, the means are much closer to one for the other three models. Furthermore, the Merton-based mean estimate is the largest among the five model-based mean estimates for three sectors (out of seven), including 1.33 for "communication," 0.92 for "materials," and 1.43 for "technology," and the second largest for the remaining four sectors. In terms of the regression  $R^2$ , it is 28.1% for Merton, 11.9% for BC, 13.2% for LS, 30.0% for DEJD, and 18.6% for CDG. Note that although the  $R^2$ under CDG is not the lowest here, it is still much lower than the  $R^2$ -value under either Merton or DEJD.

To summarize, while the results of the test of Hypothesis H1 favor the DEJD, Merton, and CDG models (in ascending order), the first two rank notably higher than CDG based on the regression  $R^2$ . As a low  $R^2$ -value suggests that the underlying model has difficulty in replicating the variation in CDS contract values effectively, the actual hedging performance of the same model may also be affected negatively. As such, the Merton and DEJD models may provide better hedging performance than does the CDG model. Furthermore, given that the Merton-implied sensitivity is more reasonable than the DEJD-implied one (e.g., for B and CCC names), the Merton model may provide better hedging performance that follows we investigate which of the five candidate models delivers the most robust hedging performance.

### 6.5.b. Evidence on hedging effectiveness

Suppose that in month t, an investor hedges a single-name CDS with the underlying equity and makes no additional trades until the end of t + 1.<sup>11</sup> At t + 1, the position is closed out and the hedging error over the 1-month period is computed as

$$\epsilon_t = V_{t+1}^{\rm cds} - b_{E,t}^{\rm cds} r_{t+1}^E$$

where the hedge ratio  $h_{E,t}^{\text{cds}}$  is as defined in Equation (10), and we make use of the fact that a CDS contract is worth close to zero when it is first initiated ( $V_t^{\text{cds}} = 0$ ).

Assume that the investor's objective is to minimize the monthly volatility of the hedged single-name CDS. Following Bertsimas, Kogan, and Lo (2000), we use root-mean-squared hedging error (RMSE) as the summary statistic for hedging errors over our sample period. Note that the RMSE is equal to the standard deviation when the mean hedging error is zero. Let RMSE<sup>M</sup> be the RMSE when model  $\mathcal{M}$ -implied hedge ratios are used. For comparison, we also compute the RMSE of the short CDS position when the CDS contract is not hedged ( $h_{E,t}^{cds} = 0$ ). Denote this RMSE by RMSE<sub> $\mu$ </sub>. One measure of hedging effectiveness calculates the reduction in the RMSE as a result of hedging and is given by

$$H_{\rm Eff} = 1 - \frac{\rm RMSE_b^{\mathcal{M}}}{\rm RMSE_u}.$$
(21)

Note that if hedge ratios implied from a particular model substantially increase volatility relative to the unhedged position, then  $H_{\text{Eff}}$  is negative.

Panel A of Table VII presents the results on the hedging performance of firm-specific hedge ratios (i.e., hedge ratios not smoothed over a given rating group or sector) under each of the five candidate models. Surprisingly, among these models the Merton  $H_{\text{Eff}}$  is the highest (7.0%), indicating that the Merton-implied hedge ratio achieves the largest reduction in the RMSE. The CDG model also has a significantly positive overall  $H_{\text{Eff}}$  (3.5%). In contrast, the overall  $H_{\text{Eff}}$  is highly negative for both the BC and LS models, implying that the hedged position—using hedge ratios derived from the two models—is much more volatile than the unhedged position. The overall negative  $H_{\text{Eff}}$  for the DEJD model has a great deal to do with the BB-rated names in the sample.

Consider next the hedging performance of the Merton and CDG models by credit ratings or sectors. Note that the Merton  $H_{\text{Eff}}$  is significantly positive for BB and B names only and that the CDG  $H_{\text{Eff}}$  is significantly positive for BB names only. On the other hand, out of the seven different sectors, the Merton  $H_{\text{Eff}}$  is significantly positive for six of them and the CDG  $H_{\text{Eff}}$  for two. These results together indicate that the Merton hedge ratio is more effective by sectors than by credit ratings.

Why is the overall  $H_{\text{Eff}}$  so negative for the BC and LS models? One possible reason is that the use of unsmoothed hedge ratios leads to dramatic increases in volatility.0 0 5.94Indeed, we observe from Table VI that for those rating or sector groups with a larger number of firms, the (rating- or sector-specific) average hedge ratios tend to be more aligned with their empirical counterparts. This result suggests that smoothing within a credit rating or industry

11 In an untabulated analysis, we also examine the performance of hedging CDS portfolio positions, with the portfolios formed based on the rating/sector category. These results are not reported as the relative performance among structural models does not change; as expected, the absolute hedging effectiveness increases because the hedging loss from one single name in the portfolio may be offset by the hedging gain from another.

Table VII. Hedging performance of structural credit risk models

This table reports empirical results on the effectiveness of hedging changes in CDS spreads with three types of hedge ratios. The first type (panel A) is firm-specific hedge ratios implied from five estimated structural models: Merton (1974), BC, LS, CDG, and the DEJD model used in Huang and Huang (2012). The other two types of hedge ratios are obtained by averaging firm-specific hedge ratios within either each credit rating category (panel B) or each sector (panel C). Given a structural model  $M_1$  the measure of hedging effectiveness used is  $H_{\rm Eff} = 1 - {\rm RMSE}_n^M {\rm RMSE}_u$  as defined in Equation (21), where  ${\rm RMSE}_n^M {\rm (RMSE}_u)$  is the root mean square error of the hedged (unhedged) position. The statistics in parenthesis are standard errors of this effectiveness obtained from 5,000 bootstrap simuations. The sample period is from January 2002 to December 2004.

01 00000	e e	ין אנוואטיו ו	errormance (H	Hedging performance (H <sub>Eff</sub> ) of various structural models	ructural mode	SIS					
01 366101	of firms	Merton	BC	LS	DEJD	CDG	Merton	BC	LS	DEJD	CDG
		Panel A: Fi	anel A: Firm-specific hedge ratios	lge ratios			Panel B: Ra	2 anel B: Rating-specific average hedge ratios	erage hedge ra	tios	
AAA	1	-0.817	0.088	0.175	0.101	0.009	-0.817	0.088	0.175	0.101	0.009
		(0.176)	(0.833)	(0.632)	(0.085)	(0.177)	(0.176)	(0.833)	(0.632)	(0.085)	(0.177)
AA	9	0.001	-0.327	0.046	-0.095	0.018	0.030	-0.024	0.050	-0.069	0.035
		(0.050)	(0.318)	(0.251)	(0.033)	(0.070)	(0000)	(0.035)	(0.023)	(0.041)	(0.022)
Α	25	-0.067	-1.684	0.052	-0.129	0.014	0.099	-0.615	0.118	0.115	0.043
		(0.038)	(0.155)	(0.119)	(0.016)	(0.034)	(0.021)	(0.141)	(0.022)	(0.030)	(0.009)
BBB	44	0.005	-90.298	-113.276	0.001	0.022	0.089	-1.818	-2.057	0.109	0.053
		(0.018)	(0.116)	(0.093)	(0.012)	(0.027)	(0.022)	(1.154)	(1.147)	(0.022)	(0.032)
BB	12	0.113	-2.898	-2.237	-21.019	0.184	0.260	-0.058	0.083	-1.822	0.163
		(0.042)	(0.223)	(0.176)	(0.023)	(0.050)	(0.109)	(0.092)	(0.101)	(0.543)	(0.089)
В	4	0.119	-30.461	-0.114	0.039	0.045	0.112	-13.806	0.014	0.073	0.062
		(0.064)	(0.410)	(0.308)	(0.041)	(0.088)	(0.063)	(6.826)	(0.047)	(0.022)	(0.118)
CCC	1	0.058	-9.933	-0.053	0.018	0.001	0.058	-9.933	-0.053	0.018	0.001
		(0.307)	(0.806)	(0.639)	(0.085)	(0.173)	(0.307)	(0.806)	(0.639)	(0.085)	(0.173)
Overall	93	0.070	-29.824	-23.849	-5.133	0.035	0.099	-11.389	-0.359	-0.186	0.058
		(0.016)	(0.080)	(0.053)	(0.008)	(0.018)	(0.041)	(3.628)	(0.215)	(0.112)	(0.040)

J.-Z. Huang et al.

of times         Metron         BC         Ls         DEJD         CDG         Metron         BC         Ls           ications         6         0.143         0.098         0.1133         0.082         0.090         0.124         0.104         0.078           reyclic         32         0.009         -9.674         -0.011         0.017         0.004         0.0533         (0.073)           reyclic         32         0.009         -9.674         -0.011         0.017         0.004         0.053         0.033           reyclic         32         0.009         -9.674         -0.011         0.017         0.004         0.053         0.033           reyclic         32         0.009         -9.674         -0.011         0.017         0.004         0.056         0.033           reyclic         32         0.003         0.017         0.0147         0.016         0.007         (0.007)         (0           restable         14         -0.056         -71.679         -0.135         0.0216         0.0147         0.0167         (0         0.075         0.0149         0.0167         (0         0.075         0.0218         0.0167         0.0167         0.0218         0	Rating	Number	Hedging pe	erformance (H	ledging performance ( $\mathrm{H}_{\mathrm{Eff}}$ ) of various structural models	ructural modε	sl					
Initiations         6         0.143         0.098         0.133         0.082         0.090         0.124         0.104         0.078           ications         6         0.143         0.098         0.133         0.082         0.090         0.124         0.104         0.038           icryclic         32         0.009         -9.674         -0.011         0.017         (0.027)         (0.033)         (0.071)         (0.063)         (0.038)           icryclic         32         0.009         -9.674         -0.011         0.017         (0.027)         (0.038)           icryclic         32         (0.027)         (0.137)         (0.107)         (0.014)         (0.031)         (0.039)           icryclic         14         -0.056         (0.133)         (0.014)         (0.015)         (0.016)         (0.073)           icryclic         14         -0.056         (0.153)         (0.021)         (0.015)         (0.016)         (0.016)           icryclic         0.056         (0.267)         (0.214)         (0.021)         (0.015)         (0.016)         (0.016)         (0.016)         (0.016)         (0.016)           icryclic         18         -0.056         (0.267)	or sector	of hrms	Merton	BC	LS	DEJD	CDG	Merton	BC	ΓS	DEJD	CDG
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$								Panel C: Sec	tor-specific av	erage hedge rat	tios	
ter cyclic 32 $(0.064)$ $(0.322)$ $(0.250)$ $(0.033)$ $(0.071)$ $(0.077)$ $(0.063)$ $(0.038)$ ter cyclic 32 $0.009$ $-9.674$ $-0.011$ $0.017$ $0.004$ $0.050$ $-0.011$ $0.039$ ter stable 14 $-0.054$ $0.003$ $0.030$ $0.060$ $0.193$ $0.060$ $0.053$ $0.056$ (0.027) $(0.167)$ $(0.017)$ $(0.014)$ $(0.031)$ $(0.009)$ $(0.167)$ $(0.007)ter stable 14 -0.054 0.003 0.030 0.060 0.193 0.060 0.053 0.056(0.039)$ $(0.267)$ $(0.137)$ $(0.121)$ $(0.047)$ $(0.015)$ $(0.030)$ $(0.101)(0.036)$ $(0.267)$ $(0.158)$ $(0.214)$ $(0.028)$ $(0.012)$ $0.082$ $-5.429$ $0.028(0.056)$ $(0.267)$ $(0.214)$ $(0.028)$ $(0.061)$ $(0.032)$ $(5.189)$ $(0.014)al 18 -0.056 -71.679 -103.578 -2.329 0.206 0.113 -6.520 -7.482(0.040)$ $(0.186)$ $(0.150)$ $(0.020)$ $(0.041)$ $(0.097)$ $(2.249)$ $(2.243)(0.041)$ $(0.065)$ $(0.228)$ $(0.187)$ $(0.024)$ $(0.024)$ $(0.033)$ $(0.069)$ $(0.088)$ $(0.087)(0.060)$ $(0.088)$ $(0.087)$ $(0.088)$ $(0.087)(0.069)$ $(0.088)$ $(0.087)(0.076)$ $(0.088)$ $(0.087)(0.076)$ $(0.088)$ $(0.087)(0.070)$ $(0.088)$ $(0.087)(0.070)$ $(0.066)$ $(0.506)(0.070)$ $(0.066)$ $(0.506)(0.070)$ $(0.016)$ $(0.080)$ $(0.0317)$ $(0.042)$ $(0.070)$ $(0.060)$ $(0.087)(0.076)$ $(0.070)$ $(0.056)$ $(0.506)(0.016)$ $(0.080)$ $(0.018)$ $(0.0$	Communications	9	0.143	0.098	0.133	0.082	0.090	0.124	0.104	0.078	0.067	0.050
$ \begin{array}{llllllllllllllllllllllllllllllllllll$			(0.064)	(0.322)	(0.250)	(0.033)	(0.071)	(0.027)	(0.063)	(0.038)	(0.017)	(0.060)
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	Consumer cyclic	32	0.009	-9.674	-0.011	0.017	0.004	0.050	-0.011	0.039	0.047	0.032
ter stable 14 $-0.054$ 0.003 0.030 0.060 0.193 0.060 0.053 0.056 8 0.096 $-36.861$ $-0.134$ 0.015 0.021) (0.047) (0.015) (0.030) (0.010) 8 0.096 $-36.861$ $-0.134$ 0.015 0.022 $-5.429$ 0.028 18 $-0.056$ $-71.679$ $-103.578$ $-2.329$ 0.026 0.113 $-6.520$ $-7.48211$ $-0.297$ $-7.1679$ $-103.578$ $-2.329$ 0.206 0.113 $-6.520$ $-7.48211$ $-0.297$ $-4.101$ 0.035 0.159 0.206 0.113 $-6.520$ $-7.48211$ $-0.297$ $-4.101$ 0.035 0.159 0.206 0.113 $-6.520$ $-7.48212$ $11$ $-0.297$ $-4.101$ 0.035 0.159 $-0.198$ 0.067) (2.249) (2.243) 13 $11$ $-0.297$ $-4.101$ 0.035 $0.159$ $-0.198$ 0.0669 (0.087) (0.077) 16 $0.148$ 0.098 $-4.252$ $-38.955$ 0.076 0.208 0.171 $-0.2410.150$ (0.150) (0.395) (0.317) (0.042) (0.057) (0.070) (0.066) (0.087) 93 0.070 $-29.824$ $-23.849$ $-5.133$ 0.035 0.076 $-3.310$ $-1.2060.016$ (0.016) (0.080) (0.053) (0.018) (0.018) (0.018) (0.350)			(0.027)	(0.137)	(0.107)	(0.014)	(0.031)	(0.009)	(0.167)	(0.007)	(0.008)	(0.005)
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	Consumer stable	14	-0.054	0.003	0.030	0.060	0.193	0.060	0.053	0.056	0.057	0.052
$ \begin{array}{llllllllllllllllllllllllllllllllllll$			(0.039)	(0.208)	(0.158)	(0.021)	(0.047)	(0.015)	(0.030)	(0.010)	(0.014)	(0.023)
$ \begin{array}{llllllllllllllllllllllllllllllllllll$	Energy	8	0.096	-36.861	-0.134	0.015	0.012	0.082	-5.429	0.028	0.048	0.030
$ \begin{array}{rrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrrr$			(0.056)	(0.267)	(0.214)	(0.028)	(0.061)	(0.036)	(5.189)	(0.014)	(0.024)	(0.016)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Industrial	18	-0.056	-71.679	-103.578	-2.329	0.206	0.113	-6.520	-7.482	0.207	0.096
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			(0.040)	(0.186)	(0.150)	(0.020)	(0.041)	(0.097)	(2.249)	(2.243)	(0.092)	(0.057)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Materials	11	-0.297	-4.101	0.035	0.159	-0.198	0.045	-0.055	0.181	0.146	0.107
$ \begin{array}{llllllllllllllllllllllllllllllllllll$			(0.065)	(0.228)	(0.187)	(0.024)	(0.053)	(0.069)	(0.088)	(0.087)	(0.051)	(0.037)
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Technology	4	0.148	0.098	-4.252	-38.955	0.076	0.208	0.171	-0.241	-12.060	0.075
1 93 0.070 -29.824 -23.849 -5.133 0.035 0.076 -3.310 -1.206 . (0.016) (0.080) (0.053) (0.008) (0.018) (0.018) (1.331) (0.738) 0			(0.150)	(0.395)	(0.317)	(0.042)	(0.087)	(0.070)	(0.066)	(0.506)	(3.304)	(0.028)
(0.080) $(0.053)$ $(0.008)$ $(0.018)$ $(0.018)$ $(1.331)$ $(0.738)$	Overall	93	0.070	-29.824	-23.849	-5.133	0.035	0.076	-3.310	-1.206	-1.179	0.042
			(0.016)	(0.080)	(0.053)	(0.008)	(0.018)	(0.018)	(1.331)	(0.738)	(0.571)	(0.023)

Table VII. Continued

group could lower the impact of uncertainty in the firm-by-firm estimation, as advocated by Schaefer and Strebulaev (2008). As such, using smoothed hedge ratios (i.e., either ratingor sector-specific (average) hedge ratios) should help mitigate this so-called "hedging crash risk."

Panel B of Table VII reports the results on hedging performance of rating-specific hedge ratios. A comparison with panel A of the table indicates that the overall  $H_{\rm Eff}$  in panel B is much less negative for the BC, LS, and DEJD models and, in fact, becomes statistically insignificant for the latter two models.<sup>12</sup> Although CDG's overall  $H_{\rm Eff}$  also increases from 3.5% to 5.8%, it is not significantly different from zero. On the other hand, the Merton overall  $H_{\rm Eff}$  increases from 7.0% to 9.9% and remains highly significant.

The hedging performance in individual rating groups also improves. For instance, the Merton  $H_{\text{Eff}}$  is now significantly positive for five out of seven groups (only two out of seven in panel A). For the BC model, its  $H_{\text{Eff}}$  for the BBB group, for example, increases from –90.3 (highly significant) in panel A to –1.82 (no longer significant) in panel B. For the LS model, its  $H_{\text{Eff}}$  for the BBB group also increases from a highly significant –113.3 in panel A to an insignificant –2.06 in panel B.

Results on hedging performance of sector-specific average hedge ratios, reported in panel C of Table VII, provide similar evidence as those in panel B do. Consider the overall  $H_{\rm Eff}$  first. Note that again,  $H_{\rm Eff}$  is much less negative for the BC, LS, and DEJD models than its counterparts in panel A, although it is still significant for the BC and DEJD models.<sup>13</sup> The CDG  $H_{\rm Eff}$  is more positive and still significantly different from zero. The Merton  $H_{\rm Eff}$  also increases slightly and remains highly significant. Overall, judging from the whole sample, averaging hedge ratios by ratings is more effective than averaging by industry in improving the hedging performance.

Next, consider  $H_{\text{Eff}}$  for individual sectors. For example, the LS  $H_{\text{Eff}}$  for "industrial" increases from -103.6 in panel A to -7.48 (albeit still significant) in panel C. The CDG  $H_{\text{Eff}}$  is now significantly positive for five sectors, as opposed to two sectors in panel A.

In summary, the results based on both the full sample and rating- or sector-specific subsamples in Table VII provide strong evidence that using smoothed hedge ratios helps improve the hedging performance. Furthermore, based on the hedging performance, the top three ranked models are the Merton, CDG, and DEJD models.

We should note that while the analysis of hedging effectiveness presented here corresponds to an out-of-sample test of hedge ratios, the estimates of model parameters make use of the full sample. In an untabulated analysis, we examine the hedging performance for 2- and 7-year CDS contracts (which are not included in the GMM estimation) and find that the results are consistent with those using the 5-year CDS. In particular, the ranking of the

- 12 Why is the BC overall  $H_{\text{Eff}}$  still large and negative with smoothed hedge ratios? The reason is that the BC model-implied hedge ratios are striking for certain firms in the sample. In an untabulated analysis, we find that these firms have an estimated default boundary *K/F* ranging from 1.26 to 1.54. When the asset value is close to this artificial boundary, the equity value becomes insensitive to the asset value. A low  $\partial E_{I} / \partial A_{I}$  inflates the model-implied equity sensitivity of the CDS spread.
- 13 The overall negative H<sub>Eff</sub> for the DEJD model is mainly caused by a BB-rated technology firm. When this firm is excluded from the sample, the hedging performance of the DEJD model is generally comparable to that of the CDG model (untabulated).

five models based on the their hedging performance remains the same. That is, our findings are robust to the aforementioned look-ahead bias.

### 6.6 Model-Implied Default Probabilities

The discussion so far has focused on the implications of structural models for variables under the risk-neutral measure. In this subsection, we examine model-implied  $\mathbb{P}$ -measure default probabilities. For comparison, we also include model-implied default probabilities under the (risk-neutral)  $\mathbb{Q}$ -measure.

As an important determinant of CDS spreads, risk-neutral default probabilities are straightforward to calculate using an estimated model. In order to calculate real default probabilities, we need to specify the dynamics of the underlying variables under the  $\mathbb{P}$ -measure and then estimate those  $\mathbb{P}$ -measure parameters. The GMM-based estimation of such parameters, however, requires that  $\mathbb{P}$ -measure moment conditions be specified. We do not pursue this approach in this analysis. Instead, we calibrate the  $\mathbb{P}$ -measure parameters in the analysis that follows when it is necessary.

For illustration we focus on the BC model—the simplest one among the three candidate models with a flat default boundary/barrier—in the analysis that follows. Given the specification of the BC model under  $\mathbb{Q}$ , its specification under  $\mathbb{P}$  involves only one extra parameter, the asset risk premium  $\pi_{\nu} \equiv \mu_{\nu} - r$ , where  $\mu_{\nu}$  is the expected asset growth rate. We calibrate  $\pi_{\nu}$  using the formula,  $\mu_{\nu} - r = \sigma_{\nu} \times SR_{\nu}$ , where  $SR_{\nu}$  denotes the asset Sharpe ratio (equal to the equity Sharpe ratio under the model). To this end, we set  $SR_{\nu}$  to 0.23, the equity Sharpe ratio of a median firm according to Chen, Collin-Dufresne, and Goldstein (2008), and then use firm-specific asset volatilities estimated earlier in Section 6.2 to calibrate firm-specific asset risk premiums.

Figure 8 plots the time series and term structure of the BC model-implied default probabilities under either the  $\mathbb{Q}$  measure (panel A) or the  $\mathbb{P}$  measure (panel B) over the full sample period. A comparison of panel A and Figure 1 indicates that the BC model fails to capture the surface of CDS spreads, given that the model assumes a constant recovery rate. As expected, the default probabilities under  $\mathbb{Q}$  are markedly higher than their counterparts under  $\mathbb{P}$ . Nonetheless, both panels show a spike in late 2002, consistent with Figure 1.

We can also compare the average model-implied real default probability with the average (historical) default rate for a given rating group. For the latter, we use the average issuer-weighted cumulative default rates by rating categories over 1920–2004 calculated by Moody's. Figure 9 plots the term structures of average default rates (solid line), the BC model-implied default probabilities under the  $\mathbb{Q}$  measure (blue dashed line) as well as the  $\mathbb{P}$  measure (red dotted line), for three different rating groups, single A (panel A), BBB (panel B), and BB (panel C). The AAA–A group is not considered here because, first, we do not have Moody's average default rates for the AAA–A group and secondly, the AAA–A group in our sample is dominated by the single A firms. Panel C includes only the BB names instead of the CCC–BB group for the similar reason.

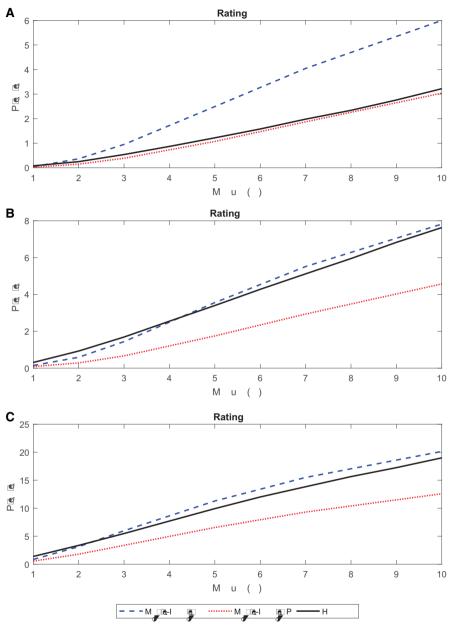
We make two observations from Figure 9. First, the BC model fits the Moody's average default rates well for A-rated names. The implication of this result is that the evidence based on single A firms in our sample is consistent with the notion of the credit spread puzzle: the model matches the average default rates but it underpredicts the CDS spreads. Second, the model underfits the average default rates for both BBB and BB names, especially at long horizons. To some extent, this result is not surprising given that on average, the model noticeably underestimates the CDS spreads for BBB and BB names over the full



sample. For the model to match the historical averages the period 1920–2004, we need higher asset volatility, default boundary, or both (than the estimates reported in Table III). Such parameter values also allow the model to fit the observed CDS spreads for BBB and BB names better, largely consistent with the credit spread puzzle.

# 7. Conclusion

Empirical studies of structural credit risk models are usually carried out using calibration, rolling window estimation, or regression analysis. This paper proposes a GMM-based specification test of these models. This alternative method allows us to directly estimate



**Figure 9.** Term structures of average default rates, and model implied risk-neutral and real default probabilities. This figure plots the term structure of average default rates (solid line), model-implied default probabilities under both the risk-neutral measure (blue dashed line), and the physical measure (red dotted line) based on the BC model, for three different rating groups, single A (panel A), BBB (panel B), and BB (panel C).

structural models, as well as test whether all the restrictions of a given model are satisfied, among other things.

For illustration, we apply the proposed specification test to five representative structural models using data on the term structure of CDS spreads and realized equity volatility (estimated with high frequency intraday data). We conduct the test using a sample of industrial firms over a post dot-com bubble and pre-financial crisis period that nonetheless includes some relatively high credit risk episodes. The test results show that the Merton (1974) model and the two diffusion-based constant-barrier models are all strongly rejected by the proposed specification test. However, the results also indicate that incorporating jumps or stationary leverage into a barrier model improves the overall fit of CDS spreads and equity volatility. Nonetheless, all five models have difficulty capturing the dynamic behavior of both equity volatility and CDS spread curves, especially for IG names. On the other hand, our results demonstrate that these models have a much better ability to explain the average sensitivity of CDS spreads to equity returns than their ability to explain the average CDS spread and equity volatility. Surprisingly, we also find that the Merton (1974) model provides the best hedging performance among all five models.

Overall, the main findings of this study, together with those of Bao and Pan (2013) on excess corporate bond return volatility, suggest a need for new structural models that can explain not only the credit spread puzzle but also the second moment variables. Another line of inquiry worth pursuing is to conduct a more rigorous and comprehensive analysis of finite-sample properties of the GMM test proposed in this study.

### Appendix

#### Table AI. Summary statistics of individual names

This table reports credit ratings, 5-year CDS spread, equity volatility, leverage ratio, asset payout, and recovery rate, for each of the 93 firms similar to those by ratings and sectors in Table I.

Company	Last rating	Five year CDS (%)	Equity volatility (%)	Leverage ratio (%)	Asset payout (%)	Recovery rate (%)
Air Prods & Chems Inc.	А	0.238	28.358	33.067	2.086	40.863
Albertsons Inc.	BBB	0.692	35.540	54.662	3.650	41.008
Amerada Hess Corp.	BB	0.817	28.458	61.871	2.929	40.081
Anadarko Pete Corp.	BBB	0.427	31.244	47.816	1.688	39.439
Arrow Electrs Inc.	BBB	2.175	44.325	62.279	2.259	39.269
Autozone Inc.	BBB	0.708	33.269	30.222	0.827	41.977
Avon Prods Inc.	А	0.230	27.128	17.924	0.998	41.353
Baker Hughes Inc.	А	0.298	39.469	20.584	1.764	40.833
Baxter Intl Inc.	BBB	0.493	39.739	33.159	1.739	40.526
BellSouth Corp.	А	0.550	43.254	39.213	3.308	41.848
Black & Decker Corp.	BBB	0.389	29.569	45.897	1.566	42.200
Boeing Co.	А	0.517	36.815	56.877	1.744	39.336
BorgWarner Inc.	BBB	0.572	29.766	48.270	1.285	40.623
Bowater Inc.	BB	2.751	30.755	62.578	3.583	41.287
CSX Corp.	BBB	0.607	29.651	69.128	2.305	40.486
Campbell Soup Co.	А	0.319	27.171	36.114	2.699	40.063
Caterpillar Inc.	А	0.350	32.081	57.902	1.992	40.122

(continued)

Table AI. Continued

Company	Last	Five year	Equity	Leverage	Asset	Recovery
Company	rating	CDS (%)	volatility (%)	ratio (%)	payout (%)	rate (%)
	rating	CD3 (70)	volatility (70)	1410 (70)	payout (70)	1410 (70)
Cendant Corp.	BBB	1.595	42.626	59.864	1.291	39.440
Centex Corp.	BBB	0.895	41.148	69.613	2.543	40.670
Clear Channel Comms Inc.	BBB	1.413	45.192	35.378	1.487	40.789
Coca Cola Entpers Inc.	А	0.327	34.774	68.903	2.281	40.019
Computer Assoc Intl Inc.	BB	2.889	54.727	35.045	1.044	35.840
Computer Sciences Corp.	Α	0.565	41.122	43.578	1.182	39.763
ConAgra Foods Inc.	BBB	0.470	27.510	43.829	3.516	39.320
Corning Inc.	BB	5.412	80.739	41.995	1.138	36.807
Delphi Corp.	BBB	1.470	40.828	77.164	1.535	40.539
Delta Air Lines Inc.	CCC	18.806	81.939	93.931	2.885	26.566
Devon Engy Corp.	BBB	0.732	31.487	56.495	2.281	40.513
Diamond Offshore Drilling Inc.	BBB	0.488	39.213	32.696	1.701	40.833
Dow Chem Co.	А	0.817	35.536	48.723	3.166	39.775
E I du Pont de Nemours & Co.	AA	0.241	30.318	37.916	2.574	41.409
Eastman Kodak Co.	BBB	1.317	37.618	56.431	2.550	38.839
Eaton Corp.	А	0.335	27.783	42.526	1.527	40.815
Electr Data Sys Corp.	BB	2.087	51.554	50.321	2.332	40.349
Eli Lilly & Co.	AA	0.219	35.486	13.956	1.898	40.494
Fedt Dept Stores Inc.	BBB	0.675	38.303	54.236	1.966	41.664
Ford Mtr Co.	BBB	2.977	47.060	92.612	2.769	41.849
GA Pac Corp.	BB	3.824	48.523	74.892	3.547	42.054
Gen Elec Co Inc.	AAA	0.427	36.356	63.713	2.223	40.883
Gen Mls Inc.	BBB	0.539	24.225	44.680	3.095	41.508
Gen Mtrs Corp.	BBB	2.434	35.537	94.017	2.595	41.278
Gillette Co.	AA	0.147	28.421	17.574	1.672	40.977
Goodrich Corp.	BBB	1.230	35.427	61.064	3.187	39.736
Goodyear Tire & Rubr Co.	В	7.671	65.509	88.106	2.245	39.840
H   Heinz Co.	A	0.310	23.404	39.061	3.199	41.748
Hilton Hotels Corp.	BBB	2.141	36.860	51.553	2.754	41.065
Home Depot Inc.	AA	0.222	39.170	14.502	0.741	42.223
IKON Office Solutions Inc.	BB	3.460	48.604	73.673	1.337	38.221
Intl Business Machs Corp.	A	0.381	31.166	32.683	0.578	39.991
Intl Paper Co.	BBB	0.740	30.566	58.274	2.944	39.674
J C Penney Co Inc.	BB	2.949	45.576	61.984	2.343	37.818
Jones Apparel Gp Inc.	BBB	0.634	32.547	26.906	1.353	41.338
Kerr Mcgee Corp.	BBB	0.745	26.472	59.613	3.398	41.242
Lockheed Martin Corp.	BBB	0.501	32.241	44.982	1.815	
Lockneed Martin Corp. Lowes Cos Inc.	A			44.982 19.222		41.173
Lowes Cos Inc. Ltd Brands Inc.	A BBB	0.356	36.642		0.587	41.788 41.529
		0.584	44.878	21.283	3.854	
Lucent Tech Inc.	B	9.525	96.827	63.895 57.910	1.255	37.988
MGM MIRAGE	BB ppp	2.167	33.197	57.910	2.675	39.764
Masco Corp.	BBB	0.612	33.101	35.400	2.758	42.234
Mattel Inc.	BBB	0.534	35.721	21.203	2.269	40.322
May Dept Stores Co.	BBB	0.608	36.953	52.074	3.923	41.765
Maytag Corp.	BBB	0.773	38.307	58.938	2.213	41.476
McDonalds Corp.	А	0.322	38.651	30.956	2.107	40.051

Downloaded from https://academic.oup.com/rof/article/24/1/45/5477416 by National Science and Technology Library -Root user on 29 September 2020

Company	Last	Five year	Equity	Leverage	Asset	Recovery
	rating	CDS (%)	volatility (%)	ratio (%)	payout (%)	rate (%)
Nordstrom Inc.	BBB	0.609	40.304	43.145	1.555	41.820
Norfolk Sthn Corp.	BBB	0.471	36.021	61.054	2.704	39.724
Northrop Grumman Corp.	BBB	0.675	26.992	51.679	1.844	40.890
Omnicom Gp Inc.	BBB	0.906	36.220	42.475	0.887	40.262
PPG Inds Inc.	А	0.360	27.727	37.415	2.667	42.133
Phelps Dodge Corp.	BBB	1.780	38.034	48.840	1.877	41.547
Pitney Bowes Inc.	А	0.211	27.063	46.124	2.645	41.674
Praxair Inc.	А	0.291	28.048	33.167	1.730	42.060
Procter & Gamble Co.	AA	0.163	23.275	21.002	1.289	40.450
Rohm & Haas Co.	BBB	0.353	29.283	43.281	2.241	42.235
Ryder Sys Inc.	BBB	0.590	29.285	65.616	2.294	39.827
SBC Comms Inc.	А	0.598	43.723	42.509	3.587	38.423
Safeway Inc.	BBB	0.724	39.373	52.084	1.893	41.592
Sara Lee Corp.	А	0.281	28.465	42.474	2.900	39.904
Sealed Air Corp. US	BBB	2.349	35.792	44.043	1.820	37.390
Sherwin Williams Co.	А	0.396	29.004	32.345	1.896	41.694
Solectron Corp.	В	4.976	86.414	54.483	1.908	39.241
Southwest Airls Co.	А	0.723	43.900	29.447	0.624	40.323
The Gap Inc.	BB	2.889	50.769	27.086	1.429	41.034
The Kroger Co.	BBB	0.754	39.574	55.452	1.960	41.729
Tribune Co.	А	0.413	25.200	34.934	1.500	41.228
Utd Tech Corp.	А	0.260	30.856	37.047	1.116	39.475
V F Corp.	А	0.323	25.458	31.046	2.687	38.877
Valero Engy Corp.	BBB	1.075	36.741	65.574	2.174	40.715
Visteon Corp.	BB	2.671	46.160	87.957	1.297	41.348
Wal Mart Stores Inc.	AA	0.193	32.359	20.540	0.991	39.991
Walt Disney Co.	BBB	0.714	43.767	38.906	1.644	39.191
Weyerhaeuser Co.	BBB	0.753	29.759	62.255	3.509	41.164
Whirlpool Corp.	BBB	0.477	31.043	58.506	2.305	40.512
Williams Cos Inc.	В	6.836	84.181	83.953	3.724	35.851

Table AI. Continued

# References

- Acharya, V. and Carpenter, J. (2002): Corporate bond valuation and hedging with stochastic interest rates and endogenous bankruptcy, *Review of Financial Studies* 15, 1355–1383.
- Acharya, V., Huang, J.-Z., Subrahmanyam, M., and Sundaram, R. K. (2006): When does strategic debt-service matter?, *Economic Theory* 29, 363–378.
- Acharya, V., Huang, J.-Z., Subrahmanyam, M., and Sundaram, R. K. (2019): Costly financing, optimal payout policies and the valuation of corporate debt, in: M. Crouhy, D. Galai, and Z. Wiener (eds.), *World Scientific Reference on Contingent Claims Analysis in Corporate Finance*, Vol. 3, pp. 77–126, World Scientific, Singapore.
- Andersen, T. G., Bollerslev, T., Diebold, F. X., and Labys, P. (2001): The distribution of realized exchange rate volatility, *Journal of the American Statistical Association* 96, 42–55.
- Anderson, R. W. and Sundaresan, S. (1996): Design and valuation of debt contracts, *Review of Financial Studies* 9, 37–68.

- Arora, N., Bohn, J., and Zhu, F. (2005): Reduced form vs. structural models of credit risk: a case study of three models, *Journal of Investment Management* 3, 43–67.
- Augustin, P., Subrahmanyam, M. G., Tang, D. Y., and Wang, S. Q. (2016): Credit default swaps: past, present, and future, *Annual Review of Financial Economics* 8, 175–196.
- Bai, J., Goldstein, R., and Yang, F. (2018): Is the Credit Spread Puzzle a Myth? Working paper, Georgetown University, University of Minnesota, and University of Connecticut.
- Bai, J. and Wu, L. (2016): Anchoring credit default swap spreads to firm fundamentals, Journal of Financial and Quantitative Analysis 51, 1521–1543.
- Bao, J. (2009): Structural models of default and the cross section of corporate bond yield spreads. Working paper, MIT.
- Bao, J., Chen, J., Hou, K., and Lu, L. (2015): Prices and volatilities in the corporate bond market. American Finance Association 2015 Boston Meetings Paper. Available at http://dx.doi.org/10. 2139/ssrn.2651243.
- Bao, J. and Hou, K. (2017): De facto seniority, credit risk, and corporate bond prices, *The Review of Financial Studies* 30, 4038–4080.
- Bao, J. and Pan, J. (2013): Bond illiquidity and excess volatility, *Review of Financial Studies* 26, 3068–3103.
- Bao, J., Pan, J., and Wang, J. (2011): Liquidity of corporate bonds, *Journal of Finance* 66, 911–946.
- Barndorff-Nielsen, O. and Shephard, N. (2002): Estimating quadratic variation using realized variance, *Journal of Applied Econometrics* 17, 457–478.
- Barndorff-Nielsen, O. and Shephard, N. (2004): Power and bipower variation with stochastic volatility and jumps, *Journal of Financial Econometrics* 2, 1–48.
- Bertsimas, D., Kogan, L., and Lo, A. W. (2000): When is time continuous?, *Journal of Financial Economics* 55, 173–204.
- Black, F. and Cox, J. (1976): Valuing corporate securities: some effects of bond indenture provisions, *Journal of Finance* 31, 351–367.
- Black, F. and Scholes, M. (1973): The pricing of options and corporate liabilities, *Journal of Political Economy* 81, 637–654.
- Bollerslev, T., Chou, R., and Kroner, K. (1992): ARCH modeling in finance: a review of the theory and empirical evidence, *Journal of Econometrics* 52, 5–59.
- Bollerslev, T., Engle, R., and Nelson, D. (1994): ARCH models, in: R. Engle and D. McFadden (eds.), *Handbook of Econometrics*, Vol. 4, pp. 2959–3038, Elsevier Science B.V., Amsterdam.
- Bongaerts, D., de Jong, F., and Driessen, J. (2017): An asset pricing approach to liquidity effects in corporate bond markets, *Review of Financial Studies* 30, 1229–1269.
- Campbell, J. and Taksler, G. (2003): Equity volatility and corporate bond yields, *Journal of Finance* 58, 2321–2349.
- Chen, L., Collin-Dufresne, P., and Goldstein, R. S. (2008): On the relation between the credit spread puzzle and the equity premium puzzle, *Review of Financial Studies* 22, 3367–3409.
- Chen, L., Lesmond, D. A., and Wei, J. (2007): Corporate yield spreads and bond liquidity, *Journal* of *Finance* 62, 119–149.
- Chen, L. and Zhao, X. (2006): Why do more profitable firms have lower leverage ratios? Working paper, Michigan State University and Kent State University.
- Chen, N. and Kou, S. G. (2009): Credit spreads, optimal capital structure, and implied volatility with endogenous default and jump risk, *Mathematical Finance* 19, 343–378.
- Chen, R., Fabozzi, F., Pan, G., and Sverdlove, R. (2006): Sources of credit risk: evidence from credit default swaps, *Journal of Fixed Income* 16, 7–21.
- Cochrane, J. H. (2009): Asset Pricing: Revised edition. Princeton University Press, Princeton, New Jersey.
- Collin-Dufresne, P. and Goldstein, R. (2001): Do credit spreads reflect stationary leverage ratios?, *Journal of Finance* 56, 1929–1957.

- Collin-Dufresne, P., Goldstein, R., and Martin, S. (2001): The determinants of credit spread changes, *Journal of Finance* 56, 2177–2207.
- Cremers, M., Driessen, J., and Maenhout, P. (2008): Explaining the level of credit spreads: option-implied jump risk premia in a firm value model, *Review of Financial Studies* 21, 2209–2242.
- Das, S. and Hanouna, P. (2009): Hedging credit: equity liquidity matters, *Journal of Financial Intermediation* 18, 112–123.
- Dick-Nielsen, J., Feldhütter, P., and Lando, D. (2012): Corporate bond liquidity before and after the onset of the subprime crisis, *Journal of Financial Economics* 103, 471–492.
- Du, D., Elkamhi, R., and Ericsson, J. (2018): Time-varying asset volatility and the credit spread puzzle, *Journal of Finance*, Forthcoming, available at https://doi.org/10.1111/jofi.12765.
- Duan, J. (1994): Maximum likelihood estimation using price data of the derivative contract, Mathematical Finance 4, 155–167.
- Duffie, D. and Lando, D. (2001): Term structures of credit spreads with incomplete accounting information, *Econometrica* 69, 633–664.
- Eom, Y. H., Helwege, J., and Huang, J.-Z. (2004): Structural models of corporate bond pricing: an empirical analysis, *Review of Financial Studies* 17, 499–544.
- Ericsson, J., Jacobs, K., and Oviedo, R. (2009): The determinants of credit default swap premia, *Journal of Financial and Quantitative Analysis* 44, 109–132.
- Ericsson, J. and Reneby, J. (2005): Estimating structural bond pricing models, *Journal of Business* 78, 707–735.
- Feldhütter, P. and Schaefer, S. (2018): The myth of the credit spread puzzle, *Review of Financial Studies* 31, 2897–2942.
- Ferson, W. E. and Foerster, S. R. (1994): Finite sample properties of the generalized method of moments in tests of conditional asset pricing models, *Journal of Financial Economics* 36, 29–55.
- François, P. and Morellec, E. (2004): Capital structure and asset prices: some effects of bankruptcy procedures, *Journal of Business* 77, 387–411.
- Frank, M. and Goyal, V. (2003): Testing the pecking order theory of capital structure, *Journal of Financial Economics* 67, 217–248.
- Friewald, N., Jankowitsch, R., and Subrahmanyam, M. (2012): Illiquidity or credit deterioration: a study of liquidity in the U.S. corporate bond market during financial crises, *Journal of Financial Economics* 105, 18–36.
- Geske, R. (1977): The valuation of corporate liabilities as compound options, *Journal of Financial* and *Quantitative Analysis* 12, 541–552.
- Hall, A. R. (2005): Generalized Method of Moments. Oxford University Press Inc., New York.
- Han, S. and Zhou, H. (2016): Effects of liquidity on the non-default component of corporate yield spreads: evidence from intraday transactions data, *Quarterly Journal of Finance* 06, 1650012.
- Hansen, L. P. (1982): Large sample properties of generalized method of moments estimators, *Econometrica* 50, 1029–1054.
- Hansen, L. P., Heaton, J., and Yaron, A. (1996): Finite-sample properties of some alternative GMM estimators, *Journal of Business & Economic Statistics* 14, 262–280.
- Hansen, L. P. and Singleton, K. J. (1982): Generalized instrumental variables estimation of nonlinear rational expectations models, *Econometrica* 50: 1269–1286.
- He, Z. and Milbradt, K. (2014): Endogenous liquidity and defaultable bonds, *Econometrica* 82, 1443–1508.
- He, Z. and Xiong, W. (2012): Rollover risk and credit risk, Journal of Finance 67, 391-430.
- Helwege, J., Huang, J.-Z., and Wang, Y. (2014): Liquidity effects in corporate bond spreads, Journal of Banking & Finance 45, 105–116.
- Huang, J.-Z. (2005): Affine structural models of corporate bond pricing. Working paper, Penn State University.

- Huang, J.-Z. and Huang, M. (2002): How much of the corporate-treasury yield spread is due to credit risk? NBER Asset Pricing Fall 2002 Conference paper. Available at http://ssrn.com/ abstract=1295816.
- Huang, J.-Z. and Huang, M. (2012): How much of the corporate-treasury yield spread is due to credit risk?, *Review of Asset Pricing Studies* 2, 153–202.
- Huang, J.-Z., Nozawa, Y., and Shi, Z. (2018): The global credit spread puzzle. Working paper, Penn State University, HKUST, and Tsinghua University.
- Huang, J.-Z., Rossi, M., and Wang, Y. (2015): Sentiment and corporate bond valuations before and after the onset of the credit crisis, *Journal of Fixed Income* 25, 34–57.
- Huang, J.-Z. and Shi, Z. (2016): Hedging interest rate risk using a structural model of credit risk. Working paper, Penn State University.
- Hull, J., Nelken, I., and White, A. (2005): Merton's model, credit risk, and volatility skews, *Journal of Credit Risk* 1, 3–27.
- Jagannathan, R., Skoulakis, G., and Wang, Z. (2002): Generalized methods of moments: applications in finance, *Journal of Business & Economic Statistics* 20, 470–481.
- Jones, E. P., Mason, S. P., and Rosenfeld, E. (1984): Contingent claims analysis of corporate capital structures: an empirical investigation, *Journal of Finance* 39, 611–625.
- Kapadia, N. and Pu, X. (2012): Limited arbitrage between equity and credit markets, Journal of Financial Economics 105, 542–564.
- Kelly, B. T., Manzo, G., and Palhares, D. (2016): Credit-implied volatility. Working paper, Chicago Booth.
- Kocherlakota, N. R. (1990): On tests of representative consumer asset pricing models, Journal of Monetary Economics 26, 285–304.
- Kou, S. G. (2002): A jump-diffusion model for option pricing, *Management Science* 48, 1086–1101.
- Leland, H. E. (2004): Predictions of default probabilities in structural models of debt, *Journal of Investment Management* 2, 5–20.
- Leland, H. E. and Toft, K. B. (1996): Optimal capital structure, endogenous bankruptcy, and the term structure of credit spreads, *Journal of Finance* 51, 987–1019.
- Lettau, M. and Ludvigson, S. (2001): Resurrecting the (C) CAPM: a cross-sectional test when risk premia are time-varying, *Journal of Political Economy* 109, 1238–1287.
- Longstaff, F., Mithal, S., and Neis, E. (2005): Corporate yield spreads: default risk or liquidity? New evidence from the credit-default-swap market, *Journal of Finance* 60, 2213–2253.
- Longstaff, F. and Schwartz, E. (1995): A simple approach to valuing risky fixed and floating rate debt, *Journal of Finance* 50, 789–820.
- Mahanti, S., Nashikkar, A., Subrahmanyam, M. G., Chacko, G., and Mallik, G. (2008): Latent liquidity: a new measure of liquidity, with an application to corporate bonds, *Journal of Financial Economics* 88, 272–298.
- McQuade, T. J. (2018): Stochastic volatility and asset pricing puzzles. Working paper, Stanford University.
- Meddahi, N. (2002): A theoretical comparison between integrated and realized volatility, *Journal* of *Applied Econometrics* 17, 479–508.
- Mella-Barral, P. and Perraudin, W. (1997): Strategic debt service, Journal of Finance 52, 531-556.
- Merton, R. (1974): On the pricing of corporate debt: the risk structure of interest rates, *Journal of Finance* 29, 449–470.
- Merton, R. (1976): Option pricing when underlying stock returns are discontinuous, *Journal of Financial Economics* 3, 125–144.
- Newey, W. K. and West, K. D. (1987): A simple positive semi-definite, heteroskedasticity and autocorrelation consistent covariance matrix, *Econometrica* 55, 703–708.
- Perrakis, S. and Zhong, R. (2015): Credit spreads and state-dependent volatility: theory and empirical evidence, *Journal of Banking & Finance* 55, 215–231.

- Predescu, M. (2005): The performance of structural models of default for firms with liquid CDS spreads. Working paper, Rotman School of Management, University of Toronto.
- Ramezani, C. A. and Zeng, Y. (2007): Maximum likelihood estimation of the double exponential jump-diffusion process, *Annals of Finance* 3, 487–507.
- Schaefer, S. and Strebulaev, I. A. (2008): Structural models of credit risk are useful: evidence from hedge ratios on corporate bonds, *Journal of Financial Economics* 90, 1–19.
- Schestag, R., Schuster, P., and Uhrig-Homburg, M. (2016): Measuring liquidity in bond markets, *Review of Financial Studies* 29, 1170–1219.
- Shi, Z. (2019): Time-varying ambiguity, credit spreads, and the levered equity premium, *Journal* of *Financial Economics*, forthcoming.
- Strebulaev, I. A. and Yang, B. (2013): The mystery of zero-leverage firms, *Journal of Financial Economics* 109, 1–23.
- Sundaresan, S. (2013): A review of Merton's model of the firm's capital structure with its wide applications, *Annual Reviews of Financial Economics* 5, 21–41.
- Tauchen, G. (1986): Statistical properties of generalized method-of-moments estimators of structural parameters obtained from financial market data, *Journal of Business and Economic Statistics* 4, 397–416.
- Vasicek, O. A. (1977): An equilibrium characterization of the term structure, *Journal of Financial Economics* 5, 177–188.
- Zhang, B. Y., Zhou, H., and Zhu, H. (2009): Explaining credit default swap spreads with equity volatility and jump risks of individual firms, *Review of Financial Studies* 22, 5099–5131.