Machine-Learning-Based Return Predictors and the Spanning Controversy in Macro-Finance*

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Abstract

We propose a two-step machine learning algorithm | the Supervised Adaptive Group LASSO (SAGLasso) method | that is suitable for constructing parsimonious return predictors from a large set of macro variables. We apply this method to government bonds and a set of 917 macro variables and construct a new, transparent, and easy-to-interpret macro variable with signi cant out-of-sample predictive power for excess bond returns. This new macro factor, termed the SAGLasso factor, is a *linear* combination of merely 30 selected macro variables out of 917. Furthermore, it can be decomposed into three sub-level factors: a novel \housing" factor, an \employment" factor, and an \in ation" factor. Importantly, the predictive power of the SAGLasso factor is robust to bond yields; namely, the SAGLasso factor is not spanned by bond yields. Moreover, we show that the unspanned variation of the SAGLasso factor cannot be attributed to yield measurement error or macro measurement error. The SAGLasso factor therefore provides a potential resolution to the spanning controversy in the macro- nance literature.

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1 Introduction

A growing literature has documented that excess returns of U.S. Treasury bonds are predictable. For instance, the predictors found thus far include forward rates (Cochrane and Piazzesi 2005) and yield-based variables constructed by using Itering (Du ee 2011),¹ as well as macroeconomic variables (e.g., Cooper and Priestley 2009; Ludvigson and Ng 2009). One debate in this literature is whether macroeconomic fundamentals have any such predictive power conditionally over bond yields. Among other things, this debate has important implications for macro- nance term structure models (MTSMs; see, e.g., Joslin, Priebsch, and Singleton 2014 (hereafter JPS)).

In this paper, we construct a new macro factor with strong and robust predictive power for bond risk premia using a two-step machine learning algorithm, termed the Supervised Adaptive Group LASSO (SAGLasso) method. We obtain the new macro variable (referred to as the SAGLasso factor) by applying the SAGLasso algorithm to a panel of 131 macro variables (along with six of their lags) | a total of 917 (131 × 7) macro variables | that are adjusted for data revisions and publication lags. In addition to its predictive power, the SAGLasso factor has two other noteworthy features. One is that the factor is parsimonious, transparent, and easy to interpret. The SAGLasso factor is a *linear* combination of merely 30 selected variables out of 917. Furthermore, it can be decomposed into three sub-level factors: a novel \housing" factor, an \employment" factor, and an \in ation" factor | which consist of 13, 11, and 6 macro variables, respectively. The other feature is that the SAGLasso factor is unspanned. Intuitively, this means that the SAGLasso factor is not subsumed (spanned) by yield factors in either predictive regressions or MTSMs. As such, the SAGLasso factor can potentially help resolve the spanning controversy in the macro- nance literature | the debate on whether macro-based return predictors are spanned or not.

We begin our analysis by describing the two-step SAGLasso method, followed by its implementation using the panel of 131 macro series. We construct eight sub-level factors | such as the

¹See also Fama and Bliss (1987), Stambaugh (1988), and Campbell and Shiller (1991).

\housing," \employment," and \in ation" factors | in the rst step and then the SAGLasso factor in the second step of the procedure. Note that we control for contemporaneous yields in both steps to minimize the information overlap between the SAGLasso factor and the yield curve.

Next, we examine the conditional predictive power of the SAGLasso factor for bond risk premia by testing two hypotheses. The rst one, Spanning Hypothesis I, states that macro variables have no incremental predictive power over the current yield curve, the rst three principal components (PCs) of yields. The second one, Spanning Hypothesis II | a stronger version of the rst hypothesis | posits that macro variables have no incremental predictive power over the Itration generated by the yield curve, proxied by the rst ve yield PCs Itered from a dynamic term structure model. Our results from both in-sample and out-of-sample tests strongly reject the two spanning hypotheses when the 5-44S. t361(f6()2295(t8(te060)he)-361(partte060)hf30060)th-30060)two60w(ariabl7er)sy32o60ariulrationres

spanned/explained by the current yield curve. Importantly, this result is robust to measurement errors in yields or in the SAGLasso macro variable itself. Taken together, these indings suggest that the SAGLasso factor provides a potential resolution to the spanning controversy.

To summarize, this study contributes to the macro nance literature in three dimensions. First, it is among the rst to introduce a machine learning algorithm suitable for constructing parsimonious return predictors from a large set of macro variables. Second, using this algorithm we construct a new, easy-to-interpret macro variable that has strong out-of-sample conditional predictive power for bond risk premia. Moreover, unlike commonly used macro variables in the literature, the SAGLasso factor is unspanned and has tiny measurement error. Third, we show that, due to its unique features, the SAGLasso factor can address those concerns raised in Bauer and Rudebusch (2016; hereafter BR), Bauer and Hamilton (2018; hereafter BH), and Ghysels, Horan, and Moench (2018) in a uni ed manner and thus can potentially help resolve the spanning controversy.

While this paper focuses on linear models of predictors, two related studies use nonlinear machine learning models to construct bond return predictors (but do not address the spanning controversy). Huang et al. (2016) nd that the macro series selected by SAGLasso is robust to various nonlinear models they consider. Bianchi, Bechner, and Tamoni (2021) study bond risk premia using tree-based algorithms as well as neural networks and nd that their superb statistical performance translates into large economic gains. While these highly nonlinear methods can accommodate more complex data, the SAGLasso method can lead to easier-to-interpret return predictors.³

The remainder of the paper is organized as follows. Section 2 states Spanning Hypotheses I & II, followed by Section 3 on the data we use. Section 4 presents the SAGLasso algorithm, constructs the SAGLasso factor, and examines its properties. Section 5 revisits the spanning controversy. Section 6 concludes. Appendix A lists some notation and terms frequently used in the paper.

³Several other studies focus on the application of machine learning in the other nance markets. Freyberger et al. (2020) use Group Lasso to study the impact of characteristics on expected stock returns. Gu et al. (2020) compare Group Lasso with other machine learning methods in the context of stock return prediction. Bali et al. (2021) and He et al. (2021) apply nonlinear machine learning models to inferring corporate bond risk premiums.

2 Hypotheses on the Predictive Power of Macro Variables

2.1 Basic Setup

We use continuously compounded annual log returns on an n-year zero-coupon Treasury bond in excess of the annualized yield on a one-year zero-coupon Treasury bond. That is, for $t=1,\cdots,T$, excess returns $rx_{t;t+12}^{(12n)}=r_{t;t+12}^{(12n)}-y_t^{(12)}=ny_t^{(12n)}-(n-1)y_{t+12}^{(12(n-1))}-y_t^{(12)}$, where $r_{t;t+12}^{(12n)}$ is the one-year log holding-period return on an n-year bond purchased at the end of month t and sold at

fraction of the variation in the term structure (Litterman and Scheinkman 1991). If the current yield curve is supposed to contain almost all the information useful for determining term premia, we arrive at Spanning Hypothesis I (a hypothesis formulated and tested by JPS and BH):

$$H_0^{S1}$$
: in Eq. (1), if $Z_t = PC_{1-3:t}^0$, then $\beta_F = 0$,

where PC_{1}^{o} $_{3} = (PC_{1}^{o}, PC_{2}^{o}, PC_{3}^{o})$, the vector of the rst three PCs of the observed yield curve.

Interestingly, Du ee (2011) nds that the fourth and fth PCs are also informative about predicting bond returns. These factors need to be estimated using Itering techniques based on both current and historical yields, however, as the e ects of such factors on cross-sectional yields are too small to dominate measurement error in observed yields. Nonetheless, a natural question is whether macro variables contain information about future bond returns that is not captured by the Itration generated by the yield curve process. If the \true" yield curve is Markov, as is commonly assumed in term structuring modeling, this question leads to Spanning Hypothesis II:

$$H_0^{S2}$$
: in Eq. (1), if $Z_t = PC_{1-5:t}$, then $\beta_F = 0$,

where $PC_{1\ 5}=(PC_{1},\ldots,PC_{5})$, the vector of the rst ve PCs of the *noise-uncontaminated* yield curve. Given the predictive power of Itered $PC_{4\ 5}$, H_{0}^{S2} provides a stronger test of the conditional predictive power of F_{t} than does H_{0}^{S1} .⁴ We also consider an alternative version of H_{0}^{S2} where Z_{t} is the spanned \cycle" factor of Cieslak and Povala (2015) in Internet Appendix IA.F.

Small-sample distortions may also take place in tests of H_0^{S1} and H_0^{S2} . BH demonstrate that estimates of standard errors in the t-test of $\beta_F=0$ can be biased because PCs (Z_t) are typically persistent and autoregressive with innovation terms that are possibly correlated with e_{t+12} . They propose a bootstrap procedure to account for the size distortion and conclude that much of extant veridence against the spanning hypothesis is in fact spurious." Besides the statistical inference about β_F in Eq. (1), BH also study the nite-sample distribution of the increase in R^2 when F_t is added to the regression. They show that serially correlated e_{t+12} due to overlapping observations could

 $^{^4}$ The use of PC_4 $_5$ rather than PC_4^o $_5$ in H_0^{S2} is because the latter's predictive power is weaker (see Internet Appendix IA.A). The version of H_0^{S2} based on PC_4^o $_5$ is examined in JPS, BR, and BH.

substantially in ate the incremental R^2 in small samples, even if F_t provides no help in predicting bond returns. We test H_0^{S1} and H_0^{S2} by conducting an asymptotic inference (Sections 4.4.2) as well as an MTSM-based nite-sample inference (Section 5.2).

3 Data

We use monthly data on bond returns and macroeconomic variables over the period January 1964 to December 2014 in our analysis. The start of our sample coincides with that of many other studies that also use the Fama-Bliss yield data set (e.g., Cochrane and Piazzesi 2005; Ludvigson and Ng

our real-time macro data is the Archival Federal Reserve Economic Data (ALFRED) database at the Federal Reserve Bank of St. Louis, which is a collection of vintage versions of U.S. economic data and contains more monthly sampled series than does the Philadelphia Fed's Real-Time Data Set. Appendix B includes the list of the 131 series in Table A.1 and describes how our macro data are compiled. The 131 series are organized in a hierarchical manner. Such a cluster structure of macro variables turns out to be useful to model selection. To that end, following Ludvigson and Ng (2011), we group the 131 series into eight categories: i) output (17 series); ii) labor market (32 series); iii) housing sector (10 series); iv) orders and inventories (14 series); v) money and credit (11 series); vi) bond and FX | interest rates or nancial (22 series); vii) prices or price indices (21 series); and viii) stock market (4 series). Column 2 of Table A.1 reports the group ID of each series. Section 4.2 shows that some of the eight groups have stronger predictive power than the others.

4 Adaptive-Lasso-Based Model Selection

In this section we rst describe the supervised adaptive group lasso algorithm. We next use the algorithm to construct a macro factor with low correlations to the yield curve. We then examine the predictive power of this new macro factor for future bond returns as well as economic gains of such bond return predictability.

4.1 Supervised Adaptive Group Lasso

For a $T \times 1$ response vector \mathbf{y} , consider the following penalized least squares (PLS) function:

$$f^{\text{PLS}}(\beta) = \|\mathbf{y} - \mathbf{X}\beta\|^2 + \lambda \underbrace{\mathbf{y}^{\text{N}}_{\text{(Mo5(yie)/F15 10.9031(1 11.9552 Tf 0 -37.832 Td)}^{\text{N}}} 2erv1Td}_{\text{(Mo5(yie)/F15 10.9031(1 11.9552 Tf 0 -37.832 Td)}}$$

lasso estimate is given by $\hat{\beta}^{lasso} = \arg \min f^{PLS}(\beta)$.

If λ is zero, then β^{lasso} equals the OLS estimate, β^{ols} , provided that the OLS estimation is feasible. Recall that none of β^{ols} 's components are zero. However, as λ increases, some components of β^{lasso} will shrink to zero, and as a result, the corresponding \useless" explanatory variables will be dropped and the resulting regression model will become more parsimonious.

Lasso has several advantages over the OLS. First, by construction, lasso reduces the variance of the predicted value and thus improves the overall (out-of-sample) forecasting performance. Second, the OLS is known to have poor nite sample properties when the dimension of parameters to be estimated is comparable with the number of observations. For instance, in our case there are 131 macro series along with six of their lags $| 917 (131 \times 7)$ macro variables in total | with only 600 observations for each series. Lasso is developed to handle such problems. Third, lasso leads to a much more parsimonious and easier-to-interpret model than the OLS. In fact, the parsimonious or sparse feature of lasso distinguishes it from ridge regression, another shrinkage method.

Despite lasso's popularity, one limitation of the method is that lasso estimates can be biased.

Zou (2006) shows that this problem can be xed by using Adaptive Lasso, which minimizes the following objective function:

$$\|\mathbf{y} - \mathbf{X}\boldsymbol{\beta}\|^2 + \sum_{i=1}^{N} \lambda_i |\beta_i|, \tag{3}$$

where different tuning parameters $\{\lambda_i\}$ are introduced to penalize different β_i s separately.

We construct a macro-based return predictor in two steps. In the rst step, we utilize the cluster structure of our macroeconomic panel and consider variable selection separately within each of the eight groups/clusters formed in Section 3; that is, we screen out less important or irrelevant individual economic series and identify informative ones within each cluster using adaptive lasso. This is done for three reasons. First, even variables within the same group may represent certain quantitative measurements of di erent economic sectors. For instance, the Industrial Production (IP) Index of Consumer Goods and the IP Index of Materials (in group i) might be connected

to bond risk premia in a di erent manner. Second, we want to select macroeconomic measures that are jointly signi cantly associated with bond risk premia. Third, adaptive lasso selects only a small number of macro variables within each cluster and thus allows us to construct parsimonious models, including easy-to-interpret group macro factors if necessary.

In the second step, we consider all the groups together, each of which now consists of only those macro variables selected in step one, and then conduct variable selection at the group level. We implement this idea using the Group Lasso of Yuan and Lin (2006) to deal with situations in which covariates are assumed to be clustered in groups (see Appendix C). That is, we select important clusters using group lasso, thereby identifying in uential economic sectors in addition to individual variables selected in the rst step.⁷

We refer to this two-step procedure as the supervised adaptive group lasso (SAGLasso) algorithm.⁸ Its key feature is to consider penalized time-series selection at both the within-cluster level and the cluster level. We construct bond return predictors by applying SAGLasso to a large set of macro series in this study. SAGLasso should also be useful in similar big data applications in nance and economics.

4.2 A Macro-Based Return-Forecasting Factor

This subsection implements the two-step SAGLasso procedure using the average excess return (the bond market return), $arx_{t;t+12} = \frac{1}{(n_b-1)} \sum_{n=2}^{n_b} rx_{t;t+12}^{(n)}$, as the dependent variable, where n_b equals 5 (10) when the full (post-1984) sample is used.

First, we perform model selection in each of the eight groups of macro series separately, using only macro variables within the same group along with their six lagged values. To minimize the

⁷Using high-dimension model selection (e.g., Huang, Shi, and Zhong 2015), Huang, Li, Ni, and Shi (2016) nd that the variables selected under the SAGLasso procedure are robust to a variety of nonlinear models. Bianchi, Bechner, and Tamoni (2021) also emphasize that it is important to exploit the cluster structure of the macroeconomic panel and do selection within groups and across groups. As such, di erent machine learning methods seemingly can capture the \common" cluster structure of the same macro data, at least for the purpose of bond return predictions.

⁸In statistical learning, a problem is considered to be supervised if the goal is to predict the value of an outcome measure based on a variety of input measures. See Appendix C for more details of the SAGLasso procedure.

information overlap with respect to yield curve factors, we include the rst three yield PCs in our variable selection but do not penalize the associated coe cients. Put di erently, in the regression framework of Eq. (1), Z_t is $PC_{1-3,t}^0$ but β_Z are not penalized; F_t includes contemporaneous and lagged macro variables in a given group and β_F are subject to shrinkage. Therefore, at the intragroup level of group j, we minimize the following objective function:

$$\|\mathbf{arx} - \mathbf{Z}\|_{Z;j}^{h1i} - \mathbf{F}\|_{F;j}^{h1i}\|^2 + \sum_{i=1}^{7N_j} \lambda_i^j |\beta_{F;j;i}^{h1i}|,$$

where λ_{j}^{i} is the tuning parameter; N_{j} denotes the number of economic series contained in group j; $\beta_{F;j;i}^{h1}$ is the i-th component of $\beta_{F;j}^{h1}$; and the superscript 1 emphasizes that these beta coexcients are obtained in the rst step of the SAGLasso procedure.

This rst step allows us to screen out a large portion of candidate predictors within each group. In total, only 39 out of 131 series remain and have non-zero coecients on their contemporaneous and/or lagged values after the adaptive lasso is applied; the number of the selected macro variables is only 58 out of 917 (131 \times 7). Let \widehat{X}_j^{h1i} , $j=i,\ldots,viii$, denote the set of macro variables, in group j, that survive from the rst stage.

In the second step, we select those relevant \widehat{X}_{j}^{h1i} using group lasso. Yield PCs are included as control variables as before. The results from the group lasso show that the coe-cients of groups i, iv, v, vi, and viii are shrunk to exactly zero; particularly, group vi (bond and FX) is not selected as a result of controlling for yield factors. For each of the three selected groups | labor market (group ii), housing (group iii), and price indices (group vii) | the group lasso solution obtained from Eq. (19) in Appendix C yields its corresponding group macro factor:

$$\widehat{g}_{\mathbf{j}} = \widehat{X}_{\mathbf{j}}^{h1/j} \widehat{\beta}_{\mathbf{j}}^{h2/j}, \qquad \mathbf{j} = ii, iii, vii,$$
(4)

where j denotes the index of group j whose beta coe cient in step two, $\widehat{\beta}_{j}^{h2i}$, is not zero. For ease of reference, we relabel $\{\widehat{g}_{i}\}$ as $\{\widehat{g}_{h}; h=1,2,3\}$. They each have a clear economic interpretation by

 $^{^9}$ For instance, consider the largest group, the \labor market," that originally contains 32 series and thus 32 \times 7 (=224) variables. Column 7 of Table A.1 indicates that only ve series (out of 32), #41, #44, #46, #48, and #49, are selected and that only 11 out of the original 224 variables are selected, including lag-5 and lag-6 of #41; #44 along with its lag-1, lag-2, and lag-3; #46 along with its lag-2; #49 along with its lag-2; and #49 itself.

construction and represent the employment, housing, and in ation factors, respectively.

Unlike in ation and employment, which are commonly incorporated in MTSMs and are well motivated by certain equilibrium term structure models (e.g., Wachter 2006), the housing sector has received little attention in the term structure literature. Given that \hat{g}_2

single aggregate macro predictor using the aforementioned three group factors:

$$\widehat{G} \equiv \sum_{h=1}^{3} \widehat{g}_{h}. \tag{5}$$

We refer to this predictor as the SAGLasso (single) macro factor hereafter. Note that this factor is a linear combination of only 30 macro variables belonging to merely 19 di erent series, yet it has strong predictive power for bond risk premia as shown below.

4.3 A Recursively Constructed SAGLasso Factor

The SAGLasso factor constructed in Section 4.2 is based on the full sample and is an unconditional/static factor. Below we construct a dynamic SAGLasso factor recursively. To avoid forward-looking bias, we estimate everything using only the information available at the time of the forecast; namely, we recursively re-estimate *both* factors and parameters when the new information becomes available. We denote a recursively constructed factor by a tilde (e.g., \widetilde{G}) to differentiate it from its unconditional counterpart, denoted by a hat (e.g., \widehat{G}).

Suppose we want to construct \widetilde{G} at month t based on observations from t-R to t-1 and use the predictor to help forecast one-step-ahead annual excess bond returns, where R>1 denotes the number of months included in the training period. Namely, in month t=R we have the following information set of monthly observations available: $\mathcal{F}_R=\{X_t,\{rx_{t:t+12}^{(n)},2\leq n\leq 5\},t=1,\ldots,R\}$.

To examine the importance of macro variables over time, we focus on rolling-window estimations. That is, we construct \widetilde{G} at, say, t+1 using observations from t-R+1 to t. We use R=240 (a 20-year training period) in this exercise. Figure 3 depicts the importance of individual macro variables over time. From the rolling-window prediction at time t, we extract coefficients of standardized macro variable k and their lagged values $\beta_{k;l;t}$ ($1 \le k \le 131, 0 \le l \le 6$), and map their

 $^{^{10}}$ See, e.g., Lewellen (2015) who uses a 10-year rolling window to form OLS-based forecasts of individual stock returns and nds that the importance of many characteristics diminishes over time. The procedure using an expanding window to construct \widetilde{G} has higher stability than that using the rolling window: $\widehat{g}_1, \widehat{g}_2$ and \widehat{g}_3 are the only groups selected. At the individual level, variables #42 (belonging to \labor market") and #53 (belonging to \housing sector") are the only new variables selected in certain months (and not included in the unconditional \widehat{G} factor). The predictive power of \widetilde{G} with the expanding window is closely comparable to that with the rolling-window.

norm $\sqrt{\sum_l \beta_{k;l;t}^2}$ to the color gradients displayed on the right side of the gure. At the group level, the selection results are fairly stable over time: The labor, housing, and in ation groups are selected in most months. The only exception is the 2002{2005 period, during which macro variables in housing and in ation groups diminished in importance and a couple of variables on industrial production are selected instead. At the individual level, the selected macro series are consistent with the results in Figure 1. Within the labor market group, nonfarm payrolls in the manufacturing and nancial sectors play crucial roles in bond return predictions. In the in ation group, the commodity price index appears the most prominent determinant of bond risk premiums.

4.4 Predictive Power of the SAGLasso Factor

4.4.1 In-Sample Evidence

Figure 2 plots the SAGLasso factor (in blue) and excess returns on the ve-year bond (in orange) in the full sample period, where shaded areas indicate the periods designated by the National Bureau of Economic Research (NBER) as recession periods. As expected, \hat{G} captures the countercyclic component in risk premia and leads movements in the realized bond returns. Indeed \hat{G} generally starts rising at the early stage of economic downturns and peaks during recessions; accordingly, excess bond returns follow and tend to peak toward the end of (or even after) recessions.

Panel A of Table 1 presents results on the in-sample predictive power of \widehat{G} , for 2-, 3-, 4-, and 5-year bonds, over the full sample. Test statistics are reported for two di erent standard errors: Hansen and Hodrick (1980) GMM (in parentheses) and Newey and West (1987) (in brackets). ¹² Columns (1){(4) show that \widehat{G} alone has signicant predictive power for excess returns, with the R^2 ranging from 0.35 for the 2-year bond to 0.39 for the 5-year one. Columns (5){(20) indicate that the

¹¹Given that the housing market boom after the early 2000s recession makes the share of housing consumption less of a concern, it is unsurprising that variables in the housing sector become less important in this period. By the same logic, the decline in the importance of in ation indices can be attributable to the stable in ation uncertainty in 2000s (e.g., Wright 2011).

¹²In an earlier version, we also report the t-statistics with Hodrick (1992) 1B covariance estimator, which is constructed using the approximate method of Wei and Wright (2013). The results for \widehat{G} are qualitatively similar, but other return predictors tend to lose their signic cance with the Hodrick standard errors.

signi cance of \widehat{G} is robust to each of the following four factors: (a) a modi ed LN09 factor (\widehat{LN}^m) , (b) the Cochrane and Piazzesi (2005) forward-rate factor (CP), the Du ee (2011) hidden factor (\widehat{H}) , and the convergence gap (\widehat{CG}) de ned by Berardi et al. (2021). The \widehat{G} factor, however, does not completely subsume any of these four factors. The main reason is that whereas \widehat{G} is a pure macro factor by construction, \widehat{LN}^m includes Treasury and FX variables (group vi), \widehat{CG} exploits information in the Federal Funds rate market, and both \widehat{CP} and \widehat{H} are purely yield-curve-based factors. For example, \widehat{G} does not subsume \widehat{CG} for the 2-year bond in the bivariate regression. This result is intuitive given that by construction, \widehat{CG} is expected to be most informative about short-term bond premiums while \widehat{G} is trained on the aggregate bond market returns rather than a speci c-maturity bond. As another example, if yield PCs are not controlled for in the second step of the construction of \widehat{G} , then the resultant \widehat{G} subsumes \widehat{LN}^m (Huang and Shi 2010).

Panel B reports the results for 2-, 5-, 7-, and 10-year bonds for the post-1984 subsample. While the results on \widehat{G} are generally similar to their counterparts in panel A, the predictive power of the other return predictors all becomes weaker except for \widehat{CG} . For instance, \widehat{G} now subsumes \widehat{LN}^m under the HH correction, but \widehat{CG} has increased values of both the t-statistics and incremental R^2 s.

In summary, Table 1 shows that \widehat{G} has both signi-cant unconditional and conditional predictive power for bond risk premia. Additionally, \widehat{G} subsumes other macro-based predictors post-1984. In Internet Appendix IA.B, we also conduct in-sample spanning tests and nd that both H_0^{S1} and H_0^{S2} are overwhelming rejected.

4.4.2 Out-of-Sample Accuracy

We next examine the out-of-sample performance of the SAGLasso factor, focusing on its incremental power above and beyond yield-curve factors.

 $^{^{13}}$ In an untabulated analysis, we also consider the output gap factor (gap) of Cooper and Priestley (2009); the new-order factor (NOS) of Jones and Tuzel (2013); the Cieslak and Povala (2015) \cycle" factor based on yield curves and in ation; and a realized jump-mean factor constructed by Wright and Zhou (2009) (the latter two for the post-1984 sample only). We nd that \hat{G} subsumes gap and NOS and is not driven out by the other two factors. Chernov and Mueller (2012) uncover a hidden factor that captures in ation expectations as well as bond risk premia; however, this \survey" factor is present only in models estimated with survey-based information.

We divide the sample into training/estimating and out-of-sample (testing) portions. The former consists of R>1 observations. We use xed rolling-windows with R=240 (R=180) for the full sample (sub-sample) analysis. If P denotes the number of one-step-ahead predictions, then T=R+P+12, where T is the total number of observations of macro series. We construct \widetilde{G} recursively month by month using only information available at the time of estimation as described in Section 4.3. Similarly, we recursively re-estimate the yield-curve factors $PC_{1-3;t}^o$ and $PC_{1-5;t}^o$ whose dynamic versions are denoted $\widetilde{PC}_{1-3;t}^o$ and $\widetilde{PC}_{1-5;t}^o$.

Given the dynamic macro and yield-curve factors, we form our out-of-sample tests of H_0^{S1} as follows: Consider a \restricted" benchmark model and an \unrestricted" model, where the former is the return forecasting model solely based on \widetilde{PC}_1^o $_{3;t}$ and the latter includes \widetilde{PC}_1^o $_{3;t}$ and G_t . Given this pair of nested specilications, we can obtain their time series of realized forecast errors over the entire (out-of-sample) testing period and then conduct a model comparison. In other words, the statistical signilicance of G's incremental predictive power can be assessed by testing the null hypothesis that the restricted model encompasses the unrestricted one. We form tests of H_0^{S2} similarly by replacing \widetilde{PC}_1^o $_{3;t}$ with \widetilde{PC}_1 $_{5;t}$.

Panel A of Table 2 accesses the out-of-sample performance of G with three metrics: the out-of-sample R^2 (Campbell and Thompson 2008) aloing R^2

(10-year) bond in the full sample (subsample). 16.

Panel A1 (A2) shows that incorporating G_t into the restricted model based on $\widetilde{PC}_{1-3;t}^o$ and a constant improves the model performance substantially in either the full or sub sample. First, both the ENC-REG and ENC-NEW test statistics greatly exceed their asymptotic critical values, regardless how the asymptotic ratio of P/R is specified, thereby rejecting both H_0^{S1} and H_0^{S2} . Second, including G_t also raises R_{oos}^2 substantially. For instance, when $\widetilde{PC}_{1-3;t}^o$ is augmented with G_t , R_{oos}^2 ranges from 0.271 for the 5-year bond to 0.349 for the 2-year bond in the full-sample analysis. Note that the high values of R_{oos}^2 here are partially attributable to the negative R_{oos}^2 values under the restricted models. To summarize, panel A shows that the improvement in forecasting accuracy due to G is statistically significant.

4.4.3 Economic Values

We now examine economic gains of \widetilde{G} 's out-of-sample predictive power. We follow Campbell and Thompson (2008) and assess a mean-variance investor's utility gains from trading on \widetilde{G} against a benchmark. The investor is assumed to dynamically allocate her portfolio between an N-year bond ($N \geq 2$) and a one-year bond (the risk-free asset) at a monthly basis, based on the standard optimal (timing) strategy (e.g., Thornton and Valente 2012). Given her risk aversion coe cient (γ) and the N-year bond return volatility at time t, the investor implements the strategy based on her out-of-sample forecasts of the N-year bond risk premium.

We consider three return predictors: \widetilde{G}_t , \widetilde{PC}_1^o 3, and \widetilde{PC}_1^o 3, the timing strategies based on these predictors are denoted \mathcal{S}^G , \mathcal{S}^Y , and \mathcal{S}^{G+Y} , respectively. In addition, we consider a buyand-hold strategy, denoted \mathcal{S}^{BH} . We then compare \mathcal{S}^G against \mathcal{S}^{BH} , as well as \mathcal{S}^{G+Y} against \mathcal{S}^Y , to examine incremental welfare gains due to \widetilde{G} . Specifically, we calculate the certainty equivalent return (CER) values for each month in the testing sample and then estimate the following regression: $u_{g;t}-u_{0;t}=\nu+\varepsilon_t$, where $u_{g;t}$ and $u_{0;t}$ represent realized utilities generated by strategies \mathcal{S}^G and \mathcal{S}^{BH} 16Bianchi et al. (2021) and that the performance of their macro factors is also relatively weak for short-term bonds.

 (S^{G+Y}) against S^Y , respectively. To examine whether the incremental utility gains are signicant or not, we test the null hypothesis that $\nu=0$ (denoted H_0) using a variant of the Diebold and Mariano (1995) test, proposed by Harvey et al. (1997), that accounts for autocorrelation in the forecasting errors.

Panel B of Table 2 reports the annualized CER values along with the corresponding p-values for H_0 (in angel brackets) with N=2,3,4,5 for the full sample or N=2,5,7,10 for the post 1984 subsample. In each panel we consider two risk version levels: $\gamma=3$ as adopted by Campbell and Thompson (2008) and Gu et al. (2020), and $\gamma=5$ as adopted by Thornton and Valente (2012) and Bianchi et al. (2021). We also follow these studies to limit the portfolio weight on the N-year bond to lie between 0 and 150%.

Results for \mathcal{S}^G vs. \mathcal{S}^{BH} , reported in Panel B1, indicate that the out-of-sample predictive power of G can generate sizable welfare bene its relevant for investors. For example, in the case of $\gamma=5$ with N=5, \mathcal{S}^G leads to certainty equivalent gains of 8.62% (4.05%) relative to \mathcal{S}^{BH} for the full (post-1984) sample. Campbell and Thompson (2008) show that the investor's welfare gain depends on the relative magnitude of predictive R^2 and the buy-and-hold Sharpe ratio. Since the R^2_{oos} values of G increases with the bond maturity and the Sharpe ratio decreases with the maturity, it is not surprising to indicate that the out-of-sample predictive power of G increases.

Results for \mathcal{S}^{G+Y} vs. \mathcal{S}^{Y} , reported in panel B2, show that the hypothesis H_0 is rejected at the 5% signi cance level in all but one case (with N=2 and $\gamma=5$). In other words, incorporating G into the out-of-sample forecasting of the bond risk premium can lead to signi cant utility gains relative to trading on \widetilde{PC}^{o}_{1-3} alone. Since these utility di erences have the units of expected annualized return, they can be roughly interpreted as the di erences in portfolio management fees. We note that a mean-variance investor with $\gamma=3$ is prepared to pay extra 43-113 bps per year to exploit the additional information as contained in factor G.

To summarize, Section 4 provides strong evidence against H_0^{S1} and H_0^{S2} . It also shows that

rejection of the these two hypothesis carries signi cant economic values.

4.4.4 Additional Evidence

We further examine the predictive power of the SAGLasso factor in Internet Appendix IA.B and summarize the main ndings here.

Given that \widehat{LN}^m is constructed using the same set of 131 macro series and includes all 131 series as well as squares and cubes of these macro variables, \widehat{LN}^m serves as a natural benchmark for \widehat{G} (a linear combination of 19 series and some of their lagged variables). We note that \widehat{G} shows stronger predictive ability than \widehat{LN}^m in both in-sample and out-of-sample analyses.

As mentioned before, the set of 131 macro series we use is adjusted for both data revisions and publication lags. One relevant question is the impact of these two adjustments on bond return predictability. We not that the return predictability evidence based on \widehat{G} is not sensitive to the vintage of macro data used. In contrast, publication lags pose much greater \danger" than data revisions in forecasting future bond returns based on macro variables, at least in our sample. This problem can be mitigated straightforwardly, however, since it is easier to make an adjustment for publication lags than to gure out preliminary macro data releases and adjust for data revisions.

To better understand the source of the predictive power of the SAGLasso factor (\widehat{G}_t) , we also examine properties of its three components: the employment (\widehat{g}_{1t}) , housing (\widehat{g}_{2t}) , and in ation (\widehat{g}_{3t}) factors. As expected, \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} all have low correlations with the yield curve factors; as a result, \widehat{G} is weakly correlated with $PC_{1-3,t}^o$ and hardly correlated with $PC_{4,t}^o$ and $PC_{5,t}^o$. The three group factors also show signicant predictive power, both individually and jointly. Following JPS, we also examine the relative importance of the three group factors across bond maturity. Our results indicate that relatively speaking, among the three group factors, \widehat{g}_{1t} is the most important, followed by \widehat{g}_{3t} , and then by \widehat{g}_{2t} , regardless of the bond maturity.

¹⁷Bianchi et al. (2021) consider more categories and $\,$ nd that variables related to the stock and labor market (the output & income and orders & inventories) are more important for the short-end (long-end) of the yield curve. Note that the aggregate bond market is used to train $\{\hat{g}_h\}$.

The SAGLasso algorithm is implemented using 131 macro variables along with six of their lags. One question that arises is: Are lags of macro variables are essential to the predictive power of the SAGLasso factor? If yes, what is the optimal number of lags to be included in our supervised learning? We repeat the baseline analysis using the 131 macro variables along with N_L of their lags, where $N_L = 0, 3, 9, 12$. We note that the evidence of the return predictability is robust to the use of no lags ($N_L = 0$). Nonetheless, our results suggest that the SAGLasso factor constructed using the 131 macro variables along with 3 or 6 of their lags has the best performance in both the in-sample and out-of-sample predictions. This inding rejects a trade-operation between including more information in the supervised learning and imposing a denser data structure to enhance the estimation stability. While the baseline SAGLasso factor (with $N_L = 6$) seems to capture more information on long-term bond premiums, the alternative SAGLasso factor with $N_L = 3$ outperforms for short-term bonds.

5 The SAGLasso factor and the Spanning Controversy

As an important application of the SAGLasso factor, we revisit the spanning controversy in this section. We focus on the three main aspects of the controversy. First, whether a macro factor's predictive power is robust to nite samples (see Section 2). Second, whether a macro factor is an unspanned pricing factor in an MTSM. Third, whether or not a macro factor's temporal variation can be captured by the yield curve. We show that the SAGLasso factor can address all three aspects of the controversy by using the dynamic term-structure modeling framework.

5.1 The Modeling Framework

Following JPS, we assume that all risks in the economy are encompassed by an \mathcal{N} -dimensional state vector $X_t = (\mathcal{P}_t, F_t)$, where \mathcal{P}_t denotes \mathcal{L} linear combinations of (noise-free) zero yields and the $(\mathcal{N}$ - \mathcal{L})-vector F_t represents macro factors as before. The short rate is an anne function of X_t :

$$r_t = \delta_0 + \delta_1^{\ell} X_t = \delta_0 + \delta_{1p}^{\ell} \mathcal{P}_t + \delta_{1f}^{\ell} F_t. \tag{6}$$

The dynamics of X_t under the risk-neutral measure $\mathbb Q$ are assumed to follow a Gaussian process:

$$X_{t} = \begin{bmatrix} \mathcal{P}_{t} \\ F_{t} \end{bmatrix} = \begin{bmatrix} \mu_{p}^{\bigcirc} \\ \mu_{f}^{\bigcirc} \end{bmatrix} + \begin{bmatrix} \bigcirc_{pp} & \bigcirc_{pf} \\ \bigcirc_{pp} & \bigcirc_{pf} \end{bmatrix} \begin{bmatrix} \mathcal{P}_{t-1} \\ F_{t-1} \end{bmatrix} + {}_{x} \epsilon_{x;t}^{\bigcirc}, \qquad \epsilon_{t}^{\bigcirc} \sim MVN(0, I).$$
 (7)

It follows from Du e and Kan (1996) that the yield of an m-period zero-coupon bond is

$$y_t^{(m)} = A_m + B_m^{\ell} X_t, \tag{8}$$

where the expressions for A_m and B_m are given in Internet Appendix IA.C.1. The market price of risk follows the \essentially a ne" structure of Du ee (2002):

$$t = \mu_X^{\mathsf{P}} - \mu_X^{\mathsf{Q}} + (^{\mathsf{P}} - ^{\mathsf{Q}})X_t = \lambda_0 + \lambda_1 X_t, \tag{9}$$

where $\{\mu^{\mathsf{P}}, \ ^{\mathsf{P}}\}$ are the P-measure counterparts of $\{\mu^{\mathsf{Q}}, \ ^{\mathsf{Q}}\}$.

5.2 Finite Sample Analysis

The statistical inference done in Section 4.4 is based on asymptotic distributions. We now examine H_0^{S1} and H_0^{S2} using a nite-sample analysis. This is necessary because, rst, our dependent variables involve overlapping observations by construction, and secondly, the rst and second PCs of yield curves are highly persistent in our sample, with rst-order autoregressive coe cients (ACF) of 0.99 and 0.94, respectively (while the ACF of the SAGLasso factor is only 0.82). Below we rst specify the underlying data-generating processes (DGPs) for H_0^{S1} and H_0^{S2} within the framework described in Section 5.1. We then construct nite-sample distributions of test statistics from return-forecasting regressions and conduct nite-sample inference based on such distributions.

5.2.1 Data-Generating Processes for Null Hypotheses

DGPs under H_0^{S1} or H_0^{S2} impose no restrictions on model parameters and allow them to be estimated freely. That is, as long as the $\mathcal{N} \times \mathcal{N}$ yield loading matrix $\mathcal{B} \equiv (B_{m_1}, \dots, B_{m_N})^{\ell}$ is invertible, the fraction of variations in term premia that are associated with macro factors is also attributable

to certain linear combinations of these yields. This type of MTSMs are referred to as spanned models and denoted by $SM(\mathcal{L}, \mathcal{N})$. If \mathcal{B} is not invertible, then the model is no longer spanned.

Given that $F_t = G_t$, the DGP for H_0^{S1} is model SM(2,3). To see why, suppose that yield PCs are defined in terms of k zero-coupon bonds with maturities $\mathcal{M} = \{m_1, \dots, m_k\}$ as follows:

$$PC_{1 \ N:t} = WY_t^{\mathcal{M}} \equiv W(\mathcal{A}_{\mathcal{M}} + \mathcal{B}_{\mathcal{M}}^{\emptyset}X_t), \quad W \in \mathbb{R}^{N \ N}.$$

Since SM(2,3) is a spanned model, rank $(\mathcal{B}_{\mathcal{M}}) = \mathcal{N} = 3$. The resultant invertibility of $W\mathcal{B}_{\mathcal{M}}^{\emptyset}$ implies

$$E_t\left(rx_{t;t+12}^{(12n)}\right) = \text{constant} + \psi_{12n;12}^{\ell}(W\mathcal{B}_{\mathcal{M}}^{\ell})^{-1}PC_{1-3;t}, \tag{10}$$

where $\psi_{m;12}=mB_m^{\emptyset}-(m-12)B_{m-12}^{\emptyset}(\ ^{\rm P})^{12}-12B_{12}$ for m>12. This result means that G_t has no incremental predictive power for annual excess returns in the presence of $PC_{1-3;t}$, consistent with H_0^{S1} . Similarly, the DGP for H_0^{S2} is model SM(4,5).

At the heart of Eq. (10) is the theoretical spanning of G_t by any three zero yields. In other words, as long as $k \geq \mathcal{N}$, the covariance matrix of $Y_t^{\mathcal{M}}$ (stacked bond yields) has a rank of 3. However, empirically the sample covariance matrices are nonsingular regardless of the choice of maturities \mathcal{M} . The standard interpretation in the literature is that observed yields (denoted $Y_t^{o\mathcal{M}}$) are contaminated by small transitory noise, modeled as idiosyncratic \measurement error" (representing a catch all term for model misspeci cation and other imperfections) as follows:

$$Y_t^{o\mathcal{M}} = \mathcal{A}_{\mathcal{M}} + \mathcal{B}_{\mathcal{M}}^{\emptyset} X_t + \eta_{Vt}, \quad \eta_{Vt} \sim MVN(0, \sigma^2 I). \tag{11}$$

The presence of η_{yt} is also important in terms of accommodating hidden yield factors in spanned models with $\mathcal{N}>3$. For instance, consider model SM(4,5), where $PC_{1-5;t}$ fully determine the term premia and absorb the role of G_t . If at least ve zero yields (or their linear combinations) are assumed to be measured without error, the full-rank $\mathcal{B}_{\mathcal{M}}^{g}$ indicates that the entire state vector can be perfectly extracted from the ve yields. Consequently, H_0^{S2} degenerates into a version of H_0^{S1} that involves more than three yield PCs. Alternatively, if measurement error is ubiquitous, it becomes directly extract higher-order PCs, say, $PC_{4;t}$, from the cross section of yields. As

such, Eq. (11) opens up the possibility that bond risk premia contain a component attributable to higher-order PCs, yet hidden from the observed yield curve | namely, a hidden factor.

5.2.2 Finite-Sample Inference

This subsection reports $\,$ nite-sample properties of test statistics under H_0^{S1} or H_0^{S2} , whose underlying DGPs are SM(2,3) and SM(4,5), respectively. We estimate these spanned models using the full-sample zero-coupon yields with maturities $\mathcal{M}=\{0.25,1,2,3,4,5\}$ to generate samples over the period 1964{2014, or using extended Fama-Bliss zero yield data with $\mathcal{M}=\{0.5,1,2,3,4,5,7,10\}$ to generate samples for the post-1984 period.

As the inference about H_0^{S2} requires all yields to be measured with errors, we implement the model estimation with maximum likelihood using the Kalman Iter. To facilitate the interpretation of the sources of risk compensation, we normalize yield-based state variables \mathcal{P}_t to the rst \mathcal{L} PCs of zero yields; namely, $X_t = (PC_1 \mid_{L/t}, G_t)$. This rotation also of errors of Salarting values in the estimation of P-dynamics of X_t . When estimating Q-measure parameters, we rotate X_t to X_t , a state vector that satisfies the canonical form of Joslin, Le, and Singleton (2013).

Under each spanning hypothesis, we generate 5,000 articial data sets from its underlying DGP estimated with the full or post-1984 sample. In the in-sample analysis, we obtain the distributions for two t-statistics (based on HH and NW standard errors, respectively) and R^2 . In the out-of-sample analysis we consider the ENC-REG and ENC-NEW tests and R^2_{oos} . We calculate the 5% critical value and p-value for each set of statistics, the latter being defined as the frequency of bootstrap replications in which the test statistics are at least as large as in the real data.

 $^{^{18}}$ In other words, instead of directly estimating parameters in Eqs. (6) and (7), we estimate another (and shorter) parameter vector $^{\mathbb{Q}}_{\mathcal{M}}$ (de ned in Internet Appendix IA.C.1) that encompasses all bond pricing information. 19 We do not consider the t-statistic based on the Hodrick (1992) standard errors here because it tends to under-reject

¹⁹We do not consider the t-statistic based on the Hodrick (1992) standard errors here because it tends to under-reject the null. Also, Ang and Bekaert (2007) show that it has desirable small-sample properties.

 $^{^{20}}$ In our baseline $\,$ nite-sample inference, there is no distinction between the in-sample factor \widehat{G}_t and the real-time factor \widetilde{G}_t . To make the out-of-sample inference truly out of sample, we perform full-scale simulations in which the time series of 131 individual macro variables are generated together with the $\mathcal{N-L}$ yield factors. In each trial, the SAGLasso estimator is implemented on the generated macro variables to construct macro factors \widehat{G}_t and \widetilde{G}_t . These re-simulated

Panel A of Table 3 reports nite-sample properties of test statistics for the full sample. Note from panels A1 (in-sample) and A2 (out-of-sample) that small-sample distortions appear more severe under H_0^{S1} . For in-sample t-statistics, the \true" 5% critical value ranges from 3.46 to 4.47, depending on the bond maturity and standard errors used; for \mathbb{R}^2 (the incremental in-sample \mathbb{R}^2 due to G_t), the 95th percentile of its small-sample distribution is higher than 9%. However, all of these critical values are substantially lower than actual statistics obtained from our data sample. Similarly, note from panel A2 that there is strong evidence against H_0^{S1} . In particular, all statistics have bootstrapped p-values less than 1%. Also, the critical value of R_{oos}^2 ranges from 11.7% for the 5-year bond to 13.6% for the 2-year bond. Results reported in panels A3 (in-sample) and A4 (out-of-sample) of Table 3 illustrate that under H_0^{S2} , small-sample distributions of test statistics show even greater deviations from their asymptotic distributions. For instance, the critical value for the HH t-statistics under H_0^{S2} (panel A3) is at least 0.8 higher than its counterpart under H_0^{S1} (panel A1), with the biggest di erence of 1.29 (= 4.75 – 3.46) for the 5-year bond. For out-of-sample tests, the ENC-REG critical value is 4.02~4.36, and the ENC-NEW critical value can be as high as 52.18 in small samples (panel A4), but the critical values are still not large enough to overturn the asymptotic analysis-based rejection of H_0^{S2} concluded in Section 4.4.2.

We nd similar results for the post-1984 sample (panel B of Table 3), although statistics estimated from the subsample are subject to less severe distortions than those from the full sample. Particularly, the asymptotic analysis-based evidence against H_0^{S1} and H_0^{S2} post 1984 (panel B of Table 2) is robust to small samples.

Overall, we draw three conclusions from Table 3. First, small-sample bias tends to decrease with the bond maturity. Second, the asymptotic analysis-based evidence against H_0^{S1} and H_0^{S2} (Table 2 and also Internet Appendix IA.B) is too strong to be overturned. Third, results on descriptive statistics show that none of the 5,000 articleal samples are able to generate a R^2 or R_{oos}^2 that exceeds the actual incremental R^2 .

We present more robustness analyses in the Internet Appendix. Section IA.D shows that model SM(2,3) provides a more robust test of H_0^{S1} than does the DGP proposed in BH. Section IA.E conducts the Ibragimov and Meller (2010) test of H_0^{S1} and H_0^{S2} that is robust to heteroscedasticity, autocorrelation, and structural breaks, and nds that among the ve yield factors and the SAGLasso factor, the latter is the only robust bond return predictor. Finally, Section IA.F examines an alternative version of H_0^{S2} where the conditioning variable Z_t is the \cycle" factor of Cieslak and Povala (2015) given that this factor is spanned. We nd that this hypothesis is rejected as well.

To summarize, the results from our nite-sample analysis strongly reject the two spanning hypotheses, suggesting that it is very unlikely for a spanned MTSM to account for the additional predictive power of the SAGLasso factor as observed in our sample.

5.3 Testing the Macro-Unspanning Hypothesis

The rejection of the spanning hypotheses with $F_t = \widehat{G}_t$ implies that MTSMs incorporating \widehat{G}_t may be preferable to \yields-only" term structure models (YTSMs), say, for term premium inference. Then a follow-up question is: Should \widehat{G}_t be used as a bond-pricing factor in an MTSM and if yes, is \widehat{G}_t a spanned pricing factor? We address this question by formulating and testing the \macro-unspanning hypothesis" (MUH), which intuitively says that in spite of its predictive power for bond risk premia, \widehat{G}_t is not a spanned pricing factor.

5.3.1 The Macro-Unspanning Hypothesis

In the MTSM framework described in Section 5.1, the MUH (arising from the conditions specified in JPS and BR for unspanned macro risks) can be stated as follows:

$$H_0^{US}: \quad \delta_{1f} = 0 \quad \text{ and } \quad {}_{pf}^{\mathbb{Q}} = 0.$$
 (12)

Under these restrictions, the short rate depends only on \mathcal{P}_t (\mathcal{L} linear combinations of zero yields), and the Q-dynamics of F_t as represented by $\{\mu_f^{\mathbb{Q}}, \ \ _{fp}^{\mathbb{Q}}, \ \ _{ff}^{\mathbb{Q}}\}$ are not identiable without information from other asset markets. It follows that only risks of yield PCs are priced in the Treasury market.

Namely, the one-period risk premium, t, given below, is \mathcal{L} -dimensional:

$$_{t}=\mu_{p}^{P}-\mu_{p}^{Q}+\left[\begin{array}{cc}P\\pp-&pp\end{array},\begin{array}{cc}Q\\pf\end{array}\right]X_{t}=\lambda_{0}+\lambda_{1}X_{t}.\tag{13}$$

For convenience, such an \mathcal{N} -factor MTSM that satis es H_0^{US} is termed an unspanned model and denoted $USM(\mathcal{L}, \mathcal{N})$.

Note that when $\mathcal{L}=3$, H_0^{US} represents the standard version of the MUH: Macro-based forecasts are not spanned by the contemporaneous yield curve (equivalent to the case focused on in BR's likelihood-ratio tests). When $\mathcal{L}>3$, H_0^{US} denotes a more general version that the predictive ability of macro factors is not spanned by the Itration generated by the yield dynamics. We examine both versions and thereby estimate both models $SM(\mathcal{L},\mathcal{N})$ and $USM(\mathcal{L},\mathcal{N})$ with $\mathcal{L}=3,4,5$ in this analysis. To match the data sample used in JPS and BR, we estimate each of these six models using zero yields with $\mathcal{M}=\{0.5,1,2,3,4,5,7,10\}$ over the period 1985{2007.

Note also that H_0^{US} is *not* simply the opposite of H_0^{S1} or H_0^{S2} . First, while H_0^{US} concerns whether a given macro factor with some explanatory power for term premia is a pricing factor, H_0^{S1} and H_0^{S2} focus on whether variables outside of the bond market provide additional explanatory power for bond risk premia. Second, term structure modeling implications from the outcome of testing H_0^{S1} or H_0^{S2} are different from those of testing H_0^{US} . For instance, suppose $\mathcal{N}=5$. Rejecting H_0^{US} implies a rejection of model USM(4,5), where the alternative model is SM(4,5); namely, it is SM(4,5) versus USM(4,5). In contrast, rejecting H_0^{S2} implies that USM(5,6) ought to be used to infer the risk premium component in long-term yields, and accepting H_0^{S2} means that SM(4,5) (or YTSM(5)) should be used; that is, it is SM(4,5) versus USM(5,6).

As a result, a test of H_0^{US} corresponds to a test of equal forecast accuracy for non-nested models in the regression setting in Eq. (1). Suppose that $Z_t = PC_1$ $_{5;t}$ and $F_t = G_t$. The question of interest is whether the additional predictive power of G_t is captured by the six yield factors (i.e., PC_1 $_{6;t}$) or any other six linear combinations of \true" yields, similar to an encompassing test for comparing non-nested models: $(PC_1$ $_{5;t}, G_t)$ versus PC_1 $_{6;t}$.

5.3.2 Statistical Tests of the Macro-Unspanning Hypothesis

We conduct two tests of H_0^{US} . One is a model-based likelihood ratio (LR) test. As there is no analytic expression available for the limiting distribution under H_0^{US} , we compute the critical values of the test statistic based on the approximation method used by BR. However, the approximation is done conservatively, and as a result, this LR test tends to under-reject H_0^{US} . To circumvent this problem and make a more robust inference, we perform another test of H_0^{US} (a model-free test in the spirit of BR) by directly testing the yield loadings on the SAGLasso factor without imposing no-arbitrage restrictions. Given the assumption that all yields are observed with measurement error, we can focus on the loading matrix $\mathcal{B}_{\mathcal{M}}^{\emptyset} = (\mathcal{B}_{\mathcal{L};p}^{\emptyset}, \mathcal{B}_{\mathcal{L};f}^{\emptyset})$ in Eq. (11) in this model-free test. To implement the test, we rst estimate Eq. (11) with the OLS and then conduct LR tests of $\mathcal{B}_{\mathcal{L};f} = 0$.

Panel A of Table 4 reports the results from both the model-based (column 2) and model-free (column 3) tests of H_0^{US} , for $\mathcal{L} = \mathcal{N} - 1 = 3, 4, 5$. Note from column 2 that the LR statistics are always smaller than the 10% critical values, $\forall \mathcal{L}$. An unreported decomposition of the log-likelihood function reveals that the di-erence between $SM(\mathcal{L},\mathcal{N})$ and $USM(\mathcal{L},\mathcal{N})$ mainly derives from the Q-likelihood. This result, as documented by BR for $\mathcal{L} = 3$ with two macro factors, is not surprising as the restrictions in H_0^{US} are not placed on the P-dynamics of $USM(\mathcal{L},\mathcal{N})$. However, our test results show that the improved yield curve—tting of $SM(\mathcal{L},\mathcal{N})$ over $USM(\mathcal{L},\mathcal{N})$ is statistically insignicant, in contrast to BR's—nding. The p-values reported in column 3 indicate that H_0^{US} is not rejected by the model-free test either at the conventional signicance level of 5%, $\forall \mathcal{L}$.

Results in panel A also suggest that the negative e ect of excluding \widehat{G} from thing the yield curve becomes weaker when $\mathcal N$ increases. This inding is not surprising: Although the higher-order PCs are considered to be unimportant in explaining cross-sectional variations in yields, they help the term structure more or less. Thus, when an additional yield factor is included in the model,

²²As discussed in BR, while H_0^{US} imposes four zero restrictions for the case of $\mathcal{L}=3$, a comparison of test statistics with the critical values of a $\chi^2(4)$ -distribution would be misleading. Under the approximation adopted by BR (detailed in their Section 3.1), test statistics are evaluated against a χ^2 -distribution with $(k-\mathcal{N})(\mathcal{N}+1)-1$ degrees of freedom when only one macro variable is used, where k is the number of bonds involved.

the already limited role of G_t in the cross section becomes more redundant.

To summarize, when the SAGLasso factor is used as the sole macro factor of an unspanned model, both the model-based and model-free tests fail to reject the MUH. As mentioned before, the main reason for this inding is that in spite of its strong predictive power for excess bond returns, the SAGLasso variable is weakly correlated with yield PCs and is unspanned (see Section 5.4). See Internet Appendix IA.G for more applications of unspanned models.

5.4 Is the SAGLasso Factor Unspanned?

To examine whether the yield curve can explain the temporal variation in the SAGLasso factor, we follow JPS and regress G_t on \mathcal{N} observed yield PCs:

$$G_t = \gamma_0 + \gamma_1 P C_1^o N_{:t} + \varepsilon_t. \tag{14}$$

To see whether the regression R^2 is low enough to invalidate spanned models, we follow BR and evaluate it against its distribution implied from an \mathcal{N} -factor spanned model rather than against unity. To this end, we consider distributions implied by \unconstrained" models as well as \constrained" ones, and also allow for macro measurement error, denoted by η_f with a standard deviation of σ_f . In contrast, BR focus on unconstrained models with zero η_f . Unconstrained models here refer to MTSMs imposing no constraints on the Sharpe ratio (SR) of bond returns. Such models may imply unrealistic SRs, as noted in Du ee (2010) and Joslin, Singleton, and Zhu (2011). MTSMs with the selected zero restrictions on $\{\lambda_0, \lambda_1\}$ are referred to as constrained models and denoted $CSM(\mathcal{L}, \mathcal{N})$ for spanned models and $CUSM(\mathcal{L}, \mathcal{N})$ for unspanned models, with \mathcal{L} being the number of yield factors included in the model (see Internet Appendices IA.C and IA.G).

Panel B of Table 4 reports the empirical R^2 value and its 95% con-dence interval (in brackets underneath) in column 5, where the interval is based on 5,000 data sets simulated from constrained model $CSM(\mathcal{N}\text{-}1,\mathcal{N})$, estimated with and without macro measurement errors, for $\mathcal{N}=4,5,6$. First, consider the case without macro measurement errors ($\eta_f=0$), a commonly made assumption in

the macro nance literature (see, e.g., JPS and BR). The results show that $\forall \mathcal{N}$, the empirical R^2 is around 14.5% and outside of its 95% con-dence interval with a p-value (de-ned as the fraction of the simulated samples in which the R^2 is below the value in the actual data) lower than 2.5%. That is, the SAGLasso factor indeed has R^2 values too low to be reconcilable with spanned models. We also evaluate empirical R^2 s against their distributions implied from unconstrained models $SM(\cdot)$ and not that the results are similar to those reported in panel B. Since we assume in our model estimation that bond yields are all measured with error, the aforementioned results provide evidence that yield measurement error does not account for the large proportion of unspanned macro variation as observed in the real data in our sample.²³

Next, we assume that $\eta_f \neq 0$. Intuitively, allowing for macro measurement errors would create a further unspanned variation of G_t and thus make it more likely for spanned models to reproduce documented regression evidence. We re-estimate model $CSM(\mathcal{N}\text{-}1,\mathcal{N})$ assuming $\eta_f \neq 0$ and not that the resulting implied R^2 distributions are barely distinguishable from their counterparts with zero η_f . For example, the 95% con-dence intervals implied from model CSM(3,4) with and without macro measurement error are [0.587,0.769] and [0.593,0.847], respectively (column 5 of Table 4). As a result, even if including η_f shifts the model-implied R^2 distribution to the left, the net impact is minimal; that is, unspanned macro variation observed in our sample cannot be attributed to macro measurement errors either. Behind this inding is the tiny standard deviation of the measurement error in G_t : $G_t = 0$ and G_t is standardized under the SAGLasso procedures (Section 4.2), G_t is negligible compared to the total standard deviation of G_t .

Panel B of Table 4 also includes the results from a spanning test applicable to macro factors allowed to contain \noise" (Du ee 2013a): if yields span the true state vector, the regression

²³BR consider regressions similar to Eq. (14) albeit with *GRO* or *INF* as the dependent variable; their simulation results, based on unconstrained models, indicate that adding small yield measurement error makes spanned models capable of generating the appearance of unspanned macro information in the real data. In an untabulated analysis we show that the main reason for such simulation results is, however, that when a macro variable with a low correlation to the yield curve is used as a spanned factor, most variation in this macro factor is captured by high-order yield factors *by construction*; as a result, a spanned model with small yield measurement error can reproduce a large amount of unspanned macro variation even if the macro variable under consideration is unspanned.

in Eq. (14) should produce serially uncorrelated residuals even though the estimated R^2 could substantially deviate from one. The estimated rst-order correlation of residuals of the regression is around 0.67, $4 \le \mathcal{N} \le 6$ (column 6). Given that the serial correlation of G_t is 0.71, the above result suggests that whatever the regression is missing cannot be explained by white-noise shocks.

Overall, the results of Section 5.4 provide strong evidence that much of the variation in G_t is not captured by the yield curve. This unspanned nature of the SAGLasso factor reinforces our earlier conclusion that it carries term premium information independent of the yield curve. Moreover, this macro variable has very small measurement error even when it is included as a spanned factor in a low-dimensional MTSM.

6 Conclusion

There is no consensus in the literature on whether or not macro variables have incremental predictive power for future excess bond returns over contemporaneous bond yields. However, macro variables considered in the empirical literature are typically standard ones, such as measures of real growth and in ation. These variables either show little unconditional predictive power for bond risk premia or are highly correlated with contemporaneous yields and thus have insignicant conditional predictive power. In this study we construct a new macro variable using Supervised Adaptive Group LASSO (SAGLasso), a machine learning algorithm, from a panel of 917 macro variables (131 macro series along with six of their lags) that are adjusted for both data revisions and publication lags. We show that this new macro variable, termed the SAGLasso (macro) factor, has strong out-of-sample predictive power for bond risk premia conditional on the yield curve. Additionally, this predictability can provide investors with signicant economic gains.

Importantly, the SAGLasso factor is parsimonious, intuitive, and easy to interpret. Speci cally, it is a *linear* combination of merely 30 selected variables out of 917, and consists of a novel housing factor, an employment factor, and an in ation factor. In addition, in spite of its strong predictive

power, the SAGLasso factor has low correlations with contemporaneous yields by construction; thus, it is a \pure" macro-based bond return predictor.

The SAGLasso macro factor also provides a potential resolution to the spanning controversy in the macro- nance literature. First, the SAGLasso factor is not spanned by contemporaneous yields. Second, in an MTSM with the SAGLasso factor as its sole macro factor, the hypothesis that it is unspanned by the yield factors is not rejected. Third, incorporating the unspanned SAGLasso factor into an MTSM with realistic Sharpe ratios has nontrivial economic bene ts. Fourth, the importance of the SAGLasso factor cannot be attributed to measurement errors in yields or itself. Furthermore, its measurement error is small.

To summarize, using a machine learning algorithm we are able to construct a new, parsimonious, and easy-to-interpret macro variable with strong and robust predictive power for bond risk premia. In addition, this new macro factor can potentially help resolve the spanning controversy in the macro nance literature. We use the algorithm to construct macro-based bond return predictors in this study but SAGLasso should also be useful in similar big data applications in nance and economics. For instance, we may construct a real-time expectation factor using the SAGLasso algorithm and examine if the implied bond risk premia are consistent with those demanded by investors in history (Piazzesi et al. 2015). This would allow us to explore an alternative explanation for the spanning controversy: It is due to the discrepancy between the short-rate expectation of real-time investors and the ex post estimates of an econometrician (Cieslak 2018). We may also expand the macro panel data to incorporate survey forecasts of macro variables, which are shown to provide additional information in term structure modeling (see, e.g., Chernov and Mueller 2012 and Kim and Orphanides 2012). We leave these questions to future research.

²⁴In an earlier version of this paper, Huang and Shi (2010) provide evidence consistent with the potential mechanism suggested by Du ee (2011). As noted in Cieslak (2018), these di erent explanations of the spanning controversy are not, however, mutually exclusive because its resolution \depends on the particular variables that the econometrician assumes a part of his/her information set" (p. 3269).

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A Notation and Frequently Used Terms

Spanning hypothesis I (H_0^{S1})	Macro variables have no additional predictive power for excess bond returns over the rst three principal components (PCs) of the observed yield curve
Spanning hypothesis II (H_0^{S2})	Macro variables have no additional predictive power for excess bond returns over the rst ve PCs of the noise-uncontaminated yield curve
Macro-unspanning hypothesis (H_0^{US})	So-called knife-edge restrictions given in Eq. (12) in the paper for a macro- nance term-structure model (MTSM) to be unspanned
\widehat{CG}	the convergence gap de ned by Berardi et al. (2021)
\widehat{CP}	the Cochrane and Piazzesi (2005) forward rate factor
\widehat{G}	the (unconditional) the Supervised Adaptive Group LASSO (SA-GLasso) macro factor constructed in this study
\widetilde{G}	the recursive SAGLasso macro factor constructed in this study
\widehat{g}_1 , \widehat{g}_2 , and \widehat{g}_3	(unconditional) SAGLasso group factors constructed in this study, representing \employment," \housing," and \in ation," respectively
\widetilde{g}_1 , \widetilde{g}_2 , and \widetilde{g}_3	recursively constructed \widehat{g}_1 , \widehat{g}_2 , and \widehat{g}_3
\widehat{H}	the hidden factor proposed by Du ee (2011)
\widehat{LN}^m	a modi ed Ludvigson and Ng (2009) macro-based return predictor
$PC_{1-3}^{o} = (PC_{1}^{o}, PC_{2}^{o}, PC_{3}^{o})$ \widetilde{PC}_{1-3}^{o} $PC_{1-5} = (PC_{1}, \dots, PC_{5})$	vector of the rst three PCs of the <i>observed</i> yield curve
PC_{1-3}	recursively constructed PC_{1-3}^o vector of the rst ve PCs of the <i>noise-uncontaminated</i> yield curve
$\overrightarrow{PC}_{1-5} = (\overrightarrow{PC}_1, \dots, \overrightarrow{PC}_5)$ \widetilde{PC}_{1-5}	recursively constructed PC_{1-5}
$\mathcal{CSM}(\mathcal{L},\mathcal{N})$	An \mathcal{N} -factor constrained, spanned MTSM Model $SM(\mathcal{L},\mathcal{N})$ with restrictions on the model-implied Sharpe ratios of bond returns
$\mathit{CUSM}(\mathcal{L},\mathcal{N})$	An \mathcal{N} -factor constrained, unspanned MTSM Model $USM(\mathcal{L}, \mathcal{N})$ with restrictions on the model-implied Sharpe ratios of bond returns
$SM(\mathcal{L},\mathcal{N})$	An $\mathcal N$ -factor spanned model an $\mathcal N$ -factor MTSM with $\mathcal L$ ($\mathcal N$ – 1)
	yield factors and one macro factor (the SAGLasso factor G) that does not satisfy the macro-unspanning hypothesis ${\cal H}_0^{US}$
$\mathit{USM}(\mathcal{L},\mathcal{N})$	An \mathcal{N} -factor spanned model an \mathcal{N} -factor MTSM with \mathcal{L} ($\mathcal{N}-1$) yield factors and one macro factor (the SAGLasso factor G) that satis es H_0^{US}
$YTSM(\mathcal{N})$	An ${\cal N}$ -factor \yields-only" term-structure model

B Macroeconomic Series Used in the Analysis

Two sets of 131 macroeconomic series are used in our empirical analysis. The rst, the standard one used in the literature, includes revised macroeconomic data. The second set consists of real-time macroeconomic data only | the macro series adjusted for data revisions and publication lags.

Table A.1 lists the 131 macroeconomic series and contains the full name (column 4) of each series, along with its series number (column 1), group number (column 2), mnemonic | the series label used in the source database (column 3), short name (column 5), and data transformation ag (column 6). The transformation ag = 1: no transformation applied to the series; ag = 2: the rst di erence applied; ag = 3: the second di erence; ag = 4: the logarithm; ag = 5: the rst di erence of logarithm; and ag = 6: the second di erence of logarithm.²⁵

We compile our macro data in three steps. First, we match the panel of 131 series with ALFRED and nd that 70 of them are included in the latter. For each of the 70 matched series, we collect its latest *nine* real-time observations at the end of each month (we do this because some macro variables need to be transformed to their second-order log-di erences). However, vintage versions of these 70 series are not balanced and go back to 1964 for only 25 series. Nonetheless, only 3 out of the 19 macro variables eventually selected by SAGLasso do *not* have their vintage data available going back to January 1985. Therefore, the look-forward biases should have a minimum impact, at least on our results obtained from the post-1984 sample.

Second, for the 45 incomplete series in ALFRED, we II in their misseriessationsdata vir 196{2.00rproaiuded(b)28(y)-25(Ludvigsion)-764(and)-25(Ngd)-25((*0114))-25((and)-25((our)-25(maen)27(ualufe) notincludedis ALFRED, these variables are resmiables notincluded to revisiom.

the integer number of months in the time interval between the end of the period over which it is measured and its release date. As shown later, such adjustments matter in our predictability analysis.

Finally, we investigate the time-series properties of these 131 series and determine transformations needed to stationarize each of these series. Table A.1 provides a complete list of the 131 series and, for each series, its data transforms applied, its publication lag, and the availability of its vintage data.

Column 7 labeled $\backslash \widehat{G}_t$ " of Table A.1 shows the values of a ag indicating which of the 131 macroeconomic series has a nonzero coe cient for its contemporaneous and/or lagged values (up to 6) in the SAGLasso regression. The ag value of \0" corresponds to the contemporaneous variable, and the value of ℓ denotes lag ℓ (in months), $\ell = 1, ..., 6$. For instance, macro series #41 (CES048) in group 2 | which measures the employment situation in the industry sector \Trade, Transportation and Utilities" | is selected by the SAGLasso approach and has 2 variables (out of 7), the lag-5 and lag-6 values of the series, included in the SAGLasso macro factor \widehat{G} . In total, 19 out of the 131 series (30 out of the 917 macro variables) enter the \widehat{G} factor. Column 9 labeled \Lag" reports each series' publication lag (in months), which is de ned as the time between the end of the period over which the series is measured and its rst release date. Note that out of the 131 series, the four in group 8 \stock market" (#81 through #84) are the only ones without a publication delay. The last column, labeled \vintage," indicates which macro series has vintage data available, where an asterisk denotes those series whose real-time series are available and used in our empirical analysis. Note that out of the 19 series included in the \widehat{G} factor and two additional series (#42 and #53) included in G (the out-of-sample version of \widehat{G}), the three commodity price indices (#111 through #113) are the only series that have no vintage data available in the ALFRED database. However, given the nature of these three series, they should not be subject to revision.

C Supervised Adaptive Group Lasso Method

We rst brie y review the group lasso (Yuan and Lin 2006). We begin with the following model:

$$Y = X\beta^0 + e, (15)$$

where e is assumed to be a T-dimensional vector of *i.i.d.* errors (we will relax this assumption later). The main assumption of the Group Lasso is that some subvectors of the true coe cients β^0 are zero. We denote by $h \in \mathcal{H}_1 = \{h : \beta^0_h \neq 0\}$ the unknown index set of non-zero subvectors of

 β^{0} . Hence, the Group Lasso involves identifying \mathcal{H}_{1} and estimating β^{0} .

The method is usually implemented by estimating the following restrictive form:

$$\min_{2\mathbb{R}^N} \left\{ \|\mathbf{y} - \mathbf{X}\boldsymbol{\beta}\|^2 + \lambda \sum_{h} \|\beta_h\| \right\}. \tag{16}$$

Note that expression (16) reduces to the Lasso when $|\mathcal{H}| = N$ and each h corresponds to the one-dimensional subspace of \mathbb{R}^T spanned by the corresponding column of the design matrix \mathbf{X} . In our implementation, we consider the general Group Lasso and more specifically, the adaptive group lasso, as follows:

$$\min_{2\mathbb{R}^N} \left\{ \|\mathbf{y} - \mathbf{X}\boldsymbol{\beta}\|^2 + \lambda \sum_{h} w_h \|\boldsymbol{\beta}_h\| \right\}. \tag{17}$$

Next, we describe the Supervised Adaptive Group Lasso (SAGLasso) algorithm proposed in Section 4.1. The method consists of two steps.

Step I: For cluster $h \in \mathcal{H}$, compute $\hat{\beta}^h$ | the cluster-wise Adaptive Lasso estimate of β^h , namely,

$$\hat{\beta}^{h} = \underset{h}{\operatorname{argmin}} \left\{ \|\mathbf{arx} - \mathbf{X}_{h} \beta^{h}\|^{2} + \sum_{j} \lambda_{h} * \hat{w}_{hj} |\beta_{j}^{h}| \right\}, \tag{18}$$

where \mathbf{arx} is a vector of average excess bond returns across maturity and \hat{w}_{hj} the j-th component of $\mathbf{\hat{w}}_{h}$, the vector of the (adaptive) weights. Zou (2006) recommends using $\hat{\beta}^{OLS}$ to construct $\mathbf{\hat{w}}_{h}$. As collinearity is a concern in our case, we set $\mathbf{\hat{w}}_{h} = 1/|\hat{\beta}_{h}^{RID}|^{-h}$, where $\hat{\beta}_{h}^{RID}$ is the best ridge regression t of \mathbf{arx} on \mathbf{X}_{h} . That is, for cluster h we only use macroeconomic variables within that cluster to construct predictive models. The optimal pairs of $(\gamma_{h}, \lambda_{h})$ are determined using ve-dimensional cross-validations. It is worth noting that tuning parameters λ_{h} are selected for each cluster separately in order to have di erent degrees of regularization for di erent clusters. This exibility allows us to uncover subtle structures that otherwise will be missed when applying the (adaptive) lasso method to all the series/clusters at the same time.

Note that for each cluster $h \in \mathcal{H}$, the adaptive lasso $\hat{\beta}^h$ has only a small number of nonzero components. Let $\beta^h = \hat{\beta}^h \setminus \mathbf{0}$, the vector of nonzero estimated components of $\hat{\beta}^h$ given by the cluster-wise model (18), and denote the corresponding part of \mathbf{X}_h by X_h . In our case, a typical cluster size $(\dim(\mathbf{X}_h))$ of 80 variables may reduce to a $\dim(X_h)$ of 8 \sim 10. Namely, the number of macro variables selected in Step I is signicantly smaller than the original number to begin with.

Step II: Construct the joint predictive model under the Group Lasso constraint as follows:

$$\hat{\beta} = \operatorname{argmin} \left\{ \|\operatorname{arx} - \mathbf{X}\beta\|^2 + \lambda \sum_{h2H} w_h \|\beta_h\| \right\}, \tag{19}$$

where X is formed by concatenating the design matrices X_h . The parameter λ is also chosen by ve-fold cross-validation. With $\lambda \to \infty$, estimates of some components of β_h s can be exactly zero. Following Yuan and Lin (2006), we obtain the solution in Eq. (19) e-ciently by using the modil ed least angle regression selection algorithm of Efron et al. (2004).

In out-of-sample tests conducted in our analysis, tuning parameters $\{\lambda_h, \lambda\}$ are selected recursively starting from the beginning of the test period using cross-validation as well as information only available at the time of estimation. However, to reduce the bias due to the limited training sample size, we use ten-fold cross-validation for the rst ve years of the out-of-sample testing period (e.g., the period 1985{1989 for the full sample). After that we go back to standard ve-fold cross-validation to restore the balance between bias and variance. Also, to reduce the computational burden in the nite-sample analysis (Section 5.2.2), we select $\{\lambda_h, \lambda\}$ once for each quarter rather than for each month; that is, $\{\lambda_h, \lambda\}$ selected in January are also used to perform SAGLasso model selection in February and March, until they are reselected in April.

Note that the SAGLasso algorithm di ers from the supervised principal component analysis (SPCA) | another two-step supervised learning approach | proposed by Bair et al. (2006) in a biological setting, which has been applied to in ation forecasts in Bai and Ng (2008).²⁷ For instance, the former takes into account the underlying cluster structure of candidate variables, whereas the SPCA does not consider all the candidates simultaneously. Also, variables selected in the SPCA are the PCs whose economic interpretations may not be obvious even though they may have satisfactory prediction performance. Factors constructed using SAGLasso, however, are easier to interpret.

Group Lasso is also applied by Freyberger et al. (2020) to identify rm characteristics in shaping expected equity returns. In their analysis, each group consists of 20 portfolios associated with (a polynomial function of) one characteristic, and model selection is done at the group level only. In our analysis, each group consists of macro variables supposed to capture the same economic concept, and Adaptive Lasso is used within each group (before model selection at the group level) to further mitigate the curse of dimensionality and boost the out-of-sample performance.

²⁷Gibson and Pritsker (2000) use partial least squares to choose risk factors of xed-income portfolios. Goto and Xu (2015) apply the graphical lasso to portfolio selection.

Table A.1: Macro Data Description

Series No.	Group		Mnemonic Description	Short Name	tran	φ t	Lag	Lag Vintage
-	-	a0m052	Personal income (AR, bil. chain 2000 \$)	Ы	2		_	*
2	-	A0M051	Personal income less transfer payments (AR, bil. chain 2000 \$)	PI less transfers	2		_	*
e	4	A0M224R	Real Consumption (AC) A0m224/gmdc	Consumption	2		_	*
4	4	A0M057	Manufacturing and trade sales (mil. Chain 1996 \$)	M & T sales	2		_	
2	4	A0M059	Sales of retail stores (mil. Chain 2000 \$)	Retail sales	2		_	
9	-	IPS10	INDUSTRIAL PRODUCTION INDEX - TOTAL INDEX	IP: total	2		_	*
7	-	IPS11	INDUSTRIAL PRODUCTION INDEX - PRODUCTS, TOTAL	IP: products	2		_	*
8	-	IPS299	INDUSTRIAL PRODUCTION INDEX - FINAL PRODUCTS	IP: nal prod	2		_	*
6	-	IPS12	INDUSTRIAL PRODUCTION INDEX - CONSUMER GOODS	IP: cons gds	2		_	*
10	-	IPS13	INDUSTRIAL PRODUCTION INDEX - DURABLE CONSUMER GOODS	IP: cons dble	2		_	*
17	-	IPS18	INDUSTRIAL PRODUCTION INDEX - NONDURABLE CONSUMER GOODS	iIP:cons nondble	2		_	*
12	-	IPS25	INDUSTRIAL PRODUCTION INDEX - BUSINESS EQUIPMENT	IP:bus eqpt	2		_	*
13	-	IPS32	INDUSTRIAL PRODUCTION INDEX - MATERIALS	IP: matls	2		_	*
14	-	IPS34	INDUSTRIAL PRODUCTION INDEX - DURABLE GOODS MATERIALS	IP: dble mats	2		_	*
15	-	IPS38	INDUSTRIAL PRODUCTION INDEX - NONDURABLE GOODS MATERIALS	IP:nondble mats	2		_	*
16	-	IPS43	INDUSTRIAL PRODUCTION INDEX - MANUFACTURING (SIC)	IP: mfg	2		_	*
17	-	IPS307	INDUSTRIAL PRODUCTION INDEX - RESIDENTIAL UTILITIES	IP: res util	2		_	*
18	-	IPS306	INDUSTRIAL PRODUCTION INDEX - FUELS	IP: fuels	2		_	*
19	-	PMP	NAPM PRODUCTION INDEX (PERCENT)	NAPM prodn	_		_	
20	-	A0m082		-				

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FCLIBNO		5 FM	1RNBA	DEPOSITORY INST RESERVES:NONBORROWED, ADJ RES REQ CHGS(MIL\$, SA)	Reserves nonbor	9		-	
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FYPE TYPE			O X C	S. D'S COMPOSITE COMMON STOCK: DIVIDEND VIELD (% DED ANNIMA)	Cleix Vic O's	c		_	
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FYGT15 INTEREST RATE L. U.S. TREASURY CONST MAUDRITIES 1-YR (% PER ANN.NSA) 19, T-bond			GM6	INTEREST RATE: U.S.TREASURY BILLS, SEC MKT, 6-MO.(% PER ANN, NSA)	6 mo T-bill	2		_	
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Table 1: Unconditional and Conditional Predictive Power of the SAGLasso Macro Factor

(columns 5-8); the Cochrane and Piazzesi (2005) forward-rate factor $\widehat{CP}_{\mathfrak{t}}$ (columns 9-12); the hidden component $\widehat{H}_{\mathfrak{t}}$ in the one-dimensional term premium factor as constructed in Du ee (2011) (columns 13-16); and the Convergence Gap \widehat{CG}_t as de ned in Berardi et al. (2021) (columns 17-20). Test statistics are computed using the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses), or the Newey and West (1987) HAC covariance estimator (in brackets). Bond The return to an n-year zero-coupon bond from month t to month t + 12 less the month-t yield on a one-year bond is regressed on the SAGLasso macro factor \widehat{G}_t alone (columns 1-4) or \widehat{G}_t and another return predictor together. The latter predictor considered includes the modi $\,$ ed Ludvigson and Ng (2011) factor $\widehat{LN}_t^{(1)}$ maturity n equals 2, 3, 4, and 5 for the full sample spanning the period January 1964 (December 2014 (Panel A), and equals 2, 5, 7, and 10 for the post-1984 sample period January 1985 (December 2014 (Panel B).

	(1)	(2)	(3)	(4)	(5)	(9)	(7)	(8)	(6)	(10)	(11)	(12)	(13)	(14)	(15)	(16)	(11)	(18)	(19)	(20)
									Panel A:	Panel A: Full sample, 1964{2014	ole, 1964{.	2014								
maturity n (year)	2	ъ	4	2	2	3	4	2	2	3	4	2	2	8	4	2	2	3	4	5
Ģ	1:047	1:982 (6:431)	2:810 (6:753)	3:498 (7:003)	0:924 (4:704)	1:671 (4:960)	2:301 (4:980)	2:807 (5:013)	0:889	1:677 (5:737)	2:314 (6:276)	2:929 (6:466)	1:038 (6:679)	1:962 (7:715)	2:783 (7:840)	3:471 (7:825)	0:924 (4:652)	1:836 (5:044)	2:667	3:368 (5:557)
E T NG	[6:427]		[7:323]	[/,09:/]	[5:206] 0:071 (1:451) [1:601]	[5:483] 0:179 (2:076) [2:300]	[5:542] 0:293 (2:609) [2:904]	(3:026) (3:026) (3:355]	[5:477]	[0:172]	[6:736]	[68,6]	[//5//]	[/32/]	[0cc:8]	[8:540]	[5:152]	[886:6]	[908:6]	[0:184]
GP₁									0:235 (2:850) [3:187]	0:453 (2:818) [3:186]	0:737 (3:246) [3:681]	0:845 (2:972) [3:361]								
च् †										,		,	0:234 (2:363) ([2:464] [0:234 0:531 2:363) (3:255) (2:464) [3:336] [0:713 (3:159) ([3:250] [0:713 2:515) 2:599]				
₫G _t																	0:172 (2:681) ([2:835] [0:203 1:635) (1:743] [0:199 1:133) (1:218] [0:181 0:861) 0:921]
\mathbb{R}^2	0:352	0:375	0:388	0:392	0:365	0:398	0:420	0:431	0:398	0:425	0:457	0:451	0:396	0:441	0:449	0:432	0:401	0:395	0:398	0:397
									Panel B:	: Subsamp	Subsample, 1985-2014	9014								
maturity n (year)	2	2	7	10	2	2	7	10	2	2	7	10	2	2	7	10	2	2	7	10
Ġ.	0:729 (5:278)	2:900 (7:584)	4:096 (6:297)	5:225 (5:680)	0:706 (5:550)	2:634 (6:027)	3:740 (4:991)	4:743 (4:574)	0:651 (4:698)	2:611 (6:234)	3:657 (5:731)	4:536 (5:252)	0:735 (5:346)	2:894 (7:569)	4:011 (6:677)	5:150 (5:979)	0:676 (5:278)	2:794 (7:062)	4:006 (5:781)	5:147 (5:327)
eNa t	[5:731]		[6:585]	[5:989]	[5:876] 0:030 (0:426) [0:462]	[6:392] 0:333 (1:916) [2:107]	[5:288] 0:447 (1:801) [1:988]	[4:857] 0:604 (1:945) [2:148]	[5:085]	[6:717]	[6:118]	[5:638]	[5:813]	[7:942]	[6:958]	[6:298]	[5:605]	[7:379]	[6:085]	[5:642]
G P₁									0:149 (1:405) [1:583]	0:551 (1:738) [1:953]	0:837 (1:993) [2:194]	1:315 (2:708) [2:953]								
đ,													0:001 (0:347) [0:378]	0:002 (0:121)	0:021 (1:241)	0:019 (1:065)				
d _{Gt}																	0:340 (3:612) ([3:979] [0:675 2:548) (2:749] [0:575 1:344) (1:442] [0:500 0:894) 0:963]
\mathbb{R}^2	0:301	0:397	0:393	0:398	0:303	0:416	0:410	0:416	0:331	0:431	0:432	0:457	0:303	0:397	0:410	0:406	0:413	0:434	0:406	0:404

Table 2: Out-of-Sample Performance Assessment

Panel A reports accuracy of out-of-sample forecasts from models with and without the real-time macro factor G as a return predictor. Benchmark predictors considered include the rst three principal components (PCs) of observed yields $(\widetilde{PC}_{1-3;t}^0)$ and the rst ve PCs of the noise-uncontaminated yield curve $(\widetilde{PC}_{1-5;t})$. The rows labeled \ENC-REG" report the out-of-sample t-statistics proposed by Ericsson (1992), and those labeled \ENC-NEW" report a variant of the ENC-REG statistic proposed by Clark and McCracken (2001); both tests share the same null hypothesis that the benchmark model encompasses the unrestricted model with excess predictors. R_{oos}^2 " denotes the out-of-sample R^2 of Campbell and Thompson (2008), and the rows labeled R_{oos}^2 " represent the incremental R_{oos}^2 due to G. Panel B reports the certainty equivalent gains (in percentage) for a mean-variance investor who selects an N-year bond ($N \ge 2$) along with a 1-year bond and who uses portfolios weights potentially depending on G-based forecasts. The investor's risk aversion coe cient γ is assumed to be either 3 or 5. The p-values of certainty equivalent

Table 4: Statistical Inference about Unspanned Macro Risks

Panel A reports results from likelihood-ratio tests of the macro-unspanning restrictions (H_0^{US}) , given in Eq. (12), that are imposed on an \mathcal{N} -factor unconstrained macro-nance term structure model (MTSM). Its underlying state vector is $X_t = (PC_1 \mid_{L,t}, \widehat{G}_t)$, where PC_{1} L;t denotes the vector of the rst \mathcal{L} principal components (PCs) of the noiseuncontaminated yield curve and \widehat{G}_t represents the SAGLasso macro factor. Model-based test statistics (column 2) are evaluated against the critical values of a χ^2 -distribution with degrees of freedom equal to $(k-\mathcal{N})(\mathcal{N}+1)-1$, where k is the number of bonds involved. Model-free test statistics (column 3) are evaluated based on the $\chi^2(k)$ -distribution. The p-values appear in angle brackets immediately beneath. Panel B considers the projection of the SAGLasso macro factor (\widehat{G}_t) onto the rst \mathcal{N} PCs of the yield curve ($PC_{1-N;t}^o$). Column 5 shows regression R^2 s along with two sets of 95% con dence intervals based on 5,000 arti cial samples simulated from model $CSM(\mathcal{L}, \mathcal{N})$ as speci ed in Section IA.G.1 (which denotes the \mathcal{N} -factor constrained MTSM with a spanned \widehat{G}_t and whose state vector $X_t = (PC_1 \mid_{L;t}, \widehat{G}_t)$). The con dence intervals in brackets beneath are obtained under either the assumption that there is no macro measurement error ($\eta_f = 0$) or that there is macro measurement error $(\eta_f \neq 0)$, as indicated in column 4 where η_f denotes macro measurement error (\Macro M.E."). Column 6 reports the rst-order serial correlation of residuals.

(1)	(2)	(3)	(4)	(5)	(6)
	Panel A: Tests of unspar	nning restrictions	Panel B: Regressions o	f \widehat{G}_t on I	PC_{1-M+}^{o}	
\mathcal{N}	Model-based	Model-free	Macro M.E.	I	, -	AR(1) of residuals
4	28.69 (0.122)	10.05 ⟨0.074⟩	No $(\eta_f = 0)$ Yes $(\eta_f \neq 0)$	[0.593	0.847] 0.769]	0.667
5	24.29 (0.185)	8.23 (0.083)	No $(\eta_f=0)$ Yes $(\eta_f\neq 0)$	[0.506		0.667
6	17.55 ⟨0.287⟩	6.17 ⟨0.104⟩	No $(\eta_f = 0)$ Yes $(\eta_f \neq 0)$	[0.263	0.651] 0.630]	0.666

Figure 1: Word Cloud from Selected Macroeconomic Series

This gure reports the list of words constituting the names of macroeconomic series that are selected from the SAGLasso algorithm. Font size of a word is proportional to the frequency with which the word appears in selected macroeconomic variables and their lags.



Figure 2: The SAGLasso Factor and Excess Returns on the Five-Year Bond

This gure presents time variation in the normalized SAGLasso factor as well as excess returns on the ve-year bond over the sample period from January 1964 to December 2013. Shaded bars denote months designated as recessions by the National Bureau of Economic Research.

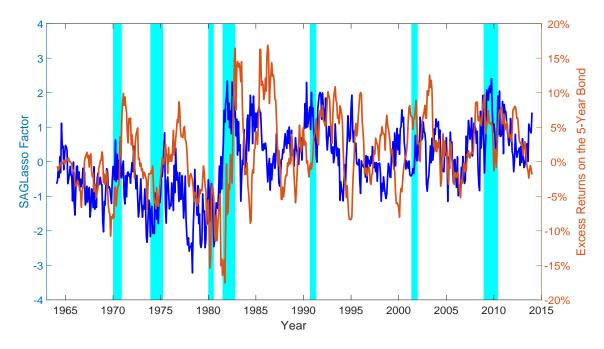


Figure 3: Time Variation of Macro Variable Importance

excess bond returns, and each macroeconomic series could have at most 7 non-zero coe cients (on their contemporaneous and lagged values). X-axis corresponds to the observation date of excess bond returns, and color gradients within each column indicate the most impactful (dark blue) to least important (white) variables. The 131 series are divided into eight groups: G1) output (17 series); G2) labor market (32 series); G3) housing sector (10 series); G4) orders and inventories (14 series); G5) money and credit (11 series); G6) bond and FX| interest rates or nancial (22 series); G7) prices or price indices (21 series); and G8) stock market (4 series). In each month since January 1984, the macroeconomic panel data over the past 20 years is input into the SAGLasso algorithm to forecast one-year-ahead This gure presents the norm of coe cients associated with the 131 macroeconomic series and their lagged values in the rolling-window bond return prediction.

Internet Appendix to \Machine-Learning-Based Return Predictors and the Spanning Controversy in Macro-Finance"	•

Internet Appendix

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IA.A Inferring Higher-Order Yield Principal Components

reveals that replacing (Itered) $PC_{4-5;t}$ by $PC_{4-5;t}^o$ results in lower R^2 values, regardless of the bond maturity, where for convenience those four R^2 values from Table 2 are shown in the row labeled R^2 (Table 2)" in panel B. Note that the decline in R^2 ranges from 0.014 for the four-year bond to 0.018 for the three-year bond (the second last row of panel B), and the percentage decrease in R^2 ranges from 5.49% for the four-year bond to 7.73% for the three-year bond (the last row). Given that the rst three factors alone can have an R^2 of 16{19% (columns 2{5 of Table IA.B5), the aforementioned amount of information loss in the fourth and fth factors is far from trivial. As such, using $PC_{1-5;t}^0$ in regression tests of H_0^{S2} would make the hypothesis overrejected.

IA.B More on Properties of the SAGLasso Macro Factor

This appendix further examines the properties of the SAGLasso macro factor (\widehat{G}) . Section IA.B.1 investigates the predictive power of the three group factors which constitute the SAGLasso factor. Section IA.B.2 examines whether the three group factors are spanned or not. Section IA.B.3 compares the predictive power of the \widehat{G} and Ludvigson and Ng (2009; LN09 hereafter) macro factors. Section IA.B.4 investigates the potential impact of data revision and publication lags on return predictability. Section IA.B.5 presents in-sample tests of the spanning hypotheses, H_0^{S1} and H_0^{S2} . Lastly, Section IA.B.6 implements the SAGLasso algorithm using 131 macro variables along with di erent numbers of their lags.

IA.B.1 Predictive Power of the Three Group Factors

The SAGLasso macro factor \widehat{G}_t consists of three group factors: the employment (\widehat{g}_{1t}) , housing (\widehat{g}_{2t}) , and in ation (\widehat{g}_{3t}) factors. To better understand the information content of factor \widehat{G}_t , we examine properties of these three group factors in this subsection. Let $\{\widehat{g}_{it}\}_{1=t-3}$ denote $\{\widehat{g}_{it}, 1 \le i \le 3\}$.

IA.B.1.1 Sample Period 1964{2014

Table IA.B1 reports the Pearson correlation matrix of \widehat{G} , $\{\widehat{g}_{it}\}_{1=i-3}$, and ve yield curve factors. The ve yield curve factors include the rst three principal components (PCs) of *observed* bond yields, $\{PC_{i;t}^0, i=1,2,3\}$, and the Itered higher-order PCs of noise-uncontaminated yields, $PC_{4;t}$ and $PC_{5;t}$. As expected, \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} all have low correlations with the yield curve factors. In

particular, the novel housing factor \widehat{g}_{2t} has a correlation of -0.167 with $PC_{1;t}^o$, -0.073 with $PC_{2;t}^o$, and 0.222 with $PC_{3;t}^o$. As a result, \widehat{G} is weakly correlated with $PC_{1-3;t}^o$ and hardly correlated with $PC_{4;t}^o$ and $PC_{5;t}^o$. Recall that by construction the \widehat{G} factor and its three component factors control for the Treasury and FX variables (group 5) out of the 131 macro series. The results shown in the table verify that \widehat{G} and $\{\widehat{g}_{it}\}_{1=i-3}$ are all weakly correlated with the yield curve. Nonetheless, as shown below these group factors have strong predictive power as a result of the SAGLasso procedure used for model selection.

We now examine the predictive power of \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} , both individually and jointly. Panel A of Table IA.B2 presents results from predictive regressions of excess bond returns on normalized \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} , for 2-, 3-, 4-, and 5-year bonds in the full sample period. Panel A1 reports coe cient estimates, t-statistics, and R-squared of univariate regressions on each of the three group factors. Note that these factors all exhibit signicant unconditional predictive power, with an R^2 of 21{22% for \widehat{g}_{1t} , about 14{15% for \widehat{g}_{2t} , and 17{18% for \widehat{g}_{3t} . Results from multivariate regressions, reported in panel A2, show that the three group factors are still all signicant and together have an (adjusted) R^2 ranging from about 40% for the 2-year bond to 43% for the 3-year bond.

As shown in Joslin, Priebsch, and Singleton (2014; JPS hereafter), the impact of macro risk factors on bond risk premia depends on horizons. Panel A of Table IA.B2 illustrates the relative importance of the three group factors across bond maturity. The univariate regression results indicate that the regression coe cient on \hat{g}_{1t} is the largest, followed by the one on \hat{g}_{3t} , and the coe cient on \hat{g}_{2t} is the lowest, regardless of the bond maturity. The univariate regression R^2 values exhibit the same pattern. In the multivarite regressions, the regression coe cients on the three group factors maintain the same ranking, regardless of the bond maturity. These results indicate that relatively speaking, among the three group factors, the employment factor (\hat{g}_{1t}) is the most important, followed by the in ation factor (\hat{g}_{3t}) , and then by the housing factor (\hat{g}_{2t}) . Note, however, that these group factors are trained on the aggregate bond market returns rather than returns on bonds with a speci c maturity. Bianchi, Bechner, and Tamoni (2021) consider more categories of macro variables and \hat{g}_{1t} is the short-end (long-end) of the yield curve.

IA.B.1.2 Sample Period 1952{2014

The full sample used in this study is 1964{2014. However, it is known that the relationship between interest rate and real activity changed signic cantly around 1964. This raises one concern about the robustness of our evidence for the predictive power of \widehat{g}_{lt} , i=1,2,3 and \widehat{G}_t based on the 1964{2014 sample: If we extend the sample to several years earlier, that may signicantly change the results. To address this concern, we reexamine the predictive power of these macro factors using the sample extended to 1952, the year from which the data coverage of the original Fama-Bliss yields starts. IA.2 However, some macro series, especially those related to housing, are not available going back that far; thus, we reconstruct the employment factor only in this robustness check, and denote the factor constructed in-sample by \widehat{g}_{1t} and its out-of-sample version by \widetilde{g}_{1t} . Recall from Section 3 that the Nabor" group includes 32 series. As two of these series are no longer available when the sample extends back to 1952, \widehat{g}_{1t} or \widetilde{g}_{1t} is constructed using the remaining 30 macro series.

Results from in-sample regressions, reported in panel B1 of Table IA.B2, indicate that the predictive power of the employment factor is robust to the extended sample. Comparing panels A1 and B1, we see that the predictive power of \hat{g}_{1t} is slightly weaker than that of \hat{g}_{1t} in terms of the magnitude of regression coe cients or R^2 value but the coe cient on \hat{g}_{1t} has greater t-value than that on \hat{g}_{1t} regardless of the bond maturity.

In the out-of-sample tests, the training period is 20 years, which is close to the 21-year period length adopted in our full-sample (1964{2014}) analysis. In other words, the employment factor is reconstructed every month after December 1971 using Adaptive Lasso within a given group, and the predictive regression is also reestimated recursively. As before, we consider the following three out-of-sample statistics: the \ENC-REG" (Ericsson 1992), the \ENC-NEW" (Clark and McCracken 2001), and the out-of-sample R-squared R_{oos}^2 (Campbell and Thompson 2008) statistics. The results shown in panel B2 of Table IA.B2 indicate that \tilde{g}_{1t} has signi-cant out-of-sample predictive power for every bond considered. Additionally, R_{oos}^2 increases in the bond maturity, ranging from 0.155 for the 2-year bond to 0.169 for the 5-year bond.

Overall, the above results provide evidence that the predictive power of the employment factor (one main component of the SAGLasso single factor \hat{G}_t) is robust to the longer sample 1952{2014.

IA.2 The supplement to Cochrane and Piazzesi (2005), available at http://www.stanford.edu/~piazzesi/cp.zip, suggests that Fama-Bliss yield data prior to 1964 is unreliable.

IA.B.2 Spanning Properties of the Group Factors

Having examined the predictive power of the three group factors, we explore, to what extent, each of the three factors is spanned or unspanned in this subsection.

Recall from Table IA.B1 that \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} all have low correlations with the yield curve factors. In an untabulate analysis, we not that the three group factors are not highly correlated with GRO (growth) and INF (in ation) either, two standard single macro variables used in the literature. Unsurprisingly, the largest correlation (0.497) occurs between the two in ation factors, \widehat{g}_{3t} and INF_t . The correlations between INF_t and the other two group factors are 0.237 for \widehat{g}_{1t} and 0.144 for \widehat{g}_{2t} . The growth variable GRO has a correlation of -0.013, 0.167, and -0.015 with \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} , respectively. These indings suggest that the three group factors are viable candidates for unspanned macro variables.

We examine whether the three group factors are spanned by the yield curve, following Section 5.4 that conducts a similar analysis for \widehat{G}_t . That is, for each of the three group factors, we rst regress the factor on the rst \mathcal{R} PCs of the yield curve $(PC_1^o_{R,t})$, where $\mathcal{R}=3$ or 6; we then evaluate the regression R^2 against its distribution implied from a constrained and spanned model; we also estimate the rst-order correlation of residuals from the regression to see if the residuals are serially uncorrelated. The model used here to generate distributions of R^2 is model $CSM(3,6)_{group}$, whose state vector includes three yield curve factors (the rst three PCs) and three macro factors, \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} . The estimation of the model is done under the assumption that the three macro factors are measured either with or without errors.

Table IA.B3 reports the regression results for each of the group factors with $\mathcal{R}=3$ (panel A) or 6 (panel B). Column 2 indicates whether the three macro variables are assumed to be measured with errors in the estimation of model. Columns 3 (panel A) and 5 (panel B) show the regression \mathbb{R}^2 s, and in brackets beneath are reported 95% con-dence intervals based on 5,000 arti-cial samples simulated from model $CSM(3,6)_{group}$. Columns 4 (panel A) and 6 (panel B) report the rst-order serial correlation of regression residuals. Clearly, the regression \mathbb{R}^2 is outside of the 95% con-dence intervals for each of the group factors in either panel. Moreover, even the smallest estimated rst-order serial correlation is around 90%, suggesting that much of the persistent component is mistakenly treated as white-noise shocks. All of the evidence indicates that the three SAGLasso

group macro factors $\{\widehat{g}_{it}, 1 \leq i \leq 3\}$ are not spanned by the yield curve factors.

IA.B.3 Comparison with the Ludvigson and Ng (2009) Factor

The LN09 single factor, constructed through dynamic factor analysis and BIC-based stepwise predictive regression, is $\overrightarrow{F6}_t = (\widehat{F}_{1t}, \widehat{F}_{1t}^3, \widehat{F}_{2t}, \widehat{F}_{3t}, \widehat{F}_{4t}, \widehat{F}_{8t})$, the particular polynomial function of LN09's eight dynamic factors that minimizes the BIC over the sample period 1964{2003. However, using our panel of 131 \real-time" macro series over 1964{2014, we nd that the selected subset includes $\overrightarrow{\mathcal{F}}_{1t}^{7} = (\widehat{F}_{1t}, \widehat{F}_{1t}^{3}, \widehat{F}_{2t}, \widehat{F}_{5t}, \widehat{F}_{5t}^{2}, \widehat{F}_{8t}, \widehat{F}_{8t}^{2})$, IA.3 whose R^{2} value is 0.256, higher than 0.214 of $\overrightarrow{F}_{6t}^{4}$'s. Hence, we let \widehat{LN}_t^m (the modi ed LN factor) be $\overrightarrow{\mathcal{F}_t}$ in our empirical analysis.

Although both \widehat{G} and \widehat{LN}^m are extracted from the same set of 131 macro series, they dier in several aspects. First, whereas \widehat{LN}^m includes all 131 series and squares and cubes of these macro variables, \widehat{G} is a *linear* combination of 19 series and some of their lagged variables, and consists of three easy-to-interpret macro group factors. Second, in terms of economic interpretation, \widehat{G} includes a housing factor that contributes little to \widehat{LN}^m , whose important components are the \real activity" (highly correlated with measures of employment and production such as IP growth), \in ation," and \stock market" factors. Also, \widehat{G} includes no variables from the \bond and FX" group and thus is much less correlated with the yield curve than \widehat{LN}^m is. Lastly, by construction \widehat{G} takes into account the dynamic response of bond risk premia to macroeconomic innovations. In contrast, information on term premia does not enter \widehat{LN}^m until the last step of its construction.

Panel A of Table IA.B4 reports the prediction results based on \widehat{LN}_t^m for the full sample. Results from the in-sample analysis reported in panel A1 show that \widehat{LN}_t^m is significant, regardless of the bond maturity, and that the R^2 increases in the bond maturity, ranging from 0.168 for the 2-year bond to 0.250 for the 5-year bond. Recall from panel A1 of Table 1 that the \mathbb{R}^2 from regressions on \widehat{G}_t ranges from 0.352 for the 2-year bond to 0.392 for the 5-year bond. The di erence between this R^2 and that of \widehat{LN}_t^m is 0.18, 0.16, 0.15, and 0.14 for the 2-, 3-, 4-, and 5-year bonds, respectively. These results indicate that \widehat{G}_t has a greater predictive power than \widehat{LN}_t^m for excess bond returns. IA.4 Results from the out-of-sample analysis also support this conclusion, as can be seen from evidence shown in panel A2 of Table IA.B4 for \widehat{LN}_t^m and that in panel A of Table 2 for \widehat{G}_t . To summarize,

TA.3 The variable \widehat{F}_{5t}^2 is also selected by Ludvigson and Ng (2011), who consider the sample period 1964(2008. IA.4 This nding is robust in the post-1984 sample period (untabulated).

even though \widehat{G}_t is linear and much more parsimonious than \widehat{LN}_t^m , the former predictor shows stronger predictive ability than the latter in both in-sample and out-of-sample analyses.

be mitigated straightforwardly, however, since in practice it is easier to make an adjustment for publication lags than to gure out preliminary macro data releases and adjust for data revisions.

Note that the main inding of this subsection is consistent with Ghysels, Horan, and Moench (2018), who document that using revised macro series in ates the predictive power of macro variables. However, while they focus on a particular macro variable | \total non-farm payroll employment" (#33 on our list of 131 series) | and individual not that both data revisions and publication lags are highly important, we examine the impact of these two elements on a large panel of macro time series and individual not that the predictive power of the SAGLasso (aggregate) macro variable is robust to the use of vintage data. Namely, the importance of revision/delay biases depends on speciic macro series, especially given that variable #33 itself is not included in \hat{G} (see Table A.1 in the paper). This implication is consistent with Ghysels et al. (2018) too. In a robustness analysis, they consider the Chicago Fed National Activity Index (an unsmoothed version of macro variable GRO) and individual that the combined elect of publication lags and data revisions on these two aggregate macro variables is small. Also, Barillas (2012) individual not preal growth measures) considered in his study.

IA.B.5 In-Sample Spanning Tests

This subsection tests the spanning hypotheses, H_0^{S1} and H_0^{S2} , by examining the incremental predictive power of \widehat{G} over the yield curve. As before, we focus mainly on the test statistics based on the HH or NW standard errors in the discussion of test results that follows.

Table IA.B5 presents the results based on the full sample. Results from regressions on $PC_{1-3;t}^o$ reported in columns 2{5, indicate that only $PC_{2;t}^o$ is signi-cant and that the R^2 ranges from 0.156 for the 3-year bond to 0.194 for the 5-year bond. Results from each of the above regressions augmented with \hat{G}_t , reported in columns 6{9, show that \hat{G} is signi-cant regardless of the bond maturity. The incremental R-squared due to \hat{G}_t , R^2 , ranges from 0.243 for the 5-year bond to 0.262 for the 3-year bond. These results provide strong evidence against H_0^{S1} .

Results from regressions on $PC_{1-5;t}$, shown in columns 10 through 13, indicate that in addition to $PC_{2;t}$, the higher-order $PC_{4;t}$ and $PC_{5;t}$ are also signi-cant for most bonds. The R^2 ranges in the results of the observed yields is unable to electively.

from 0.221 for the 2-year bond to 0.255 for the 4-year bond. Augmenting these regressions with \widehat{G}_t yields a R^2 ranging from 0.232 for the 5-year bond (column 17) to 0.253 for the 3-year bond (column 15). Importantly, \widehat{G}_t is significantly different from zero regardless of the bond maturity and standard errors used, indicating a rejection of H_0^{S2} . In addition, $PC_{2;t}$ and $PC_{4;t}$ become less significant (and insignificant for the 2- and 3-year bonds) in the presence of \widehat{G}_t .

The results for the post-1984 sample, reported in Table IA.B6, are qualitatively the same as those for the full sample. Particularly, \widehat{G}_t is signi cant, regardless of the bond maturity and standard errors used, conditional on either $PC_{1-3;t}^o$ (columns 6{9}) or $PC_{1-5;t}$ (columns 14{17}); namely, H_0^{S1} and H_0^{S2} are strongly rejected by the post-1984 sample too. Compared with its counterparts for the full sample (Table IA.B5), R^2 due to \widehat{G}_t is actually higher except for the 2-year bond. For instance, R^2 from regression tests of H_0^{S1} for the 5-year bond is 0.297 for the post-1984 sample (column 7) and 0.243 for the full sample (column 9 in Table IA.B5). Regarding the impact of PCs in the presence of \widehat{G}_t , $PC_{1;t}^o$ ($PC_{2;t}^o$) remains signi cant for the 2- and 5-year bonds (10-year bond) in the tests of H_0^{S1} . For regression tests of H_0^{S2} (columns 14{17}), $PC_{1;t}$ is signi cant regardless of the bond maturity, $PC_{2;t}$ is signi cant for the 7- and 10-year bonds, and $PC_{5;t}$ for the 2-year bond only.

An earlier version of the paper also considers test statistics based on Hodrick 1B standard errors. We not that \hat{G} remains significant regardless of the bond maturity, whereas some of the PCs become insignificant. For instance, $PC_{2;t}^o$ remains significant only for the 4- and 5-year bonds and is subsumed by \hat{G}_t regardless of the bond maturity.

In summary, when factor \widehat{G} is used as the macro-based return predictor, our in-sample test results show that this new macro variable has predictive power above and beyond the contemporaneous yield curve or yield dynamics, and thereby reject both Spanning Hypotheses I and II.

IA.B.6 Tests Using Macro Variables with Di erent Lags

So far the SAGLasso algorithm has been implemented using 131 macro variables along with six of their lags. In this subsection we address the following two questions: (1) Are lags of macro variables are essential to maintain the predictive performance as documented in Section 4, given disentangle higher-order PCs from noise in yields. Filtered higher-order PCs ($PC_{4-5;t}$) contain more information about bond risk premia than higher-order observed PCs ($PC_{4-5;t}$).

that 21 constituent variables (out of 30) of G are lagged? (2) If so, what is the optimal number of lags to be included in our supervised learning?

These are nontrivial questions as a panel of macro data with no lags or a small number of lags has a denser structure and might deliver better out-of-sample performance given the limited length of the training period. To see this, recall that tuning parameters are selected using cross-validations in the SAGLasso algorithm (see Appendix C). Therefore, as we include more and more lags, the estimation process is inevitably subject to more \noise", which could overweigh bene ts of incorporating more historical information in the construction of the SAGLasso factor.

In what follows, we repeat the analysis in Section 4.1 using 131 macro variables along with N_L of their lags, where $N_L = 0, 3, 9, 12$. To be more speci-c, for each value of N_L , we -rst reconstruct the SAGLasso factor following the procedures described in Appendix C and then examine the predictive power of the reconstructed SAGLasso factor.

Figure IA.B1 depicts the unconditional predictive power of the SAGLasso factor constructed using the macro data with $N_L=0,3,6,9,12$. For brevity, we report the results for 2-year and 5-year bonds only. Panel A shows that including lags clearly enhances the in-sample predictive power of the SAGLasso macro factor.^{IA.6} However, using more lags does not necessarily raise the R^2 value: it is the highest with $N_L=3$ for the 2-year bond and with $N_L=6$ for the 5-year bond.

As discussed above, including more than 6 lags may induce nontrivial sampling variability of the SAGLasso estimates that is sulciently large to 0 set the gains from using more data. This conjecture is conlimited by the results for the out-of-sample R^2 shown in Panel B. Since the SAGLasso factor is estimated recursively (with a rolling 20-year window) in the out-of-sample analysis, we face greater uncertainty compared to the in-sample estimation. As a result, we note that the SAGLasso factor with $N_L = 9$ or 12 hardly outperforms the SAGLasso factor with $N_L = 0$ (no lag) in terms of the out-of-sample R^2 .

Overall, the results shown in Figure IA.B1 suggest that the SAGLasso factor constructed using the 131 macro variables along with 3 or 6 of their lags has the best performance in both the in-sample and out-of-sample predictions. This indingre ects a trade-or between including more information

^{1A.6}Note that including lags into the SAGLasso algorithm does not simply lead to an expansion in the set of selected macro variables. Instead, the coe cients of some previously selected (contemporaneous) variables are shrunk to zero, \crowded out" by more powerful lagged variables. For example, 29 macro variables are selected with $N_L = 0$, but only 9 of them have nonzero coe cients with $N_L = 3$.

in the supervised learning and imposing a denser data structure to enhance the estimation stability. While the baseline SAGLasso factor (with $N_L=6$) seems to capture more information on long-term bond premiums, the alternative SAGLasso factor with $N_L=3$ outperforms for short-term bonds.

Next, we examine whether or not the choice of lag length a ects our inferences with respect to Spanning Hypotheses I and II. We test these two hypotheses using the above SAGLasso factor with di erent values of N_L and report the test results in panels A and B of Table IA.B7, respectively. As before, the test statistics used include the Hansen-Hodrick one, the Newey-West statistic, and R^2 (the incremental in-sample R^2) for the in-sample tests, as well as the ENC-REG statistic, the ENC-NEW statistic, and R^2_{oos} (the incremental out-of-sample R^2). Note that both of the spanning hypotheses are overwhelmingly rejected in both the in-sample and out-of-sample tests, regardless of the value of N_L considered. In particular, the two hypotheses are strongly rejected when no lags ($N_L = 0$) are used in the construction of the SAGLasso factor.

Finally, we perform the $\,$ nite-sample analysis based on the SAGLasso factor with $N_L=3$. Untabulated results show that the $\,$ nite-sample u27teSAeforemenstatistic, in TableItremacrond

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form for YTSMs, the JLS canonical form de nes the most general admissible Gaussian MTSM for a given dimension of the state vector.

Denote the state vector satisfying the JLS canonical form is denoted by X_t . Its Q-measure dynamics and the resulting bond pricing formula are

$$r_t = r_1^{\mathcal{Q}} + i \cdot X_t, \tag{IA.C1}$$

$$X_t = {}_{x}^{\bigcirc} X_{t-1} + {}_{x} \epsilon_t^{\bigcirc}, \tag{IA.C2}$$

$$y_t^{(m)} = A_m(\ _Y^{\bigcirc}) + B_m(\ _Y^{\bigcirc})^{\emptyset} X_t$$
 (IA.C3)

where $r_{7}^{\mathbb{Q}}$ denotes the long-run mean of the short rate under \mathbb{Q} , $^{\mathrm{IA.7}}$ $_{i}$ is a vector of ones, $^{\mathbb{Q}}-I$ has the real Jordan form determined by the eigenvalue vector $\gamma^{\mathbb{Q}}$, and $^{\mathbb{Q}}_{x}$ is lower triangular. Under this representation, $^{\mathbb{Q}}_{y} \equiv \{\gamma^{\mathbb{Q}}, r_{7}^{\mathbb{Q}}, ^{\mathbb{Q}}, ^{\mathbb{Q}}\}$ governs X_{t} 's \mathbb{Q} -dynamics and thus fully determines bond pricing. Coe cients A_{m} and B_{m} are given by

$$B_{m} = \frac{1}{m} \left(I - {\begin{pmatrix} Q \ell \end{pmatrix}} \right)^{-1} \left(I - {\begin{pmatrix} Q \ell \end{pmatrix}}^{m} \right) i,$$

$$A_{m} = r_{1}^{Q} - \frac{1}{2m} \sum_{i=1}^{m-1} B_{i}^{\ell} {\begin{pmatrix} X & X \end{pmatrix}}^{\ell} B_{i}.$$

While the state vector X_t de nes the minimum number of parameters shaping the risk-neutral distribution of bond yields, it keeps silent about the role of macro factors F_t in bond pricing. Unless the macro-unspanning restrictions, as specified in Eq. (12), are imposed, F_t are included in MTSMs as pricing factors, i.e., there is a linear mapping between F_t and X_t as follows:

$$F_t = A_f + B_f X_t$$
.

For ease of notation, in the discussion that follows in this this subsection, we drop the subscript/superscript \mathcal{M} from $Y_t^{\mathcal{M}}$ and $\{\mathcal{A}_{\mathcal{M}}, \mathcal{B}_{\mathcal{M}}\}$, where \mathcal{M} denotes the maturities of zero yields to be considered. Suppose that the yield-curve factors in X_t are defined by a full-rank loading matrix $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the property of the subscript $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the property of the subscript $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the property of the subscript $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the property of the subscript $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the subscript $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ and $\overline{\mathbb{R}^{N_t}}$ are the subscript $\overline{\mathbb{R}^{N_t}$

$$X_t = \mu_x^{\mathbb{Q}} + \ \ _x^{\mathbb{Q}} X_{t-1} + \ \ _x \epsilon_t^{\mathbb{Q}},$$

where $\mu_{\mathbf{X}}^{\mathbb{Q}}=(u_{7}^{\mathbb{Q}}^{\mathbb{Q}},\mathbf{0}_{1})^{\theta}$. However, as long as X_{t} is stationary under the risk-neutral measure and the rst element of $\gamma^{\mathbb{Q}}$ is non-repeated, $r_{7}^{\mathbb{Q}}$ and $u_{7}^{\mathbb{Q}}$ are interchangeable in de ning the canonical form: $r_{7}^{\mathbb{Q}}=-u_{7}^{\mathbb{Q}}/\gamma_{1}^{\mathbb{Q}}$.

^{IA.7}In the JSZ canonical form there is no constant term in the short-rate equation (IA.C1). Instead, there is a constant term in the transition equation:

 $W_{\perp} \in \mathbb{R}^{\perp}$, i.e., $\mathcal{P}_t = W_{\perp}Y_t$. It follows that the latent state vector X_t can be rotated to $X_t^{\text{IA.8}}$

$$X_t = 0 + 1X_t,$$

where

$$0 = \begin{bmatrix} W_{\perp} \mathcal{A} \\ A_f \end{bmatrix}, \quad 1 = \begin{bmatrix} W_{\perp} \mathcal{B} \\ B_f \end{bmatrix}.$$

The resultant bond-pricing coe cients for the rotated state vector X_t are

$$B_m = {}_{1}{}^{1\ell}B_m,$$

$$A_m = A_m - B_m \ 0.$$

This leads to a closed-form expression for the probability density function of observed yields conditional on X_t , which completes the maximum likelihood estimation.

Note that $\{A_m, B_m\}$, defined in Eq. (8), depend on ${}^{\mathbb{Q}}_M \equiv \{\gamma^{\mathbb{Q}}, r_1^{\mathbb{Q}}, A_f, B_f, {}_{\chi}\} \supset {}^{\mathbb{Q}}_{\chi}$. As such, adding macro factors to DTSMs allows for greater exibility in thing the conditional distribution of bond yields, as evidenced by the $(\mathcal{N} - \mathcal{L})(\mathcal{N} + 1)$ additional free parameters in MTSMs. IA.9

Even if we ignore the additional exibility o ered by F_t , it is preferable to factorize the conditional likelihood function in terms of $X_t = (\mathcal{P}_t^\emptyset, F_t^\emptyset)$, as opposed to latent factors X_t . First, if the yield portfolios as represented by \mathcal{P}_t are assumed to be priced perfectly (JSZ; JPS), the P-measure conditional density of state variables, $l(X_t|X_{t-1},\mu_X^P, -\frac{P}{X}, -x)$, can be assessed with standard linear projection; JSZ show that the OLS leads to ML estimators of $\{\mu_X^P, -\frac{P}{X}\}$. Second, even if we allow all yields to be measured with error, an OLS regression of X_t^P (= $X_t + \eta_t$) provides fairly reasonable starting values in the estimation of $\{\mu_X^P, -\frac{P}{X}, -x\}$.

IA.C.2 Selection of MTSMs

In Sections IA.G.2 and IA.G.3 of the paper, we follow JPS and conduct a large-scale search for the best set of zero restrictions on risk premium parameters in constrained models $CSM(\mathcal{L},\mathcal{N})$ and $CUSM(\mathcal{L},\mathcal{N})$. This section provides details of this analysis.

 $^{^{\}mathsf{IA.8}}\mathsf{The}$ invariant transformation from X_t to X_t calls for the loading matrix W_{\perp} . As the number of yield factors $\mathcal{L} \leq 5$ in models considered in Sections 5.2 and IA.G, W_{\perp} is estimated based on model YTSM(5) (see Internet Appendix IA.A for details). Unreported results show that the rst three rows of W_5 are almost identical to those of W_5 (as well as the loading matrix implied from model YTSM(3)), but there is substantial difference in the remaining rows.

^{1A.9}Therefore, model $SM(\mathcal{L}, \mathcal{N})$ has $2.5\mathcal{N}^2 + 3.5\mathcal{N} - \mathcal{N}\mathcal{L} - \mathcal{L} + 2$ parameters in total to estimate.

Recall from Section IA.G.1 that $CSM(\mathcal{L}, \mathcal{N})$ and $CUSM(\mathcal{L}, \mathcal{N})$ denote \mathcal{N} -factor constrained, spanned and unspanned MTSMs, respectively, where the underlying state vector $X_t = (PC_1 \ _{L:t}, \widehat{G}_t)$ and $PC_1 \ _{L} = (PC_1, \ldots, PC_L)$ denotes the rst \mathcal{L} PCs of bond yields. The one-period risk premium is as specified in Eq. (13):

$$t = \lambda_0 + \lambda_1 X_t = \lambda_0 + \lambda_1 \cdot (PC_1 / t, \widehat{G}_t)^{\ell}$$

where risk premium parameters λ_0 and λ_1 are an \mathcal{N} -dimensional vector and an $\mathcal{N} \times \mathcal{N}$ matrix, respectively. In the discussion below, we focus on the selection of spanned models $CSM(\mathcal{L}, \mathcal{N})$.

JPS's nding. Du ee (2010) also documents that there are two factors driving the variation in risk premium and presents evidence that this is a robust property of models with the Sharpe ratio constraints. These ndings in turn help explain why the restrictions placed on λ_0 and λ_1 make model-implied Sharpe ratios consistent with ones observed in data.

Note that while all three models, $CSM(\mathcal{N}\text{-}1,\mathcal{N})$ with $4 \leq \mathcal{N} \leq$ 6, imply non-zero compensation

where Y_t^o denotes the time-t observed yields of k zero-coupon bonds with maturities $\mathcal{M} = \{m_1, \dots, m_k\}$, $U_{\mathcal{M}}$ is a $k \times 3$ matrix with columns equal to the rst three eigenvectors of the variance matrix of Y_t^o , and the diagonal matrix ε_t represents thing errors.

We aim to show that the parameter restrictions specified in Eq. (IA.D5) have a close a first to the restrictions required for the MTSM in Section 5.1 to satisfy the hypothesis that macro variables have no predictive power for excess bond returns unconditionally (under the P-measure). Following Du ee (2007), we refer to this hypothesis as the \general" null hypothesis (GNH). To proceed, we rst introduce such restrictions, termed \macro-independence" restrictions in this study.

IA.D.2 \Macro-Independence" Restrictions

Consider the MTSM in Section 5.1. Given that the expected excess return on an m-period bond from t to t + j is

$$E_{t}\left(rx_{t;t+j}^{(m)}\right) = \operatorname{constant} + \psi_{m;j}^{\ell}X_{t}, \tag{IA.D6}$$
where $\psi_{m;j} = mB_{m}^{\ell} - (m-j)B_{m-j}^{\ell}({}^{\mathsf{P}})^{j} - jB_{j}^{\ell},$

the GNH implies that the last \mathcal{N} - \mathcal{L} columns of the model-implied matrix $\psi_{m:j}$ are entirely zero, regardless of bond maturity m or return horizon j. How to implement such restrictions in the model depends on j. Recall that, in our empirical analysis, predictive regressions use annual excess returns sampled at the monthly frequency, while MTSMs are estimated with monthly observations.

Let $\lambda_1 = [\lambda_{1p}, \lambda_{1f}]$ in Eq. (9). If j = 1 (month), then setting λ_{1f} to zero prevents macro factors from a ecting expected one-period excess returns. Without loss of generality, we allow all \mathcal{L} yield curve factors \mathcal{P}_t to drive variations in bond risk premia. As a result,

$$\psi_{m,1} = -(m-1)B_{m-1}^{\ell}\lambda_1 = -(m-1)B_{m-1}^{\ell}\left[\lambda_{1p}, 0_{N-(N-L)}\right]. \tag{IA.D7}$$

Under this specification, $E_t(rx_{t;t+1})$ is orthogonal to the macro state vector F_t . However, F_t can still a ect longer-horizon (j > 1) excess returns because future monthly returns, $\{E_t(rx_{t+i;t+i+1})\}_{i=1}^{t}$ are not orthogonal to F_t . For instance, note that $E_{t+1}(rx_{t+1;t+2})$ is determined by \mathcal{P}_{t+1} and $E_t(\mathcal{P}_{t+1})$ depends on F_t . Consequently, F_t contains information about future excess annual returns.

Asiswhen j > 1to ensure the state variables determining term premia to vary inde-

pendently of the macro factors, we specify the following P-measure dynamics of X_t :

$$X_{t} = \begin{bmatrix} \mathcal{P}_{t} \\ F_{t} \end{bmatrix} = \begin{bmatrix} \mu_{p}^{\mathsf{P}} \\ \mu_{f}^{\mathsf{P}} \end{bmatrix} + \begin{bmatrix} P_{p} & 0_{L-(N-L)} \\ 0_{(N-L)-L} & P_{ff} \end{bmatrix} \begin{bmatrix} \mathcal{P}_{t-1} \\ F_{t-1} \end{bmatrix} + \chi \epsilon_{X;t}^{\mathsf{Q}}.$$
 (IA.D8)

That is, the variation in F_t is independent of expected monthly bond returns at all leads and lags; thus, even for annual excess returns, the last \mathcal{N} - \mathcal{L} columns of $\psi_{m;12}$ are constrained to be zero.

Eqs. (IA.D7) and (IA.D8) together lead to the following conditions, termed \macro-independence" restrictions and denoted by H_0^{MI} , for the model to satisfy the GNH:

$$H_0^{MI}: \stackrel{\mathsf{P}}{fp} = 0, \qquad \stackrel{\mathsf{Q}}{pf} = \stackrel{\mathsf{P}}{pf} = 0, \text{ and } \stackrel{\mathsf{Q}}{ff} = \stackrel{\mathsf{P}}{ff}.$$
 (IA.D9)

Let $MIM(\mathcal{L}, \mathcal{N})$ denote the model subject to these restrictions. Unless specified otherwise, we focus on MTSMs with $\mathcal{N} = \mathcal{L} + 1$ and $F_t = G_t$ in the analysis that follows. For instance, model MIM(3,4) is used below to conduct the nite-sample inference about the GNH.

IA.D.3 VAR-based DGPs and Tests of the GNH

Note that the parameter restrictions specified in Eq. (IA.D5) are very close to the \macro-independence" restrictions given in Eq. (IA.D9) under model MIM(3,4). The only fundamental difference between the VAR-based model in Eqs. (IA.D4) and (IA.D5) and model MIM(3,4) is that the former does not rely on the Dufference and Kan (1996) restrictions for an aline mapping from bond yields to the yield-curve factors. However, empirically this difference is expected to have little impact on the dynamics of expected excess returns, as matrix U_M obtained from the PCA does not significantly deviate from the loading matrix \mathcal{B}_M in Eq. (11). IA.11 Therefore, like model MIM(3,4), the above VAR-based model implies that term premia are time-varying and driven by yield PCs only; that is, by construction, the macro factors F_t have no predictive power for future yields and bond returns. As such, the VAR-based model in Eqs. (IA.D4) and (IA.D5) satis as the GNH rather than H_0^{S1} stated in Section 2.2. Put differently, as macro risks are not priced at all in this VAR-based DGP, it is not suitable for conducting tests of evidence for unspanned macro risks.

To further illustrate this point, we generate bootstrap samples using the VAR-based model and

 $^{^{\}text{IA.11}}$ To see this, another equivalent approach to estimating Eq. (11) is regressing the bond yields on yield PCs. While the Du e-Kan restrictions are not imposed in this estimation (unless the number of factors equals k-1), the small magnitude of measurement errors ensures that the OLS-implied loading matrix for $PC_{1-3/t}$ is very close to $\mathcal{B}_{\mathcal{M}}$ if the term structure is truly described by a no-arbitrage dynamic term structure model (Du ee 2010a).

investigate the properties of regression statistics under the same DGP. To proceed, letting F_t be the single SAGLasso factor G_t in the model, we estimate $\mu_p, \mu_f, p_p, f_f, p_t$ and f_t with MLE as in Section 5. Next, we generate bootstrap samples from Eqs. (IA.D4) and (IA.D5) and use a residual bootstrap to resample the PCs and SAGLasso factor based on Eq. (IA.D5). We construct bootstrapped yields, Y_t^b , as follows:

$$Y_t^b = U_{\mathcal{M}} \cdot PC_{1-3:t}^b + \eta_t^b$$

where $PC_{1-3;t}^b$ denotes the vector of three bootstrapped PCs. Following BH, η_t^b is generated from $MVN(0, \sigma^2 I)$, where σ is set to the sample standard deviation of the ting errors $\hat{\varepsilon}_t$ (pooled across maturities). IA.12 Finally, excess bond returns are calculated using bootstrapped yields.

IA.D.4 Finite Sample Analysis Using the VAR-based DGP

What if the above VAR bootstrap design is used to examine the nite-sample properties of the regression in Eq. (1) in tests of H_0^{S1} ? To answer this question, we examine nite-sample distributions of regression statistics in testing H_0^{S1} :

$$rx_{t;t+12}^{(12n)} = \alpha + \beta_p^{\ell} PC_{1-3;t}^{\ell} + \beta_g G_t + e_{t+12}.$$
 (IA.D10)

Table IA.D1 reports the results. A comparison of panels A1{B2 of the table with their counterparts in Table 3 based on model SM(2,3) reveals that the VAR-based bootstrap still understates the size distortions in the regression in Eq. (IA.D10). Indeed, the 5% critical values implied by model SM(2,3) are more than twice as great as those implied by the VAR-based model for most statistics/maturities. The discrepancy between these two DGPs is substantial in both in-sample and out-of-sample analyses and especially glaring in the coe-cients of determination. For instance, panel A1 of Table IA.D1 indicates that the upper bound of the 95% con-dence interval for R^2 is around 3.3%, but this upper bound is merely comparable to the median of the SM(2,3)-implied distributions. More precisely, the VAR-based 5% critical value has a true size of up to 46%, implying that the nite-sample test based on the VAR bootstrap design would reject the null more than eight times as often as it should.

For completeness, panels A3{B4 of Table IA.D1 report the nite-sample distributions implied IA.12We nd that replacing these simulated measurement errors with the ones bootstrapped from the actual (maturity-speci c) tting errors has only marginal impact on the nite-sample distributions. by the macro-independent model MIM(3,4). As expected, they closely resemble their VAR-based counterparts illustrated in panels A1{B2 of the table. Namely, both MIM(3,4) and the VAR-based DGP di er sharply from spanned MTSMs and lead to in ated rejection rates in tests of H_0^{S1} .

To summarize, in our case, nite-sample tests of H_0^{S1} using the VAR-based DGP is actually oversized and thus biased against the null hypothesis. In contrast, the spanned MTSM specified in Section 5.2.2 provides a more relevant and robust test of H_0^{S1} in nite sample analysis.

IA.E Ibragimov-Muller Tests of Spanning Hypotheses I and II

This section conducts an alternative and robust test of H_0^{S1} and H_0^{S2} , drawing an inference about the hypotheses based on the test developed by Ibragimov and Muller (2010; IM hereinafter).

It is known that standard heteroscedasticity and autocorrelation consistent (HAC) corrections perform poorly in small samples. The IM test can improve the performance of these procedures by not relying on consistency of the given variance estimator. In IM's approach, regression coe-cients β are estimated q times on q subsets of the whole sample. IM prove that, for each coe-cient β_i , the t-statistic computed from the q estimates of $\hat{\beta}_i$ has approximately the same distribution as a standard t-statistic computed from independent and zero-mean Gaussian variables. Muller (2014a) nds that the IM test has outstanding size and power properties in the presence of strongly autocorrelated of regression disturbances. Muller (2014b) further notes that the IM test is an \attractive choice" for predictive regression problem and is also robust to structural breaks.

Following Meller (2014a), we divide the whole sample into q nonoverlapping consecutive blocks of (approximately) equal length, with q=8 or 16. Table IA.E1 reports the p-values of the resultant t-tests of both H_0^{S1} and H_0^{S2} , for both the full and post-1984 samples. As the IM test assumes the independence of blocks, we insert 12-month gaps between adjacent blocks in the full-sample analysis. As such, the regression coe-cients estimated from di-erent blocks of data are arguably independent from each other. For brevity, we report the testing results for the average excess bond return only, which is over two-through four-year (ten-year) maturities for the 1964{2014 (1985{2014}) sample, as maturity-speci-c estimates for each of q sample subsets are rather noisy. While the evidence on $PC_{2;t}^o$ (the \slope" factor) is consist with BH, $PC_{1;t}^o$ (the \level" factor) becomes insigni-cant in the post-1984 sample when $Z_t = \widehat{G}_t$ (the SAGLasso factor). However, even the

strong evidence for the predictive power of $PC_{2;t}^o$ is tempered when we consider H_0^{S2} : its p-value skyrockets to 0.33 and 0.38 in the full and post-1984 samples, respectively. In contrast, the p-values of \hat{G}_t are uniformly lower than 0.05 for both H_0^{S1} and H_0^{S2} , regardless of the choice of q.

Overall, the IM tests indicate that among the ve yield curve factors and the macro factor \hat{G}_t , the latter is the only robust predictor of future excess bond returns at the 5% signicance level.

IA.F An Alternative Version of Spanning Hypothesis II

In the tests of H_0^{S2} conducted so far, the yield-curve factors used in the hypothesis are the rst ve principal components (PCs) of the noise-uncontaminated yield curve. As mentioned in Section 2.2, including the higher-order PCs is motivated by the notion of hidden factors a la Du ee (2011). This section introduces and tests another version of H_0^{S2} that is based on an alternative set of the yield-curve factors, the \cycle" factor (\widehat{cf}) of Cieslak and Povala (2015). As noted in Cieslak and Povala (2015), the cycle factor is spanned (see also Cieslak 2018), as well as analogous to the single risk premium factor in Du ee (2011) that contains a hidden component.

Cieslak and Povala (2015) propose an illustrative three-factor dynamic term-structure model (DTSM) in which \widehat{cf} corresponds to a single \risk premium factor" denoted by x_t , where x_t captures all of forecastable variation in one-year expected excess returns for bonds of all maturities. While the Cochrane and Piazzesi (2005) factor $\widehat{(CP)}$ plays a similar role in the DTSM proposed in Cochrane and Piazzesi (2008), Cieslak and Povala (2015) demonstrate that their methodology (based on linear projections of yields on trend in ation) is more elective in recovering the variation in risk premiums from noise-contaminated yields and, as a result, \widehat{cf} subsumes \widehat{CP} in predicting excess bond returns. In other words, x_t is analogous to Duilee (2011)'s single risk premium factor, RP_t , that determines the *one-month-ahead* risk premia on all bonds. In particular, x_t contains a hidden component that cannot be detected using the cross-section of yields and that needs to be inferred, say, with a proxy for trend in ation as done in Cieslak and Povala (2015). In this sense, x_t can be regarded as an \annual" version of RP_t and, accordingly, \widehat{cf} maps to the smoothed estimate of RP_t obtained in Duilee (2011). That is, as an estimate of x_t , \widehat{cf} summarizes all information on one-year-ahead risk premia.

 $^{^{\}text{IA.13}}$ The state vector underlying the ve-factor DTSM in Du ee (2011) consists of the rst ve PCs of yield innovations. As a result, RP_t is a linear combination of these ve PCs.

It follows that we can formulate an alternative version of H_0^{S2} using \widehat{cf} as the conditioning variable:

 $H_0^{S2;cf}$: The SAGLasso macro factor \widehat{G} has no additional predictive power for bond risk premia in the presence of \widehat{cf} .

One way to test $H_0^{S2;cf}$ is based on the following predictive regression of excess bond returns:

$$rx_{t;t+12}^{(12n)} = \alpha + \beta_c^{\ell}$$

other. It follows that the P-measure dynamics of the state variables are

$$X_{t} = \mu_{X}^{P} + \begin{bmatrix} \phi^{P} & 0 & 0 & \phi^{P}_{g} \\ 0 & \phi^{P}_{rr} & 0 & \phi^{P}_{rg} \\ 0 & 0 & \phi^{P}_{xx} & \phi^{P}_{xg} \\ \phi^{P}_{x} & \phi^{P}_{gr} & \phi^{P}_{gx} & \phi^{P}_{gg} \end{bmatrix} \times_{t=1} + \begin{bmatrix} \sigma & 0 & 0 & \sigma_{g} \\ 0 & \sigma_{rr} & 0 & \sigma_{rg} \\ 0 & 0 & \sigma_{xx} & \sigma_{xg} \\ \sigma_{x} & \sigma_{gr} & \sigma_{gx} & \sigma_{gg} \end{bmatrix} \epsilon_{x;t}^{P}.$$
 (IA.F13)

Note that the parameter ϕ_{xg}^{P} is important as it determines whether G_t has unconditional predictive power for excess bond returns; if $\phi_{xg}^{P} = 0$, the model in Eq. (IA.F13) degenerates into conformity with Du ee (2007)'s GNH. Under the speci cation in Eq. (IA.F12), G_t contains no *conditional* predictive power when x_t is controlled for, regardless of the value of ϕ_{xg}^{P} .

As, by de nition, the risk-premium factor x_t does not a ect the short rate, we specify the following equation to complete the model:

$$r_t = \delta_0 + \delta_r r_t^r + \delta \tau_t, \tag{IA.F14}$$

where r_t denotes the one-year yield with $\delta_r > 0$ and $\delta_r > 0$.

The MTSM as represented by Eqs. (IA.F12){(IA.F14) is estimated using zero yields with maturities of one through ten years over the full sample period 1971.11{2014.12 (matching the beginning of the sample used in Cieslak and Povala 2015). The estimated model is then used to generate 5,000 bootstrapped data samples.

Table IA.F1 summarizes the nite-sample properties of the six test statistics used that are based on the 5,000 bootstrapped data samples, including the 95th percentile of the bootstrap distribution (underlined as the 5% critical value in the table) and the p-value (in angle brackets) for each test statistic. A comparison of these nite-sample critical values with those (under H_0^{S2}) reported in panels B3 and B4 of Table 3 reveals that the small-sample bias is less severe in the regression in Eq. (IA.F11) than that in Eq. (1) speci ed for testing H_0^{S2} . Consistent with the conclusion drawn from their asymptotic distributions, the bootstrap distributions of all statistics shown in Table IA.F1 overwhelmingly reject the null hypothesis $H_0^{S2;cf}$ that \hat{G}_t contains no predictive power conditioned on \hat{cf}_t at the 5% signic cance level, with the only exception of the ENC-REG test for the 7-year bond for which the small-sample p-value is 6.6%.

To summarize, the above results of tests of the spanning hypothesis $H_0^{S2;\it{cf}}$ provide further

evidence that the SAGLasso macro factor has signi cant, additional predictive power for excess bond returns conditioning on the yield curve information.

IA.G Unspanning Tests and Applications of Unspanned Models

This section focuses on unspanned MTSMs with the SAGLasso factor as the sole macro risk factor. We formally describe the macro-unspanning hypothesis (MUH) in Section 5.3.1 and then investigate its statistical signic cance as well as its economic importance in Sections 5.3.2 through IA.G.2. Lastly, Section IA.G.3 quantiles the information content of the SAGLasso factor.

While the above test results demonstrate the empirical relevance of G_t as an unspanned macro risk, the tests of the MUH per se are more interesting statistically than economically. On the one hand, to be statistically legitimate, the MUH has to be formulated as Eq. (12). On the other hand, the consensus is that, in general, macro variables hold greater promise in helping to improve a term structure model's time-series accuracy than its goodness-of- t (e.g., Du ee (2011) nds that a YTSM(5) is adequate for producing thing errors of 6 bps). Given this insight, a more relevant question to ask is whether using G_t as a pricing factor has any economic bene ts. Put di erently, does an unspanned MTSM with G_t as its sole macro factor provide any added economic value over an otherwise spanned model? As shown below, the answer to these questions depends on whether MTSMs are subject to certain constraints on their model-implied Sharpe ratios.

IA.G.1 Model-Implied Sharpe Ratios

One issue not addressed in the likelihood-ratio tests considered in Section 5.3.2 (as well as in BR) is that the MTSMs under scrutiny impose no constraints on the Sharpe ratio (SR) of bond returns and that such \unconstrained" models may imply unrealistic SRs, as noted in Du ee (2010) and Joslin, Singleton, and Zhu (2011; JSZ hereafter). Speci cally, Du ee documents that while the empirical benchmark for the unconditional maximum SR is 0.15~0.20, SRs implied from unconstrained Gaussian dynamic term structure models in his analysis are much higher than the benchmark.

Untabulated results indicate that among the three spanned MTSMs, $\{SM(\mathcal{L}, \mathcal{N})\}_{3}$ $_{L}$ $_{5}$, considered in panel A of Table 4, even the most \reasonable'' model-implied sample mean (population

mean) of conditional maximum SRs is 0.715 (0.825) when SRs are computed with log returns; the sample mean increases to 1.309 when SRs are computed with simple returns. Consistent with Du ee (2010), we not that the model-implied SRs increase with the model dimension. For model SM(5,6), the sample mean of the maximum conditional SRs could even be higher than 10^{35} (for simple returns), an obviously unplausible level. As such, though statistically appealing, the test results presented in panel A of Table 4 are based on misspeci ed models.

One way to ensure that an MTSM generates plausible SRs is to directly impose restrictions on risk premia, say, that only the level and slope risks be priced (a restriction suggested by Du ee 2010 and implemented in Du ee 2011). Another way is to let the data decide what restrictions are empirically relevant. We implement the latter approach by following JPS to search for the best zero restrictions on risk premium parameters $\{\lambda_0, \lambda_1\}$ that minimize the Bayesian information criterion (note that t essentially represents SRs of bond portfolios with payo s that track the pricing factors). The resultant models selected by this approach (see Internet Appendix IA.C.2) all possess the following two properties: (a) variations in expected excess bond returns are mainly driven by two factors and, (b) the SAGLasso factor plays a signi cant role in both term-premium factors. Importantly, conditional maximum SRs implied by these selected models are generally in line with those observed empirically. For convenience, the MTSMs with the selected zero restrictions on $\{\lambda_0, \lambda_1\}$ are referred to as constrained MTSMs and denoted by $CSM(\mathcal{L}, \mathcal{N})$ ($CUSM(\mathcal{L}, \mathcal{N})$) for spanned (unspanned) models, with \mathcal{L} being the number of yield factors included in the model.

With model selections performed on market prices of risk, unspanned and spanned models are no longer nested, however, and as a result, the LR test-based statistical inference made in Section 5.3.2 no longer applies. Nonetheless, as shown below we can still measure the economic values of the macro-unspanning restrictions imposed on constrained models.

IA.G.2 Out-of-Sample Forecasts of Bond Yields

This subsection investigates whether it is bene cial to include the SAGLasso factor as unspanned by the yield curve in an MTSM. We consider MTSMs with and without the macro-unspanning restrictions and examine whether these restrictions help to forecast future bond yields. We seek to

 $^{^{\}text{IA.15}}$ Untabulated results indicate that this problem persists in MTSMs tested by BR, in which our SAGLasso factor is replaced with (GRO, INF), two macro factors often used in this literature.

quantify the e ectiveness of these restrictions as forecasting tools.

We focus on six-factor models in this analysis given Du ee's (2011) argument that ve yield factors summarize all information (in both the time series and cross section) in the yield curve. Regardless, including at least ve yield factors instead of three makes it harder to see the importance of the macro-unspanning restrictions.

The procedure is similar to the out-of-sample analysis in Section 4.4.2. However, since recursive estimation of MTSMs is computationally very costly (especially for models CSM(5,6) and CUSM(5,6), which require model selection for the risk premium), our yield forecasts are formed based on model estimates for the 1985{2007 sample. With the model parameters xed, we re Iter yield factors using observations up to month $t \geq 2007.12$ and then construct forecasts of the T-year bond yield in month-(t + h), where T = 0.5, 1, 3, 5, 7, 10 and h = 1, 3, 6, 12 in our empirical analysis. The out-of-sample (test) period extends from January 2008 to December 2013.

Panel A of Table IA.G1 reports the root mean squared forecast error (RMSE) produced by unconstrained models SM(5,6) and USM(5,6) for each of 24 combinations of T and h. Note that the models deliver closely comparable forecasting performance, especially at short horizons. This inding is not surprising, given that they should produce identical yield forecasts if $PC_{1-5:t}$ is assumed to be observed without error (see Section 4.2 of JSZ). Although our assumption that all bonds (and portfolios) are priced imperfectly prevents us from exploiting the JSZ-type separation of parameters in the likelihood function, the assumption allows the macro-unspanning restrictions to a ect the Itering process and thus the model estimations. As indicated by our empirical results, this impact makes a sizable difference only at the one-year horizon, where USM(5,6) provides more accurate forecasts at the short end of the yield curve but is outperformed by SM(5,6) at the long end. Nonetheless, recall that both SM(5,6) and USM(5,6) generate unrealistic model-implied SRs.

Panel B of Table IA.G1 shows the results from constrained models CSM(5,6) and CUSM(5,6). They too have similar forecasting performance when the forecast horizon is short with h=1,3 (month). However, when h=6 or 12, CUSM(5,6) signi cantly outperforms CSM(5,6), especially for the 1-year and longer maturity yields. For example, when h=12, the unspanning restrictions reduce the forecast error by as much as 30 bps for the 3-year yield or 40 bps for the 7-year yield. That is, the improvements in forecasting performance owing to an unspanned \widehat{G} are much more robust once certain zero restrictions on t are imposed. To decipher the discrepancy between these two

pairs of models, we examine the model-implied P-dynamics. As discussed by JPS (in their Section IV.B), enforcing zero restrictions on their risk premium parameters increases the persistence of state variables. We con rm this inding by noting that the eigenvalues of $_{X}^{P}$ in CUSM(5,6) are substantially larger than their counterparts in CSM(5,6). This increase prevents variations in risk premia from completely dominating short-rate expectations and makes model-implied long-dated yield expectations more reasonable and potentially closer to the \true" yield expectations.

Taking the above indings together with the LR test results presented in Section 5.3.2, we conclude that by making the model more parsimonious, the macro-unspanning restrictions do not hurt the in-sample ting and thus boost the out-of-sample performance.

IA.G.3 Forecastable Variations in Excess Returns Attributable to G_t

Having explored the unspanned nature of G_t , we quantify the information content in G_t within a (G-based) MTSM. Speci cally, we examine how much of the predictable variations in excess bond returns can be captured by G_t and the potential role of hidden yield factors in the model. Put di erently, we examine how much information related to the bond risk premium may be lost by excluding unspanned macro risks from term structure modeling. Note that this exercise represents an MTSM-based version of the regression analysis conducted in Section IA.B.5.

To this end, we consider the constrained models only (because this exercise requires reasonable model-implied moments of risk premia), and focus on the unspanned models.^{IA.16} We implement models $CUSM(\mathcal{L}, \mathcal{N})$ for $\mathcal{L}=3,4,5$.

IA.G.3.1 Variance Decomposition for Excess Bond Returns

We discuss the population properties of annual excess bond returns. Results reported in Table IA.G2 cover the ve-year bond only as it is closely related to the \in-four-years-for-one-year" forward premium, as shown in the following:

$$E_t\left(rx_{t+12}^{(60)}\right) = FP_t^{4,1} - 4E_t\left(y_{t+12}^{48}\right) + \left(E_t(y_{t+48}^{(12)}) - y_t^{(12)}\right).$$

But the results for other maturities are broadly similar.

^{IA.16}Although the macro-unspanning restrictions tend to grant macro factors the \privilege" of retaining their contributions to term premia, this is less of an issue here given that G_t is constructed after controlling for the yield curve information. Regardless, the spanned models generate qualitatively similar results (untabulated).

Consider the model CUSM(3,4) rst. Its model-implied unconditional mean of excess bond returns is 2.85% (column 2), consistent with its data counterpart of 2.73% (untabulated). The unconditional variance is 58.25 (column 3) and calculated using the following formula:

$$\text{Var}\left(rx_{t:t+12}^{(60)}\right) = \psi^{\emptyset} \text{Var}(X_t) \psi + 48^2 \left[\sum_{i=0}^{11} B_{48}^{\emptyset} \quad ^i \quad ^{\emptyset} B_{48}\right] + (5^2 + 4^2 + 1) \sigma_y^2, \text{(IA.G15)}$$
 where $\psi = 60 B_{60}^{\emptyset} - 48 B_{48}^{\emptyset} \quad ^{12} - 12 B_{12}^{\emptyset}.$

Among the three terms on the right-hand side (RHS) of Eq. (IA.G15), the rst one represents the unconditional variance of the conditional expectation, which quantities forecastable variation in the excess bond return; the second term denotes the variance of shocks to the \true" excess return; and the last term is the variance of the measurement error's contribution to the observed return shocks. Since this last term is typically small in models with $\mathcal{N} \geq 3$, the predictability of bond returns is mainly determined by the relative magnitudes of the rst two terms on the RHS.

Furthermore, how much of $\operatorname{Var}\left(rx_{t;t+12}^{(60)}\right)$ is forecastable depends on the conditioning information used to forecast. If the state vector X_t itself is used, then the full-information R^2 implied by $\operatorname{CUSM}(3,4)$ is 0.463 (the ratio of 27.01 in column 4 to 58.25), comparable to the regression R^2 of 0.439 reported in Table IA.B6 (column 7). The full-information R^2 , however, cannot be achieved when the conditioning variables consist of the rst $\mathcal{R} (\leq \mathcal{L})$ PCs of observed yields only. An elective measure for the gap between the information contained in X_t and that in $\operatorname{PC}_{1-R;t}^o$ is the following ratio of variances of these two relevant forecasts:

$$VR_{R}^{o} = \frac{\psi^{\emptyset} \operatorname{Var}(X_{t} | PC_{1-R;t}^{o})\psi}{\psi^{\emptyset} \operatorname{Var}(X_{t})\psi}, \quad \mathcal{R} \leq \mathcal{L}.$$
 (IA.G16)

If $\mathcal{R}=3$, then CUSM(3,4) implies a $VR_{\mathcal{R}}^o$ of 71.4% (Table IA.G2, column 5 in braces); that is, almost 30% of the information in X_t is lost if we ignore G_t and rely solely on $PC_{1-3;t}^o$ to infer term premia. IA.17

What happens if the rst \mathcal{R} ($\leq \mathcal{L}$) PCs of the *true* yields are used as the conditioning variables? We can repeat the above analysis using the following variant of Eq. (IA.G16):

$$VR_{R} = \frac{\psi^{\theta} \operatorname{Var}(X_{t}|PC_{1-R;t})\psi}{\psi^{\theta} \operatorname{Var}(X_{t})\psi}.$$
 (IA.G17)

Column 6 shows that VR_3 is 72.9% (in braces), only slightly greater than VR_3^0 (71.4%). This is

 $[\]overline{^{1A.17}}$ Du ee (2011) uses $\overline{VR_R^o}$ to evaluate the importance of yield factors hidden from the contemporaneous term structure and nds that PC_1^o $_{3/t}$ recover only 70% of the information on expected excess returns on the ve-year bond, consistent with the notion of hidden factors.

not surprising as the cross-sectional e ect of $PC_{1-3;t}$ is supposedly large enough to dominate the measurement error. Obviously, if the conditioning variables are X_t , the variance ratio is 100% (column 9). Notice that because $\mathcal{R} = \mathcal{L} = 3$, results from CUSM(3,4) in columns 7 and 8 are the same as those in columns 5 and 6.

Given that model CUSM(3,4) leaves no room for hidden yield factors, we consider the higher-dimensional models ($\mathcal{L}>3$) next. As expected, in such cases the information loss will be higher (than with $\mathcal{L}=3$) if the conditioning information consists of $PC_{1-3;t}^o$ only. As shown in column 5, VR_3^o is about 71% under CUSM(4,5) and 65% under CUSM(5,6) (a model that is supposed to encompass both unspanned yield and macro factors). That is, about one-third of the information in X_t is lost if only $PC_{1-3;t}^o$ are used to infer term premia under CUSM(5,6). As before, replacing $PC_{1-3;t}^o$ with $PC_{1-3;t}^o$ hardly reduces the information lost, with VR_3 equal to 71.3% under CUSM(4,5) and 67.2% under CUSM(5,6) (column 6). Note from column 7 that including higher-order PCs of the *observed* yield curve, $PC_{4;t}^o$ and $PC_{5;t}^o$, in the conditioning variables hardly helps to dig up more information on risk premia. For instance, for CUSM(5,6), $VR_5^o = 65.1\%$ (column 7), only slightly higher than $VR_3^o = 64.9\%$ (column 5). Again, this is because the cross-sectional e ect of higher-order PCs is too small to overwhelm the measurement error.

If we can *perfectly* infer the hidden factors by extracting information from yield dynamics as well as in the cross section, we can estimate risk premia more accurately. For instance, under model CUSM(5,6), $VR_5=75.8\%$ (column 8), much higher than either $VR_5^0=65.1\%$ (column 7) or $VR_3=67.2\%$ (column 6). In fact, this dierence between VR_5^0 and VR_5 suggests a wedge between the information in observed yields and that in \true" yields, whereas there is no evidence for a similar gap for the rist three PCs, as indicated by columns 5 and 6. Nonetheless, the VR_5 of 75.8% still implies an information loss of almost 25% even in this ideal case. Given that under model CUSM(5,6), G_t is not spanned by $PC_{1-6,t}$ and that the velyield factors presumably summarize all (time-series and cross-sectional) information on the yield side (Duee 2011), a more reasonable implication of the result that $VR_5=75.8\%$ is the following: The information loss is at least about one-quarter when G_t is excluded from return predictors, even though they include $PC_{1-5,t}$.

We use the phrase \hat{C}_1 for two reasons: First, the variance ratio is computed under the assumption that PC_1 $_{5;t}$ are perfectly observable. In practice, however, econometricians have to perform. Itering analysis to infer PC_4 $_{5;t}$. Du ee (2011) documents that the Kalman. Iter recovers

only two-thirds of the information in the true state vector for monthly excess returns (and about 82% of that for annual excess returns in an earlier version of the paper). In contrast, measurement error has little impact on factor G_t . Second, the period 1985{2007 sample is special in the sense that the fraction of the total variance attributable to macro-driven variations is particularly low. If the estimation sample is extended to either 1964 or 2014, the model-implied variance ratio would drop below 67% (untabulated). Once these two facts are taken into account, the results from model-based risk premium decomposition are expected to be close to the test results of H_0^{S2} (columns 14{17 in Table IA.B6) | namely, with respect to the state vector $X_t = (PC_{1-5,t}, G_t)$, the SAGLasso factor accounts for almost half of the predictable variations in excess bond returns.

It is worth emphasizing that risk premium accounting based on variance ratios is analogous to the variance decomposition (in the context of reduced-form VARs), of which the results are sensitive to the order of state factors chosen for identication. The projection of G_t on PC_1 $_{L;t}$ in VR_L maximizes the explanatory power of yield PCs (Bikbov and Chernov 2010). This point can be illustrated by changing the order of state factors and calculating the following variance ratio:

$$VR_{3+G} = \frac{\psi^{\ell} \text{Var}(X_t | X_t^{nH}) \psi}{\psi^{\ell} \text{Var}(X_t) \psi}, \tag{IA.G18}$$

where $X_t^{nH} = (PC_{1-3;t}, G_t)$. Results in column 9 indicate that under CUSM(5,6), the rst three PCs plus the SAGLasso factor capture 97.9% of forecastable variation in excess bond returns. Although this inding does not necessarily mean that hidden factors are unimportant in return prediction in this case, it does imply that, compared to ignoring hidden yield factors (as shown in column 9), excluding unspanned macro risks (associated with G_t , as shown in column 8) bears more serious economic consequences in the inference of term premia.

IA.G.3.2 Calculations of Variance Ratios

This subsection provides details on the calculations of variance ratios used in Section IA.G.3.1. All the calculations are based on MTSMs speci ed in either Section 5.2 (for spanned models) or Section IA.G (for unspanned ones).

Consider $VR_{\mathcal{R}}^o$, the variance ratio de ned in Eq. (IA.G16) that focuses on the forecast of excess bond returns based on the rst \mathcal{R} ($\leq \mathcal{L}$) PCs of observed yields. Recall that by de nition, the rst

 \mathcal{L} PCs are given by

$$PC_1^0$$
 $L:t = W_{R:M}Y_t^0 = W_{R:M}A_M + W_{R:M}B_M^0X_t + W_{R:M}\eta_t$

where $W_{R;\mathcal{M}}$ is an $\mathcal{R} \times k$ loading matrix, which is equal to the transpose of $U_{R;\mathcal{M}}$ in Eq. (IA.D4). Below subscripts are suppressed for simplicity of notations. It follows that the expectation of the true state factor X_t conditioned on these PCs equals

$$E(X_t|PC_{1-R;t}^0) = E(X_t) + Var(X_t)BW^0 Var(PC_{1-R;t}^0)^{-1}PC_{1-R;t}^0$$

where the variance of $PC_{1-R;t}^{o}$ is

$$Var(PC_1^0|_{R:t}) = WB^{\ell}Var(X_t)BW + WW^{\ell}\sigma^2.$$

The variance of $E(X_t|PC_1^o|_{R;t})$ is

$$Var(X_t|PC_{1-R:t}^0) = Var(X_t)\mathcal{B}W^{\ell}Var(PC_{1-R:t}^0)^{-1}W\mathcal{B}^{\ell}Var(X_t).$$

Next, consider VR_R , the variance ratio specified in Eq. (IA.G17) that concerns the inference of risk premium based on the rst R PCs of true yields. Recall that these PCs, $PC_{1-R;t}$, constitute a segment of the state vector X_t . Denoting the remaining N-R state factors by X_t^{nR} , we have

$$E(X_t|PC_{1\ R;t}) = \begin{bmatrix} PC_{1\ R;t} \\ E(X_t^{nR}) + CV^{-1}PC_{1\ R;t} \end{bmatrix}, \text{ and}$$

$$Var(X_t|PC_{1\ R;t}) = \begin{bmatrix} V & C^{\ell} \\ C & CV^{-1}C^{\ell} \end{bmatrix},$$

where $V = Var(PC_1 | R_t)$ and $C = Cov(X_t^{nR}, PC_1 | R_t)$.

Table IA.A1: Properties of Principal Components of Observed Yield Curves

Panel A reports correlations between principal components (PCs) of observed yields and Itered estimates of yield PCs, denoted by PC_i^o and PC_i , respectively, where $i=1,\ldots,5$. Population correlations are computed by simulating 100,000 months of bond yields. The 95% con dence intervals for the sample correlations, as displayed in parentheses, are derived from 5,000 simulations with the same number of observations as in the data sample. The yield maturities in all simulations are three months and one through ve years. Panel B reports results from regressions of the return to an n-year zero-coupon bond from month t to month t+12 less the month-t yield on a one-year bond on the rst ve PCs of observed yields, PC_1^o $_5 = (PC_1^o, \ldots, PC_5^o)$. Test statistics are computed using either the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses) or the Newey and West (1987) HAC covariance estimator (in brackets). The row labeled R^0 (Table 2)" copies the R^0 values from regressions of excess returns on Itered estimates of the rst ve PCs, reported in Table IA.B5 (columns 10 through 13). The R^0 measure represents the di erences between R^0 values in Panel B and R^0 (Table 2). The last row in panel B reports the percentage decrease in the R^0 . The sample spans the period January 1964 to December 2014.

(1)	(2)	(;	3)	(4)	(5)	(6)	(7)
	Panel A: Co	$prr(PC_{i,t},PC_{i,t})$	$PC_{i,t}^o$			-	s of excess returns I on $PC_{1-5,t}^{o}$
					Bon	d maturity	n
	Population	San	nple	2	3	4	5
$PC_{1,t}^o$	0.9999	0.9	998	3.526	3.031	2.080	0.422
2,0		[0.9998	0.9999]	(1.116)	(0.529)	(0.264)	(0.043)
				[1.266]	[0.601]	[0.300]	[0.048]
$PC_{2,t}^o$	0.9905	0.9	902	-0.688	-1.330	-2.038	-2.621
		[0.9885	0.9916]	(-3.650)	(-3.674)	(-3.961)	(-4.105)
				[-4.021]	[-4.092]	[-4.431]	[-4.601]
$PC_{3,t}^o$	0.9612	0.9	818	0.784	1.011	1.485	1.688
		[0.9787	0.9845]	(1.233)	(0.920)	(1.041)	(0.978)
				[1.384]	[1.034]	[1.156]	[1.079]
$PC_{4,t}^o$	0.7233	0.7	595	-1.956	-2.836	-2.798	-0.961
		[0.7238	0.7912]	(-1.702)	(-1.295)	(-0.910)	(-0.244)
				[-1.842]	[-1.418]	[-1.005]	[-0.271]
$PC_{5,t}^o$	0.2125	0.6	107	4.060	10.521	15.004	14.677
		[0.5584	0.6581]	(2.693)	(4.536)	(5.636)	(4.358)
				[2.363]	[3.620]	[4.074]	[3.151]
			R^2	0.205	0.215	0.241	0.228
			R^2 (Table IA.B5)	0.221	0.233	0.255	0.245
			R^2	-0.016	-0.018	-0.014	-0.017
		Percent	age decrease in \mathbb{R}^2	-7.24%	-7.73%	-5.49%	-6.94%

Table IA.B1: Correlation between Yield Curve and New Macro Factors

This table reports the Pearson correlation coe cients between four newly constructed macroeconomic factors and ve yield-curve factors. The four macroeconomic factors include employment (\hat{g}_{1t}) , housing (\hat{g}_{2t}) , in ation (\hat{g}_{3t}) , and the aggregate SAGLasso factor (\hat{G}_t) constructed in Section 4.2. The ve yield curve factors include the rst three principal components (PCs) of *observed* bond yields, $\{PC_{1;t}^o, i=1,2,3\}$, and the Itered higher-order PCs of noise-uncontaminated yields, $PC_{4;t}$ and $PC_{5;t}$. The sample spans the period January 1964 to December 2014.

	\widehat{G}_t	\widehat{G}_{1t}	\widehat{G}_{2t}	\widehat{G}_{3t}	PC 0 1;t	$PC_{2;t}^o$	$PC_{3;t}^o$	PC _{4;t}
\widehat{G}_{1t} \widehat{G}_{2t}	0.620							
	0.527	0.577						
\widehat{G}_{3t}	0.524	0.467	0.351					
$PC_{1:t}^o$	-0.100	-0.226	-0.167	-0.199				
$PC_{2;t}^o$	-0.352	-0.222	-0.073	-0.270	-0.006			
$PC_{3;t}^o$	0.167	0.239	0.222	0.196	0.018	0.003		
$PC_{4;t}$	-0.094	-0.031	-0.106	0.021	-0.000	0.013	0.044	
$PC_{5;t}$	-0.021	-0.027	-0.282	0.284	0.024	0.008	-0.011	0.092

Table IA.B2: Predictive Power of Three SAGLasso Group Factors

The return to an n-year zero-coupon bond from month t to month t + 12 less the month-t yield on a one-year bond is regressed on \hat{g}_{1t} , \hat{g}_{2t} , and \hat{g}_{3t} , the group factors, constructed in Section 4.2, that represent employment, housing and in ation, respectively, for n = 2, ..., 5. Results reported in panel A are based on the January 1964 (December 2014 sample, including those from both univariate (panel A1) and multivariate predictive regressions (panel A2). Results reported in panel B are based on the January 1952{December 2014 sample, where only the employment factor is considered (because of data limitations) and constructed using this longer sample (\widehat{g}_{1t}) . In-sample results from regressions on \hat{g}_{1t} are shown in panel B1 and out-of-sample (OOS) results based on \widetilde{g}_{1t} are reported in panel B2. Test statistics are computed using either the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses) or the Newey and West (1987) HAC covariance estimator (in brackets). The ENC-REG statistic denotes the OOS t-statistic proposed by Ericsson (1992), whose 95th percentile of the asymptotic distribution is $^{1} = 1.645$. The row labeled \ENC-NEW" reports a variant of the ENC-REG statistic proposed by Clark and McCracken (2001); their simulation shows that the 95% critical value is around 1.584 for testing one additional predictor. Both tests share the same null hypothesis that the benchmark model encompasses the unrestricted model with excess predictors. The R_{oos}^2 statistic denotes the OOS R^2 of Campbell and Thompson (2008).

maturity <i>n</i> (year)	2	3	4	5		2	3	4	5
				Panel A: S	Sample period	1964{201	4		
	Panel A	1: Univar	iate Regre	ssions		Panel A	2: Multiva	ariate Reg	ressions
\widehat{g}_{1t}	0.828 (3.796)	1.526 (4.149)	2.082 (4.272)	2.568 (4.545)		0.942 (2.850)	1.401 (3.040)	1.744 (3.038)	2.062 (3.165)
R^2	0.220	[4.594] 0.222	[4.689] 0.213	[4.948] 0.211	-	[3.107]	[3.301]	[3.280]	[3.401]
\widehat{g}_{2t}	0.643 (2.608) [2.969]	1.162 (2.861) [3.249]	1.631 (3.178) [3.589]	2.051 (3.364) [3.786]		0.722 (1.965) [2.141]	0.968 (2.052) [2.236]	1.223 (2.215) [2.413]	1.461 (2.321) [2.528]
R^2	0.143	0.139	0.141	0.149	_	[2]	[2.200]	[2.110]	[2.020]
\widehat{g}_{3t}	0.723 (3.096) [3.449]	1.358 (3.075) [3.431]	1.872 (3.023) [3.380]	2.222 (2.875) [3.215]		0.847 (2.544) [2.754]	1.249 (2.534) [2.748]	1.574 (2.486) [2.698]	1.763 (2.358) [2.555]
R^2	0.168	0.176	0.172	0.173		0.404	0.431	0.420	0.417
				Panel B: S	Sample period	1952{201	4		
	Panel B	1: In-Sam	ple Regres	ssions		Panel B	2: \widetilde{g}_{1t}^* vs.	constant	(OOS)
\widehat{g}_{1t}^*	0.751 (4.161)	1.397 (4.524)	1.932 (4.767)	2.390 (5.084)	ENC-REG	3.329	3.600	3.719	3.991
R^2	[4.665] 0.206	[5.025] 0.213	[5.227] 0.211	[5.525] 0.211	ENC-NEW R_{oos}^2	136.93 0.155	134.56 0.164	127.99 0.166	125.341 0.169

Table IA.B3: Unspanned Variation in SAGLasso Group Factors

This table reports results from linear projections of each of the three SAGLasso group macro factors $\{\widehat{g}_{it},1\leq i\leq 3\}$ onto the rst \mathcal{R} principal components (PCs) of the yield curve $(PC_{1}^{o}_{\mathcal{R};t})$, where $\mathcal{R}=3$ (panel A) or 6 (panel B) and the group factors are the employment (\widehat{g}_{1t}) , housing (\widehat{g}_{2t}) , and in ation (\widehat{g}_{3t}) factors. Columns 3 and 5 show the regression R^2 s, and in brackets beneath are reported 95% con dence intervals based on 5,000 articial samples simulated from a six-factor constrained term structure model with spanned macro risks. The state vector of the model, denoted by $CSM(3,6)_{group}$ and specified in Section IA.G.1, includes three yield curve factors (the rst three PCs) and three macro factors, \widehat{g}_{1t} , \widehat{g}_{2t} , and \widehat{g}_{3t} . Column 2 indicates whether the three macro variables are assumed to be measured with errors in the estimation of model $CSM(3,6)_{group}$. Columns 4 and 6 report the rst-order serial correlation of regression residuals.

(1)	(2)	(3)	(4)	(!	5)	(6)
Dependent	Macro	Panel A		\widehat{g}_{it} on $PC^o_{1-3,t}$	Panel E Regress		\widehat{g}_{it} on $PC_{1-6,t}^o$
variable	Measure- ment Error	I	\mathbb{R}^2	AR(1) of residuals		\mathbb{R}^2	AR(1) of residuals
\widehat{g}_{1t}		0.1	116		0.1	125	
	No	[0.148	0.770]		[0.206	0.809]	
	Yes	[0.140	0.773]	0.951	[0.201	0.814]	0.948
\widehat{g}_{2t}		0.0	082		0.1	119	
	No	[0.144	0.816]		[0.171	0.845]	
	Yes	[0.137	0.802]	0.960	[0.164	0.829]	0.946
\widehat{g}_{3t}		0.1	106		0.1	123	
-	No	[0.152	0.708]		[0.219	0.766]	
	Yes	[0.145	0.697]	0.903	[0.216	0.753]	0.893

Table IA.B4: Predictive Power of Alternative Macroeconomic Factors for Excess Bond Returns

The return to an n-year zero-coupon bond from month t to month t+12 less the month-t yield on a one-year bond is regressed of 131 macro series that are not adjusted for data revisions, and a factor denoted $\widehat{G}_{\mathrm{r}}^{\mathrm{rev,lag}}$ (panel C) and constructed using the labeled NENC-REG" reports the out-of-sample t-statistics proposed by Ericsson (1992), whose 95th percentile of the asymptotic distribution is $^{-1}$ = 1.645. The row labeled NENC-NEW" reports a variant of the ENC-REG statistic proposed by Clark and McCracken (2001); their simulation shows that the 95% critical value is around 1.584 for testing one additional predictor. Both tests share the same null hypothesis that the benchmark model encompasses the unrestricted model with excess predictors. The row labeled $\backslash R_{\rm oos}^2$ " denotes the out-of-sample R^2 of Campbell and Thompson (2008). The sample spans the period January 1964 on a macro factor (F_t) , for $n=2,\ldots,5$. The three macro factors considered include the modi ed Ludvigson and Ng (2011) factor, $\widehat{LN}_{\rm t}^{\rm m}$ (panel A); a factor denoted $\widehat{G}_{\rm t}^{\rm rev}$ (panel B) and constructed using the SAGLasso procedure (Section 4.1) albeit with the set SAGLasso procedure albeit with the set of 131 macro series that are not adjusted for either data revisions or publication lags. In the in-sample analysis, t-statistics are computed using the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses) and the Newey and West (1987) HAC covariance estimator (in brackets), respectively. In the out-of-sample analysis, the row to December 2014.

	Predi	ctive regr	essions of	excess re	turns to a	an n -year	Predictive regressions of excess returns to an n -year zero-coupon bond on alternative macro factors $(F_{ m t})$	puod uod	on altern	ative mad	ro factors	(F_{t})
	т.	Panel A: $F_{\rm t}=\widehat{LN}_{\rm t}^{\rm m}$	$r_{\rm t} = \widehat{LN}_{\rm t}^{\rm m}$	_		Panel B:	Panel B: $F_{ m t}=\widehat{G}_{ m t}^{ m rev}$		Ą,	Panel C: $F_{ m t}=\widehat{G}_{ m t}^{ m rev;lag}$	$=\widehat{G}_{t}^{rev;lg}$	<u>6</u>
maturity n (year)	2	က	4	വ	5	ю	4	വ	5	က	4	വ
	Panel A	Panel A1: In-sample	ple		Panel B	Panel B1: In-sample	ple		Panel C	Panel C1: In-sample	ple	
Coe , on $F_{ m t}$	0.724 (4.227)	1.473 (4.932)	2.181 (5.804)	2.792 (6.554)	1.039 (5.780)	1.039 1.993 (5.780) (6.357)	2.832 (6.715)	3.542 (7.009)	1.135 (6.023)	2.150 (6.412)	3.037 (6.681)	3.807 (7.102)
R^2	[4.641] 0.168	[5.390] 0.207	[6.319] 0.234		[6.215] 0.347	[6.215] [6.802] 0.347 0.379	[7.191] 0.394	[7.513] 0.402	[6.547] 0.414	[6.547] [6.946] 0.414 0.441	[7.183] 0.453	[7.595] 0.464
	Panel A	Panel A2: Out-of-sample	-sample		Panel B.	Panel B2: Out-of-sample	-sample		Panel C	Panel C2: Out-of-sample	-sample	
ENC-REG ENC-NEW $R_{\rm cos}^2$	2.660 115.96 0.051	3.336 4.136 137.06 162.59 0.112 0.186	4.136 162.59 0.186	5.104 173.71 0.225	3.867 159.78 0.118	4.975 182.11 0.200	5.933 207.94 0.274	7.266 219.67 0.314	4.308 204.64 0.123	5.217 235.34 0.238	5.647 253.81 0.294	6.558 262.21 0.326

Table IA.B5: In-Sample Tests of Spanning Hypotheses I and II: 1964{2014

The return to an n-year zero-coupon bond from month t to month t+12 less the month-t yield on a one-year bond is regressed respectively on (i) the rst three principal components (PCs) of observed bond yields PC $_{1/3,t}$ (columns 2-5); (ii) PC $_{1/3,t}$ and the SAGLasso macro factor \widehat{G}_{t} (columns 6-9); (iii) the Itered rst ve PCs of noise-uncontaminated yields PC $_{1/5,t}$ (columns 10-13); and (iv) PC $_{1/5,t}$ and \widehat{G}_{t} (columns 14-17). Test statistics are computed using the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses), or the Newey and West (1987) HAC covariance estimator (in barentheses). January 1964 to December 2014.

(1)	(2)	(3)	(4)	(5)	(9)	(7)	(8)	(6)	(10)	(11)	(12)	(13)	(14)	(15)	(16)	(17)
					Spa	Spanning Hypothesis	oothesis I						Spa	Spanning Hypothesis	othesis II	
maturity n (year)	2	က	4	22	2	ж	4	2	2	8	4	2	2	ю	4	22
P1t	3:636	3:286		0:738	5:512	6:774	7:176	6:535	2:193	2:163	1:918	1:216	3:034	3:713	4:020	3:777
	(1:106)	(0.533)	(0.285)	(0:070)	(2:810)	(1:814)	(1:364)	(1:010)	(1:280)	(0:692)	(0:443)	(0:226)	(3:091)	(2:058)	(1:527)	(1:147)
P2 _t	0:688	1:328		2:619	0:236	0:489	0:893	1:224	0:441	0:838	1:279	1:636	0:151	0:303	0:553	0:752
	(3:351)	3:291) (3:789)	(1:338)	1:413) (1:808) (1:994)	(3:720)	3:657)	3:924) (4:071)	(1:424)	(1:477)	1:900) (2:048)
	[3:732]	3:709]		4:288]	[1:456] [1:565] [2:019] [2:231]	[4:124] [4:098]	4:413] [4:580]	[1:554]	[1:638] [2:116] [2:284]
$P3_t$	0:782	1:000		1:665	0:118	0:233	0:213	0:382	0:480	0:571	0:811	0:857	0:053	0:217	0:258	0:444
	(1:174)	(0.849)		(0:917)	(0:214)	0:236) (0:166) (0:258)	(1:065)	(0:742)	(0:199)	(0.694)	(0:120)	(0:372) (0:336) (0:474)
	[1:319]	[0:626]		[1:015]	[0:236]	0:260]	0:179] [0:274]	[1:167]	[0:812]	[998:0]	[0:749]	[0:160]	[0:394] [0:349] [0:486]
P4 _t									0:766	2:467	4:004	5:112	0:205	1:431	2:600	3:402
) (886:0)	1:880)	2:396)	2:384)	(0:312)	(1:338) (1:925) (1:982)
] [666:0]	1:871]	2:337] [2:330]	[0:331]	[1:397] [1:960]	2:007]
$P5_t$									4:375	9:333	12:097	11:581	4:424	9:423	12:220	11:730
									(2:185)	(2:573)	(2:405)	(1:858)	(2:967)	(3:534)	(3:322)	(2:540)
									[2:241]	[2:629]	[2:472]	[1:914]	[3:104]	[3:691]	[3:489]	[2:681]
ф ф					1:007	1:872	2:548	3:110					1:005	1:853	2:513	3:061
					(5:958)	(6:370)	(6:649)	(6:542)					(6:575)	(7:100)	(7:135)	(6:892)
					[6:268]	[6:266]	[6:847]	[6:806]					[7:042]	[7:573]	[7:628]	[7:401]
\mathbb{R}^2	0:167	0:156	0:183	0:194	0:422	0:418	0:432	0:436	0:221	0:233	0:255	0:245	0:472	0:486	0:494	0:477
\mathbb{R}^2 due to $\mathfrak{G}_{\mathfrak{t}}$					0:255	0:262	0:250	0:243					0:251	0:253	0:240	0:232

Table IA.B6: In-Sample Tests of Spanning Hypotheses I and II: 1985{2014

The return to an n-year zero-coupon bond from month t to month t + 12 less the month-t yield on a one-year bond is regressed respectively on (i) the t-rst three principal components (PCs) of observed bond yields PC_{1/3,t} (columns 2-5); (ii) PC_{1/3,t} and the SAGLasso macro factor \hat{G}_t (columns 6-9); (iii) the Itered rst ve PCs of noise-uncontaminated yields PC_{1/5,t} (columns 10-13); and (iv) PC_{1/5,t} and \hat{G}_t (columns 14-17). Test statistics are computed using the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses), or the Newey and West (1987) HAC covariance estimator (in brackets). The sample spans the period January 1985 to December 2014.

(1)	(2)	(3)	(4)	(5)	(9)	(7)	(8)	(6)	(10)	(11)	(12)	(13)	(14)	(15)	(16)	(17)
					Spa	Spanning Hypothesis	oothesis I						Spa	Spanning Hypothesis I	othesis II	
maturity n (year)	7	വ	7	10	7	2	7	10	2	2	7	10	7	വ	7	10
P _{1;t} (P _{1;t})	6:268	11:951	15:082	19:997	6:160	11:544	14:522	19:305	2:877	7:345	10:466	14:210	2:482	5:863	8:469	11:699
	(2:172) [2:439]	(1:168)	(0:979) ((1:001) [1:119]	(3:629)	(2:066)	(1:564) [1:720]	(1:511) [1:672]	(2:385)	(1:701)	(1:618) [1:827]	(1:631)	(3:939)	(2:794)	(2:270)	(2:193)
$P_{3,t}^{(P_{2;t})}$	0:274	1:450	2:255	3:210	0:039	0:568	1:043	1:711	0:107	0:709	1:281	1:662	0:003	0:294	0:722	096:0
ì	(1:279) (2:013)	2:331) (2:850)	(0:223)	(1:024)	1:466) (2:194)	(1:269)	(2:369)	3:020)	3:101)	(0:041)	(1:247)	2:188) (2:532)
	[1:468] [2:292]	2:626] [3:179]	[0:253]	[1:160]	1:635]	2:410]	[1:416]	[2:646]	3:359] [3:407]	[0:046]	[1:408]	2:463] [2:819]
$P_{3;t}^{o}(P_{3;t})$	0:187	0:525	1:867		0:244	0:311	1:573	1:954	0:022	0:295	1:253	0:885	0:003	0:203	1:129	0:729
	(0:524) (0:439) ((0:524) (0:439) (1:146) ((1:096)) (968:0)	1:457) (1:445)	(00:100)	(0:428)	1:483) (0:783)	(0:016)	(0:356)	1:626) (0:952)
	[0:561]	0:469] [1:203]		[1:215]	0:446]	1:601]	1:625]	[0:103]	0:439]	1:481] [[977:0]	[0:017]	0:389]	1:725] [1:031]
P4;t									0:222	0:302	0:388	0:297	0:152	0:041	0:033	0:150
									(0:757)	(0:313)	0:291) (0:183)	(0:647)	(0:054)	0:031)	(0:122)
									[0:835]	0:345]	0:320]	0:201]	[0:711]	[0:059]	0:034	[0:134]
P _{5;t}									1:023	2:230	0:790	0:356	0:810	1:657	0:018	0:615
									(2:101)	(1:573)	(0:36)	(0:136)	(2:038)	(1:456)	(0:011)	0:308)
									[2:164]	[1:451]	[0.359]	[0:122]	[2:199]	[1:391]	[0:010]	0:280]
Φ					0:713	2:677	3:679	4:553					0:693	2:605	3:512	4:414
					(6:419)	(6:330)	(5:576)	(5:221)					(6:480)	(6:225)	(5:551)	(5:278)
					[6:822]	[6:841]	[6:014]	[5:636]					[6:819]	[6:674]	[5:945]	[5:676]
\mathbb{R}^2	0:140	0:142	0:170	0:206	0:393	0:439	0:448	0:471	0:184	0:176	0:225	0:240	0:417	0:450	0:472	0:483
\mathbb{R}^2 due to \mathbf{G}_{t}					0:253	0:297	0:278	0:265					0:232	0:274	0:247	0:243

Table IA.B7: Tests of Spanning Hypotheses Using Macroeconomic Variables with Di erent Lags

The benchmark model in tests of Spanning Hypothesis I is based on the rst three principal components (PCs) of observed bond yields and, in tests of Spanning Hypothesis II, is based on the Itered 1st ve PCs of noise-uncontaminated yields. The columns labeled \HH" report test statistics based on the Hansen and Hodrick (1980) GMM covariance estimator, and the columns labeled NNW" report their counterparts based on the Newey and West (1987) HAC covariance estimator. \ENC-REG" denotes the out-of-sample t-statistics proposed by Ericsson (1992), This table reports both the in-sample and out-of-sample tests of spanning hypotheses, using macroeconomic variables with 0, 3, 6, 9, or 12 lags. and \ENC-NEW" represents a variant of the ENC-REG statistic proposed by Clark and McCracken (2001). The rows labeled \setminus R^2 " (R^2_{oos}) represent the incremental in-sample (out-of-sample) R^2 due to G. The sample spans the period January 1964 to December 2014.

Lags HH NW R2 HH NW R2 ENC-REG ENC-NEW R5 Panel A: Tests of Spanning Hypotheses I 6.711 7.021 0.240 6.136 6.394 0.194 5.168 151.150 0.299 4.548 103.117 0 0 6.425 6.845 0.280 6.414 6.716 0.239 4.570 221.703 0.331 3.761 156.355 0 9 7.449 7.68 0.256 6.542 6.809 0.243 4.764 191.912 0.349 4.511 147.103 0 12 6.947 7.649 7.044 7.033 0.224 4.764 191.912 0.349 4.506 151.385 0 12 6.947 7.649 7.046 7.03 0.244 5.420 236.068 0.325 4.586 236.068				In-sample	e tests				J	Out-of-sample tests	nple tests		
HH NW R2 ENC-REG ENC-NEW R20s ENC-REG ENC-NEW 6.136 6.394 0.194 5.168 151.150 0.299 4.548 103.117 6.414 6.716 0.239 4.570 221.703 0.349 4.871 147.103 7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.20 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.416	SUS	2-y	ear bond		5-y ₁	ear bond		2	-year bond		5	-year bond	
6.136 6.394 0.194 5.168 151.150 0.299 4.548 103.117 6.414 6.716 0.239 4.570 221.703 0.331 3.761 156.355 6.542 6.809 0.243 4.764 191.912 0.349 4.871 147.103 7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.277 4.916 230.903 0.330 3.717 136.416) D	표	NN	R^2	표	MN	R^2	ENC-REG	ENC-NEW	R_{00s}^2	ENC-REG	ENC-NEW	R_{00s}^2
6.136 6.394 0.194 5.168 151.150 0.299 4.548 103.117 6.414 6.716 0.239 4.570 221.703 0.331 3.761 156.355 6.542 6.809 0.243 4.764 191.912 0.349 4.871 147.103 7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.758 7.270 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 4.781 180.940 0.353 4.526 130.102 7.982 8.048 0.210 4.916 230.903 0.330 3.717 136.416	Panel A: Te	ests of Span	Ining Hyp	otheses I									
6.414 6.716 0.239 4.570 221.703 0.331 3.761 156.355 6.542 6.809 0.243 4.764 191.912 0.349 4.871 147.103 7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	0	6.711	7.021	0.240	6.136	6.394	0.194	5.168	151.150	0.299	4.548	103.117	0.205
6.542 6.809 0.243 4.764 191.912 0.349 4.871 147.103 7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.775 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	3	6.425	6.845	0.280	6.414	6.716	0.239	4.570	221.703	0.331	3.761	156.355	0.228
7.104 7.033 0.225 3.481 163.430 0.211 2.935 98.113 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	9	5.958	6.268	0.255	6.542	608.9	0.243	4.764	191.912	0.349	4.871	147.103	0.271
6.795 7.170 0.244 5.420 236.068 0.325 4.606 151.385 6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	6	7.449	7.634	0.289	7.104	7.033	0.225	3.481	163.430	0.211	2.935	98.113	0.104
6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	12	6.947	7.367	0.305	6.795	7.170	0.244	5.420	236.068	0.325	4.606	151.385	0.206
7.918 0.226 6.758 7.220 0.176 4.928 135.506 0.296 4.389 83.981 7.617 0.265 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.042 0.251 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 9.081 0.274 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 8.863 0.289 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	Panel B: Te	ests of Span	Ining Hyp	otheses II									
7.617 0.265 7.004 7.455 0.223 5.286 243.125 0.387 3.861 150.602 7.042 0.251 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 9.081 0.274 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 8.863 0.289 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	0	7.392	7.918	0.226	6.758	7.220	0.176	4.928	135.506	0.296	4.389	83.981	0.186
7.042 0.251 6.892 7.401 0.232 4.781 180.940 0.353 4.526 130.102 9.081 0.274 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 8.863 0.289 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	3	7.059	7.617	0.265	7.004	7.455	0.223	5.286	243.125	0.387	3.861	150.602	0.239
9.081 0.274 7.982 8.048 0.210 3.656 152.386 0.204 2.835 82.606 8.863 0.289 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	9	6.575	7.042	0.251	6.892	7.401	0.232	4.781	180.940	0.353	4.526	130.102	0.256
8.863 0.289 7.748 8.314 0.227 4.916 230.903 0.330 3.717 136.416	6	8.931	9.081	0.274	7.982	8.048	0.210	3.656	152.386	0.204	2.835	82.606	0.073
	12	8.444	8.863	0.289	7.748	8.314	0.227	4.916	230.903	0.330	3.717	136.416	0.186

Table IA.C1: Estimates of Parameters on the Market Price of Risk

This table reports the maximum likelihood estimates of parameters λ_0 and λ_1 that govern bond risk premia in an \mathcal{N} -factor constrained, spanned macro- nance term structure model (MTSM) as specified and denoted $CSM(\mathcal{L},\mathcal{N})$ in Section IA.G.1. The underlying state variables include the SAGLasso macro factor, \widehat{G} , constructed in Section 4.1 and the first \mathcal{L} principal components (PCs) of bond yields, $PC_1 = (PC_1, \ldots, PC_L)$. The three MTSMs considered include CSM(3,4) (panel A), CSM(4,5) (panel B), and CSM(5,6) (panel C). The one-period risk premium is as specified in Eq. (13): $t = \lambda_0 + \lambda_1 X_t = \lambda_0 + \lambda_1 \cdot (PC_1 - \mathcal{L}_{/t}, \widehat{G}_t)^{\emptyset}$. Zero entries of λ_0 and λ_1 refect our model selection outcome. Values in parentheses are standard errors computed using Monte Carlo simulations.

				λ_1 ($\mathcal N$	$\times \mathcal{N})$		
State variables	λ_0	$\lambda_1(\cdot,\mathcal{N})$	$\lambda_1(\cdot,1)$	· 	•••		$\lambda_1(\cdot,5)$
variables		\widehat{G}_t	$PC_{1;t}$	$PC_{2;t}$	$PC_{3;t}$	PC _{4;t}	PC _{5;t}
Panel A:	Model CS/	M(3,4)					
$PC_{1;t}$	0.013 (0.002)	-6.11e-04 (8.97e-05)	-0.054 (0.016)	-0.313 (0.087)	0		
$PC_{2;t}$	0.002 (9.31e-04)	-1.45e-04 (7.12e-05)	0	0	-0.458 (0.0143)		
$PC_{3;t}$	0	0	0	0	0		
\widehat{G}_t	-0.278 (0.152)	-0.159 (0.081)	0.093 (0.035)	0	0		
Panel B:	Model CSA	Λ (4,5)					
$PC_{1;t}$	0.018 (0.003)	-8.13e-04 (9.04e-05)	-0.049 (0.007)	-0.152 (0.060)	0	0	
$PC_{2;t}$	0.002 (0.001)	-1.32e-04 (9.13e-05)	0	-0.031 (0.035)	-0.129 (0.139)	0.140 (0.148)	
$PC_{3;t}$	0	0	0	0	0	0	
$PC_{4;t}$	0	0	0	0	0	0	
\widehat{G}_t	0	0	-0.633 (0.243)	0	0	-8.77 (4.871)	
Panel C:	Model CSA	Λ (5, 6)					
$PC_{1;t}$	0.029 (0.003)	-6.47e-04 (8.76e-05)	-0.048 (0.009)	-0.173 (0.076)	0	0	-0.708 (0.259)
$PC_{2;t}$	0	-2.60e-04 (9.26e-05)	0	0	-0.207 (0.102)	0.098 (0.115)	0
$PC_{3;t}$	0	0	0	0	0	0	0
$PC_{4;t}$	0	0	0	0	0	0	0
$PC_{5;t}$	0	0	0	0	0	0	0
â							

Table IA.D1: Finite-Sample Properties of Statistics in Testing Spanning Hypothesis I under a VAR-based Data-Generating Process

This table presents results based on nite-sample distributions of the statistics that are involved in tests of Spanning Hypotheses I stated in Section 2.2. The analysis is based on 5,000 bootstrapped samples generated from the reduced-form VAR described in Eqs. (IA.D4) and (IA.D5) (panels A1 through B2) or from the macro- nance term structure model MIM(3,4) (panels A3 through B4) that satis es the \macro-independence restrictions" given in Eq. (IA.D9). The length of each bootstrapped sample is set to be consistent with either the full sample (panel A) or the post-1984 subsample (panel B). Test statistics considered include those computed using the Hansen and Hodrick (1980) GMM covariance estimator (HH), the Newey and West (1987) HAC covariance estimator (NW) with 18 lags, the out-of-sample ENC-REG test of Ericsson (1992), or the out-of-sample ENC-NEW test of Clark and McCracken (2001). For each test statistics, the 95th percentile of the bootstrap distribution is reported as the 5% critical value, and the p-values (in angle brackets) are the frequency of bootstrap replications in which the test statistics are at least as large as the statistic in the data. The \ R^2 " and \ R^2 " and \ R^2 " measures denote the

Table IA.E1: Ibragimov-Muller Test of Spanning Hypotheses I and II

The average return to zero-coupon bonds from month t to month t+12 less the month-t yield on a one-year bond is regressed on either $PC_{1-3;t}^{o}$ and \hat{G}_{t} for Spanning Hypothesis I (H_{0}^{S1}) or $PC_{1-5;t}$ and G_{t} for Spanning Hypothesis II (H_{0}^{S2}) , where $PC_{1-3;t}^{o}$ denotes the rst three principal components (PCs) of observed bond yields; $PC_{1-5;t}$ the Itered rst ve PCs of noise-uncontaminated yields; and \hat{G}_{t} the SAGLasso single factor. All reported quantities are the p-values for the Ibragimov-Meller (2010) test of the individual signic cance of the coe-cients. The dependent variable is the excess return averaged over 2- through 5-year (10-year) bond maturities in regressions over the full sample period 1964{2014} (the post-1984 subsample). In the full-sample analysis, each block is constructed such that they are 12 months apart from each other.

			Spa	anning Hy	pot	theses Te	sted		
	H	<i>I</i> ₀ S1	H	I_0^{S2}		H	<i>S</i> 1 0	H	<i>S</i> 2 0
	Fı	ull sample	, 1964{2	014		S	ubsample,	, 1985{20)14
q (# of blocks)	q = 8	<i>q</i> = 16	<i>q</i> = 8	<i>q</i> = 16		<i>q</i> = 8	<i>q</i> = 16	<i>q</i> = 8	<i>q</i> = 16
$PC_{1:t}^{o}(PC_{1:t})$	0.039	0.001	0.006	0.003		0.219	0.417	0.001	0.001
$PC_{2:t}^{o}(PC_{2:t})$	0.016	0.009	0.327	0.047		0.020	0.006	0.036	0.379
$PC_{3:t}^o(PC_{3:t})$	0.162	0.354	0.309	0.615		0.037	0.647	0.536	0.743
$PC_{4;t}$			0.186	0.961				0.278	0.942
$PC_{5;t}$			0.170	0.107				0.002	0.002
\mathfrak{G}_t	0.009	0.018	0.004	0.014		0.044	0.049	0.015	0.019

Table IA.F1: Tests of An Alternative Version of Spanning Hypotheses II

This table presents asymptotic and nite-sample results from tests of an alternative version of Spanning Hypothesis II, denoted $H_0^{S2;cf}$, that states that the SAGLasso macro factor (Section 4.2) has no additional predictive power for future excess bond returns, conditional on the \cycle" factor of Cieslak and Povala (2015). The tests of $H_0^{S2;cf}$ are based on the following regression, as specified in Eq. (IA.F11):

$$rx_{t;t+12}^{(12n)} = \alpha + \beta_c^{\ell} \widehat{cf}_t + \beta_g^{\ell} \widehat{G}_t + e_{t+12},$$

where $rx_{t:t+12}^{(12n)}$ is the excess return to an n-year zero-coupon bond from month t to month t+12, for n=2,5,7,10; \widehat{cf}_t denotes the cycle factor; and \widehat{G}_t the SAGLasso macro factor. For the insample results (panel A), t-statistics are computed using either the Hansen and Hodrick (1980) GMM covariance estimator (in parentheses) or the Newey and West (1987) HAC covariance estimator (in brackets). Out-of-sample tests considered (panel B) include the \ENC-REG" test of Ericsson (1992) and the \ENC-NEW" test proposed by Clark and McCracken (2001). The R^2 and R^2 measures denote the incremental R^2 and out-of-sample R^2 of Campbell and Thompson (2008), respectively, due to augmenting univariate regressions of $rx_{t;t+12}^{(12n)}$ on \widehat{cf}_t with \widehat{G}_t as in the above equation. The sample spans the period November 1971{December 2014. To obtain the nite-sample distributions of the aforementioned six statistics, 5,000 bootstrapped samples are generated from the term structure model speci ed in Eqs. (IA.F12){(IA.F14) in Section IA.F. For each set of test statistics, the 95th percentile of the bootstrap distribution is reported and underlined as the 5% critical value, and the p-values (in angle brackets) are the frequency of bootstrap replications in which the test statistics are at least as large (small) as the statistic in the data.

maturity (year)	2	5	7	10		2	5	7	10
	Panel A	A: In-sam	ple under	$H_0^{S2,cf}$		Panel B	Out-of-sa	ample und	$\text{ler } H_0^{S2,cf}$
\widehat{G}_t	0.688	2.491	3.376	4.153					
HH	(4.257)	(4.994)	(4.537)	(4.367)	ENC-REG	1.917	3.099	3.620	4.513
	(<u>1.964</u>)	(<u>2.121</u>)	(<u>2.601</u>)	(2.890)		(<u>1.617</u>)	(<u>2.675</u>)	(3.837)	(4.067)
	⟨0.001⟩	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$		$\langle 0.033 \rangle$	$\langle 0.026 \rangle$	$\langle 0.066 \rangle$	$\langle 0.029 \rangle$
NW	[4.684]	[5.506]	[4.953]	[4.735]	ENC-NEW	41.321	77.762	80.203	77.102
	[1.872]	[2.120]	[2.588]	[2.857]		[1.374]	[4.429]	[9.080]	[10.746]
	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$		$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$
R^2	0.132	0.144	0.131	0.124	R_{oos}^2	0.053	0.143	0.132	0.103
	(0.011)	(0.032)	(0.062)	(0.072)		(<u>0.010</u>)	(<u>0.033</u>)	(<u>0.065</u>)	(<u>0.075</u>)
	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.001 \rangle$		$\langle 0.000 \rangle$	$\langle 0.000 \rangle$	$\langle 0.001 \rangle$	$\langle 0.009 \rangle$

Table IA.G1: Out-of-sample Forecasting Performance of Macro-Finance Term Structure Models

models (MTSMs). Forecasted yields include the 0.5-, 1-, 3-, 5-, 7-, and 10-year yields. The forecast horizons considered are 1, 3, 6, and 12 months. The four MTSMs | denoted by SM(\mathcal{L}, \mathcal{N}), USM(\mathcal{L}, \mathcal{N}), and CUSM(\mathcal{L}, \mathcal{N}) | are all driven by six factors ($\mathcal{N}=6$), including the macro-unspanning conditions (H_0^{US}) speci ed in Eq. (12). Each of the four MTSMs is estimated once using the 1985-2007 sample. The This table reports the root mean square errors (RMSEs) for out-of-sample yield forecasts formed from four di erent macro- nance term structure ve yield curve factors ($\mathcal{L}=5$) and the sole SAGLasso macro factor (\widehat{G}_t). Among the four models, SM (5,6) and USM (5,6) are unconstrained models (panel A), and CSM (5,6) and CUSM (5,6) are constrained models (panel B), in which selected zero restrictions are placed on parameters governing bond risk premia. Additionally, while models SM (5,6) and CSM (5,6) are spanned, the other two are unspanned models that satisfy Kalman Iter is implemented recursively with observations from 1985.1 to the time that the forecast is made, beginning in 2008:1 and extending through 2014:12. Errors are reported in basis points of annualized yields.

					ו מוכן א. סמר טי זמווויסור ואויטבא וסו מווכטואנו מוויכע וווסמכוא							
-orecast	y	$y^{(6)}$	y	y ⁽¹²⁾	$y^{(}$	$y^{(36)}$	y	$y^{(60)}$	y	$y^{(84)}$	$y^{()}$	y ⁽¹²⁰⁾
norizon	SM (5, 6)	USM (5, 6)	SM (5, 6)	USM (5, 6)	SM (5, 6)	USM (5, 6)	SM (5, 6)	USM (5, 6)	SM (5, 6)	USM (5, 6)	SM (5, 6)	USM (5, 6)
	25.40	24.32	21.08	20.71	25.62	25.72	27.50	26.79	30.05	29.26	32.29	31.66
	48.19	46.31	48.30	45.96	54.07	54.98	53.50	54.37	51.95	50.65	48.77	51.97
	80.27	74.93	81.44	76.26	84.47	85.86	81.61	84.27	76.98	78.20	69.34	73.90
	139.51	128.08	142.04	130.69	133.32	128.10	114.04	112.76	99.78	99.73	82.13	89.99
- -orecast	y	y ⁽⁶⁾	y	y ⁽¹²⁾	Panel B: Ou	Panel B: Out-of-sample RMSEs for constrained models $y^{\rm (36)}$	ISEs for constr	$y^{(60)}$	y	$y^{(84)}$	y	y(120)
norizon	CSM (5, 6)	CUSM (5, 6)	CSM (5, 6)	CUSM (5, 6)	CSM (5, 6)	CUSM (5, 6)	CSM (5, 6)	CSM (5,6) CUSM (5,6)	CSM (5, 6)	CUSM (5, 6)	CSM (5, 6)	CUSM (5, 6)
	24.15	27.73	20.00	20.63	25.01	24.86	26.08	26.08	28.71	43.32	30.54	30.63
	45.77	46.85	45.89	43.75	51.84	48.78	50.92	49.41	48.77	52.60	46.23	46.15
	74.83	66.69	74.63	63.74	79.10	68.63	79.22	72.83	74.17	63.69	67.11	59.98
	102.13	95.51	104.02	81.35	116.20	87.04	115.87	91.30	109.84	69.34	92.13	66.01

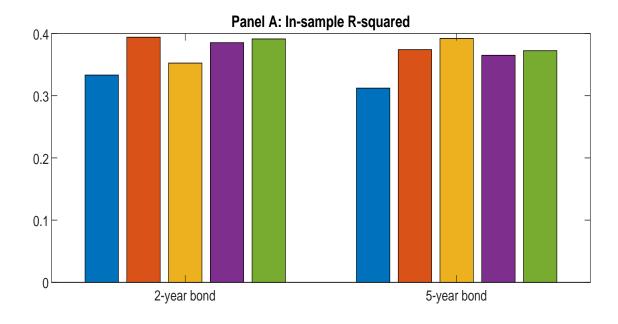
Table IA.G2: Properties of Annual Excess Returns for Five-Year Bonds Implied by Term Structure Models with Unspanned Macro Risks

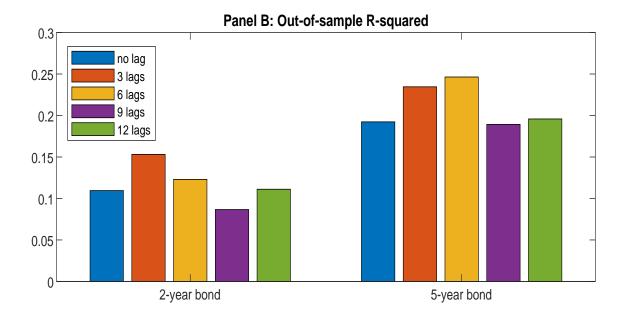
This table presents the model-implied population moments of unconditional and conditional excess returns on a ve-year bond, based on the macro- nance term structure model $CUSM(\mathcal{L},\mathcal{N})$ speci ed in Section IA.G.1. Model $CUSM(\mathcal{L},\mathcal{N})$ is an \mathcal{N} -factor model with unspanned macro risks and \zero restrictions" imposed on risk premium parameters, whose underlying state vector $X_t = (PC_{1-L:t}, G_t)$, where $PC_{1-L:t}$ represent the rst \mathcal{L} principal components (PCs) of the true yields and G_t the (unspanned) SAGLasso macro factor. The last six columns quantify the variance of true conditional expected excess returns attributable to time variation in the true state vector X_t (column 4), the rst three PCs of observed yields (column 5), the rst three PCs of true yields (uncontaminated by measurement errors) (column 6), the rst \mathcal{L} PCs of observed yields (column 7), the rst \mathcal{L} PCs of true yields (column 8), and the rst three yield PCs plus the SAGLasso factor G_t (column 9), respectively. For each of the last vecolumns, their ratios to the full-information variance (column 4) | the variance ratios \VR" | are reported in braces. The R^2 reported for each of the last three columns is their ratios to the total variance (column 3). The sample period extends from January 1985 to December 2007.

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
\mathcal{L}	Mean	Total Variance	Variance of conditional expectation based on					
			Full info	$PC_{1-3,t}^{o}$	$PC_{1-3,t}$	$PC_{1-\mathcal{L},t}^{o}$	$PC_{1-\mathcal{L},t}$	$PC_{1-3,t}$

Figure IA.B1: Predictive \mathbb{R}^2 of Macroeconomic Factors Based on Di erent Lags

This gure depicts the in-sample and out-of-sample \mathbb{R}^2 from bond return predictions with single macroeconomic factors. Macroeconomic factors are constructed from 131 macro variables, along with 0, 3, 6, 9, or 12 of their lags. The sample spans the period January 1964 to December 2014.





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